

## Joint inversion of ReMi dispersion curves and refraction travel times using particle swarm optimization algorithm

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### Abstract

Shear-wave velocity ( $V_S$ ) is an important parameter used for site characterization in geotechnical engineering. However, dispersion curve inversion is challenging for most inversion methods due to its high non-linearity and mix-determined trait. In order to overcome these problems, in this study, a joint inversion strategy is proposed based on the particle swarm optimization (PSO) algorithm. The seismic data considered for designing the objects are the Rayleigh wave dispersion curve and seismic refraction travel time. For joint inversion, the objective functions are combined into a single function. The proposed algorithm is tested on two synthetic datasets, and also on an experimental dataset. The synthetic models demonstrate that the joint inversion of Rayleigh wave and travel time return a more accurate estimation of  $V_S$  in comparison with the single inversion Rayleigh wave dispersion curves. To prove the applicability of the proposed method, we apply it in a sample site in the city of Tabriz located in the NW of Iran. For a real dataset, we use refraction microtremor (ReMi) as a passive method for getting the Rayleigh wave dispersion curves. Using the PSO joint inversion, a three-layer subsurface model was delineated. The results obtained for the synthetic datasets and field dataset show that the proposed joint inversion method significantly reduces the uncertainties in the inverted models, and improves the revelation of boundaries.

**Keywords:** Shear Wave, Joint Inversion, Remi, Particle Swarm Optimization, Travel Time.

### 1. Introduction

Seismic surveying techniques provide relevant data regarding soil behavior at a very low strain level for large portions of soil, tested in an undisturbed state using the procedures that are time- and cost-effective [1]. Shallow shear-wave velocity ( $V_S$ ) has long been recognized as a key factor in variable ground-motion amplification and site response in sedimentary basins [2]. The velocity profiles together with the depth of the basement below the sediments are the useful data used in geotechnical studies for the correct construction of buildings [3]. The  $V_S$  structure is important in site-effect studies and geotechnical engineering, but it is quite difficult and expensive to derive it from the conventional geophysical techniques [4]. The current techniques of estimating shallow shear-wave velocities for

assessment of earthquake site responses are too costly for use at most construction sites [5].

The refraction microtremor (ReMi) method [5] is a passive-source multi-channel method that uses a linear array configuration. This method provides effective and efficient means to obtain the general information about large volumes of the subsurface in one dimension per setup, where the appropriate setup length is related to the desired depth of investigation [6]. ReMi is based on obtaining the dispersion curve for the Rayleigh waves, but in this case, using the ambient seismic noise or microtremor. For the processing procedure, as for the other surface wave methods, after construction of the dispersion curves, the next step is the inversion of the dispersion curve to obtain a single  $V_S$  profile. The inversion stage in processing the ReMi data, due to its non-

linearity and multi-dimensionality, is an important issue to achieve a reliable  $V_s$  profile.

Surface wave inversion is strongly non-linear, ill-posed, and mix-determined, and this leads to strong solution non-uniqueness, as evidenced by several authors [1]. In order to overcome these problems, constraining the interpretation, and decreasing the uncertainty in estimating the structures was proposed, which is based upon the PSO algorithm. Inverting the recorded data sets separately may lead to incorrect interpretation of an underground structure, i.e. for an underground model with a high-velocity layer overlying a low velocity layer, neither refraction nor reflection seismic alone is able to resolve the parameters of the low-velocity layer [7]. The information required for the water table, bed rock, and layer interface can be obtained using the refraction seismic, whereas dispersion curves do not give any information about the number of layers, while the refraction travel times, in principle, could [8]. Therefore, it is possible, by integration of the surface waves and refraction travel time, to reduce the intrinsic weakness of each method.

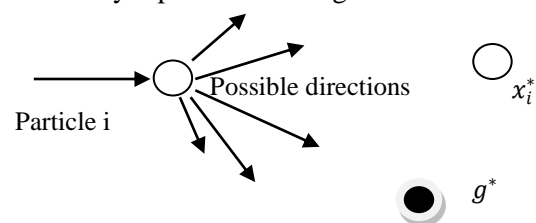
For joint inversion by particle swarm optimization (PSO) algorithm, we used the global criterion method, in which all misfit functions (i.e. objective functions) were combined to form a single function. By finding the global minimum of the misfit function, the best solution to a problem could be obtained. PSO algorithm is one of the global optimization methods that belong to a group of metaheuristic searching algorithms. In geophysical surveys, several significant PSO applications have recently been emerged. Fernández Martínez et al. [9] have presented the application of a whole family of PSO algorithms to analyze and solve a VES inverse problem associated with a seawater intrusion in a coastal aquifer in southern Spain. Pekşen et al. [10] have inverted the self-potential (SP) data by the application of PSO algorithm. Poormirzaee et al. [11] have proposed the seismic travel time inversion scheme based on the particle swarm optimization technique. Recently, Zarean et al. [12] have presented the application of mutation-based PSO algorithms to analyze the surface wave dispersion curves using the microtremor records. The proposed joint inversion algorithm was written and processed in MATLAB, and tested on the synthetic datasets. Finally, the reliability of the PSO joint inversion was investigated in a sample site in Tabriz located in the NW of Iran in order to study the site effect. The results obtained for both the synthetic and real datasets were compared

with the single PSO inversion of ReMi data, and also with a multi-objective optimization algorithm, non-dominated sorting genetic algorithm-II (NSGA-II).

## 2. Methodology

### 2.1. Particle Swarm Optimization (PSO)

PSO is a stochastic evolutionary computation optimization technique used in many engineering fields. It is inspired by the social behavior of the individuals (called particles) in groups in nature like a flock (swarm) of birds searching for food [13]. This algorithm searches the space for an objective function by adjusting the trajectories of individual agents, called particles, as these trajectories form piecewise paths in a quasi-stochastic manner [14]. The particles move toward promising regions of the search space by exploiting information springing from their own experience during the search as well as the experience of other particles. For this purpose, a separate memory was used, where each particle stores the best position ( $x_i^*$ ) it has ever visited in the search space. The best position of each particle experience the other comprised ones, and then the best position, which belongs to a minimum of misfit function, selected as the global best ( $g^*$ ). This procedure (i.e. finding  $x_i^*$ ,  $g^*$ ) was repeated for a certain iteration. Finally, the best global  $g^*$  was determined as the optimum solution. The movement of particles was schematically represented in Figure 1.



**Figure 1. Schematic representation of motion of a particle in PSO, moving towards global best  $g^*$  and current best  $x_i^*$  for each particle [14].**

Particle swarm consists of a swarm of particles, each moving or flying through the search space according to the velocity update Eq.1 [13]. The velocity of each particle was modified iteratively by its personal best position, and the best position was found by the particles in its neighborhood.  $v_i$  is the velocity of the  $i$ th particle in the swarm,  $x_i$  is the particle position,  $x_i^*$  denotes the personal best position, and  $g^*$  is the best position found by particles in its neighborhood.

$$v_i^{t+1} = v_i^t + \alpha\epsilon_1 \odot (g^* - x_i^t) + \beta\epsilon_2 \odot (x_i^* - x_i^t) \quad (1)$$

In Eq. 1,  $\epsilon_1$  and  $\epsilon_2$  are two random vectors and each entry takes a value between 0 and 1. The Hadamard product of the two matrices  $u \odot v$  is defined as the entry-wise product. The parameters  $\alpha$  and  $\beta$  are the learning parameters or acceleration constants, which can typically be taken as, say,  $\alpha \approx \beta \approx 2$  [14].

The initial locations of all particles should distribute relatively uniformly so that they can sample over most regions, which are especially important in multimodal problems. The initial velocity of a particle can be taken as 0, i.e.  $v_i^{t=0} = 0$ . The new position can then be updated by Eq. 2 [14].

$$x_i^{t+1} = x_i^t + v_i^{t+1} \quad (2)$$

A number of variations have been proposed on the original PSO to overcome its shortcomings and drawbacks such as slow convergence and wandering near the global minimum in the final stage of the search. One of the most notable steps in these formulations is the introduction of an inertia weight by Shi and Eberhart [15]. An inertia term (i.e. static inertia weight),  $\omega \in (0,1)$ , was introduced into the original PSO velocity rule, as follows:

$$v_i^{t+1} = \omega v_i^t + \alpha \epsilon_1 \odot (g^* - x_i^t) + \beta \epsilon_2 \odot (x_i^* - x_i^t) \quad (3)$$

So long as  $\omega \in (0,1)$ , Eq. 3 helps the particles forget their lower-quality past positions in order to be more affected by the higher-quality information of late, which seems to make more sense conceptually [16].

For  $\omega$ ,  $\alpha$ , and  $\beta$ , there are several popular parameter sets in the literature (Table 1). Another

notable recent variation in the original PSO algorithm is the introduction of the so-called constriction factor by [17]. This method introduces a constriction factor  $\chi \in (0,1)$  into the original velocity rule (i.e. Eq. 1), which has the effect of reducing the velocity of the particles as the search progresses, and thereby contracting the overall swarm diameter. This, in turn, results in a progressively smaller domain being searched [18]. Applying a constriction factor into PSO improves the convergence of the particles (Eq. 4). The other parameters used in different studies are listed in Table 1.

$$v_i^{t+1} = \chi [v_i^t + \alpha \epsilon_1 \odot (g^* - x_i^t) + \beta \epsilon_2 \odot (x_i^* - x_i^t)] \quad (4)$$

Using the constriction factor seems to be superior to the introduction of the inertia term (for more information, see [16]).

Another feature of the PSO algorithm is the velocity clamping, which is important for its improvement. Eberhart and Kennedy have introduced velocity clamping, which helps particles take reasonably sized steps in order to comb through the search space rather than bouncing almost excessively [16].

Like other evolutionary algorithms, the difficulty in escaping from the local optimum still exists in PSO. Some researchers have used the mutation operator to make the PSO break away from the local optimum. The PSO algorithm with mutation operator not only has great advantages of convergence property but also can avoid the premature convergence problem [19].

**Table 1. Proposed PSO parameter sets in different references.**

No. Set	PSO parameters				Reference
	$\alpha$	$\beta$	$\chi$	$\omega$	
1	1.300	2.800	0.7298	-	Schutte and Groenwold [20]
2	2.050	2.050	0.7290	-	Evers [16]
3	0.948	2.041	-	0.729	Carlisle and Dozier [21]
4	1.700	1.700	-	0.600	Trelea [22]
5	1.494	1.494	-	0.729	Clerc and Kennedy [23]
6	2.000	1.800	-	0.800	Fernández Martínez et al. [18]

## 2.2. Refraction Microtremor (Remi) And Seismic Refraction Techniques

The ReMi technique is a cheap and quick "passive" geophysical technique. It is based upon the ambient noise measurements that are carried out with seismic arrays to obtain information on the surface wave velocity dispersion. Urban conditions such as the existing underground facilities and ambient noise due to cultural activity restrict the general application of the conventional

geophysical techniques [24]. The ReMi method combines the urban utility and ease of microtremor array techniques with the operational simplicity of the spectral analysis of the surface wave (SASW) technique and the shallow accuracy of the multi-channel analysis of the surface wave (MASW) technique. As for the SASW technique, ReMi is based upon obtaining the dispersion curve of the Rayleigh waves, but in this case, the ambient seismic noise or microtremor is used.

Configurations of 12-48 single vertical, 8-12 Hz exploration geophones can give surface-wave phase velocities at frequencies as low as 2 Hz and as high as 26 Hz. This range is appropriate for constraining the shear velocity profiles from the surface to 100 m depth [5].

After Louei [5], the reliability and accuracy of the ReMi method has been investigated in different case studies. Rucker [6] has applied the ReMi shear-wave technique for the geotechnical characterizations, and several geotechnical applications have been shown in his publication. Scott et al. [25] have performed measurement of the shear-wave velocity to 30 m depth ( $V_{S30}$ ) for the hazard assessment of Reno basin. They were successful in obtaining the detailed shallow shear-wave velocity transect across an entire urban basin with a minimum effort. Coccia et al. [26] have used the ReMi technique for determining the 1D shear-wave velocity in a landslide area, and have concluded that in marginally stable slope areas, the ReMi method can provide the data needed for calculating the shear-wave velocity vertical profiles down to a depth of few tens of meters. This issue can be achieved even using an array shorter than the commonly recommended minimum value of 100 m. Panzera and Lombardo [27] have successfully used the ReMi and MASW techniques to investigate the dynamic properties of the main lithotypes outcropping in the Siracusa region and their relationships with the local seismic response. Poormirzaee and Hamidzadeh [28] applied the ReMi data to study the structure of  $V_S$  in urban areas, while using other active seismic methods was limited.

The seismic refraction surveying method uses the seismic energy that returns to the surface after traveling through the ground along the refracted ray paths. The first arrival of the seismic energy at a detector offset from a seismic source represents either a direct ray or a refracted ray [29]. On the local scale, the refraction surveys are widely used in the foundation studies on the construction sites to derive estimates of the depth to the rock head beneath a cover of the superficial material. Refraction surveys find wide applications in the exploration programs for underground water supplies in sedimentary sequences, often employed in conjunction with the electrical resistivity methods.

In general, the travel time  $t_n$  of a ray, critically refracted along the top surface of the  $n$ th layer, is given by the following relation:

$$t_n = \frac{x}{v_n} + \sum_{i=1}^{n-1} \frac{2z_i \cos \theta_{in}}{v_i} \quad (5)$$

Where

$$\theta_{in} = \sin^{-1}(v_i / v_n)$$

In Eq. 5,  $x$  is the offset distance from shot point,  $v$  is the velocity of layer,  $z$  is the depth of refractor, and  $\sin \theta = v_1 / v_2$  is the Snell's Law [29].

### 2.3. Joint inversion of Rayleigh wave and refraction travel time by PSO

The Rayleigh wave dispersion curves and refraction travel times are jointly inverted through a procedure based on the PSO technique. The main goal of the proposed algorithm is to improve the reconstruction of the subsurface structure by exploiting the complementary information attainable by the Rayleigh wave dispersion and refraction travel times. The Rayleigh wave dispersion inversion procedure was performed using the fundamental mode.

The most important parameters that influence the Rayleigh wave propagation are the shear-wave velocity ( $V_S$ ) and layer thickness, while density ( $\rho$ ) and P-wave velocity ( $V_P$ ) play a minor role [30]. On the other hand, the refraction travel time depends on the longitudinal velocity and thickness. In order to obtain accurate results, in the joint inversion procedure, it was decided to link  $V_P$  and  $V_S$  by means of the Poisson ratio ( $\sigma$ ). In this way, in general, a wide range of Poisson values [0.1, 0.48] is allowed for each layer. Of course, a suitable range of Poisson values depend on the studied area, which can be determined by the primary information. Using Eq. 6 and the above Poisson values, a straight equation was obtained (Eq. 6). For each particle (i.e. the model), the  $V_P$  and  $V_S$  values were checked to detect the  $V_P/V_S$  ratio. If this ratio exceeds the imposed limits, the algorithm for satisfying Eq. 6 generates new random values for  $V_P$  and  $V_S$ .

$$v_p = v_s \left( \frac{\sqrt{1-\sigma}}{\sqrt{\frac{1}{2}-\sigma}} \right) \quad (6)$$

$$1.5 < \frac{v_p}{v_s} < 5 \quad (7)$$

Also the parameter density was fixed according to the classical Gardner et al [31] empirical  $V_P$ - $\rho$  relationship:

$$\rho = \log(0.23 + (kV_P)^{0.25}) \quad (8)$$

Where  $K = 1/0.3048$  is a constant to convert feet to meter.

For the joint inversion of ReMi and seismic refraction data, the summation of the root mean square (RMS) error was considered as the objective function (OBF). In order to solve the forward modeling, and estimate the theoretical dispersion curve, the code based on the matrix algorithm developed by Herrmann [32] was used. The root mean square misfit between the observed and calculated values for velocity was defined as the objective function ( $OBF_1$ ) according to the following equation:

$$OBF_1 = \sqrt{\frac{\sum_{j=1}^{n_p} (v^{obs} - v^{cal})^2}{n_p}} \quad (9)$$

where  $n_p$  is the number of samples,  $v^{obs}$  is the observed phase velocity, and  $v^{cal}$  is the calculated one.

Also the forward algorithm used in the inversion is based on a 1D ray-tracing for the P-wave travel times. The root mean square misfit between the observed and calculated refraction travel times are defined as the object function ( $OBF_2$ ), according to the following equation:

$$OBF_2 = \sqrt{\frac{\sum_{j=1}^{n_p} (t^{obs} - t^{cal})^2}{n_p}} \quad (10)$$

where  $n_p$  is the number of points,  $t^{obs}$  is the observed travel time, and  $t^{cal}$  is the calculated travel time. Also, for the seismic refraction data, the forward algorithm used in the inversion is based on a 1D ray-tracing for the P-wave travel times.

In the joint inversion procedure, the elements of the objective function can have different physical dimensions and various orders of magnitude. Thus to have stable results, normalization is needed [7]. For normalization, the values for the parameters in the objective function are divided into its observed values (Eq. 11).

$$OBF = \sqrt{\frac{(\sum_{j=1}^{n_p} (X^{obs} - X^{cal}))^2}{X^{obs} n_p}} \quad (11)$$

where  $x^{obs}$  is the observed value, and  $x^{cal}$  is the calculated one. The general flowchart of the PSO joint inversion algorithm is shown in Figure 2. We investigated this algorithm in some synthetic and real datasets.

## 2.4. Synthetic Dataset

In order to test the PSO joint inversion algorithm, and evaluate its performance, we considered two synthetic models (A and B). Also for an efficient study of the proposed joint inversion algorithm

(i.e. PSO joint Inv.), the obtained  $V_s$  profile was compared with the estimated  $V_s$  profile of PSO single inversion of ReMi data (i.e. PSO Inv.), and also by the non-dominated sorting genetic algorithm (NSGA-II). In the PSO single inversion approach [33], only the ReMi data was inverted. NSGA-II, Proposed by Deb et al. [34], is a modified version of the non-dominated sorting genetic algorithm (NSGA), proposed by Srinivas and Deb [35]. This algorithm, as a multi-objective optimization algorithm, has been investigated in many literatures [36].

To investigate the PSO joint inversion algorithm, we first considered the 4-layer synthetic model reported in Table 2 (model A). Also the particle and maximum number of iterations were selected to be 80 and 50, respectively. The adopted model was designed in order to reproduce a typical hidden-layer case, which is clearly prone to erroneous refraction travel time interpretation. The dispersion curve and the estimated travel time values are showed in Figures 3a and 3b. Also the mean results obtained for different inversion algorithms for model A are shown in Table 3 and Figure 3c.

The PSO joint inversion method is probed by a four-layer model (model B). Table 4 shows model B and the search space used for inversion. The dispersion curve and the estimated travel time values are showed in Figures 4a and 4b. The mean results obtained for inversion in model B are shown in Table 5 and Figure 4c.

## 2.5. Field Dataset

To further explore the applicability of the PSO joint inversion algorithm described above, the ReMi and seismic refraction data was acquired in the city of Tabriz in the NW of Iran (Figure 5). Then the dataset was reanalyzed in the present study using the PSO joint inversion approach. The data was collected in a profile line. In this study, the ReMi and seismic refraction method was performed using an OYO 24-channal seismograph and 4.5Hz and 28 Hz geophones with a receiver spacing of 5 m. Unfiltered 17 second records were collected at the studied site. Also fourteen records were gathered. The ReMi data processing consisted of three steps: 1) preliminary detection of surface waves 2) extracting the dispersion curve 3) inversion of the dispersion curve. In this study, the module Pickwnin/SW of the commercial software package SeisImager v.3.1 [37] for detection of surface waves and getting dispersion curve was used (Figure 6).

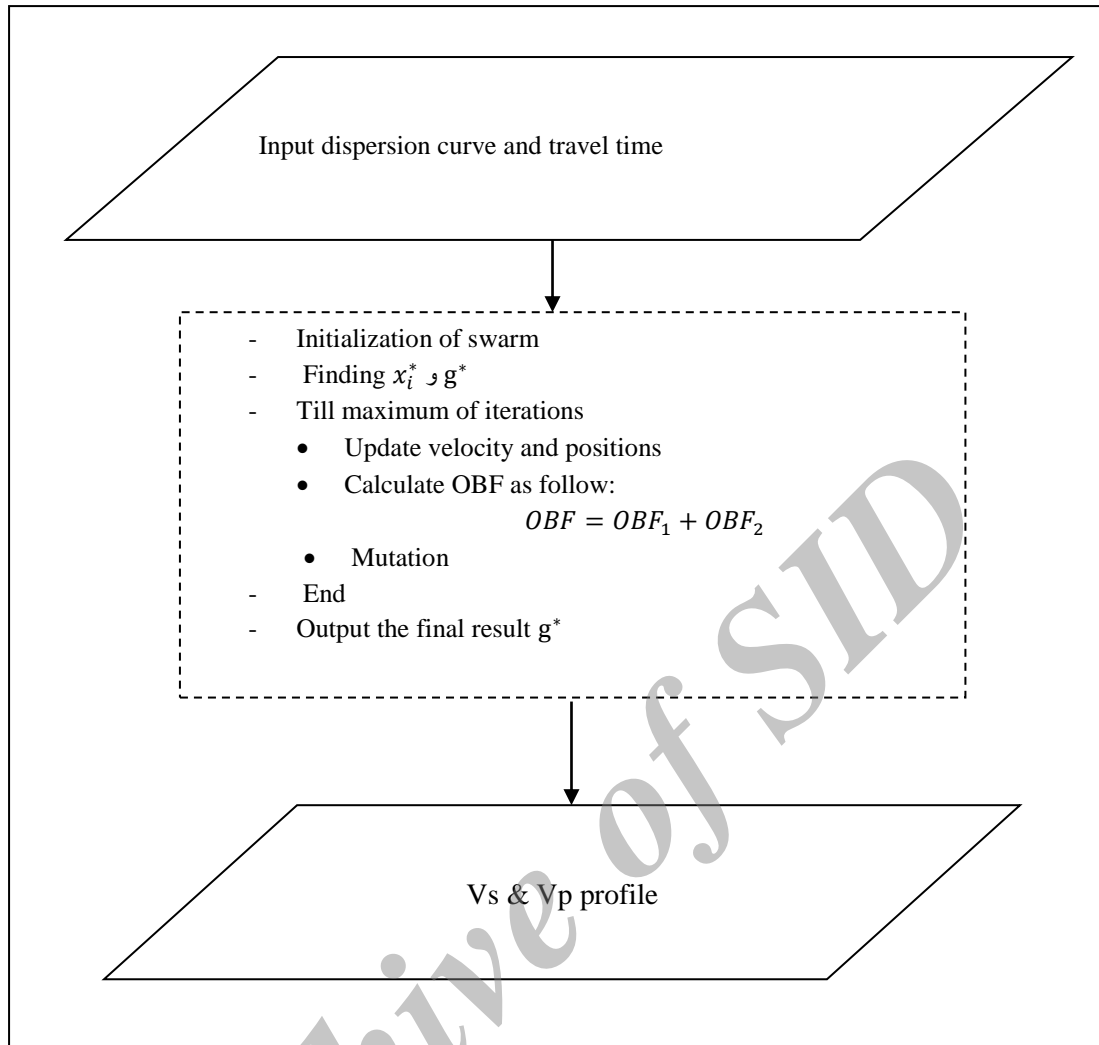


Figure 2. PSO joint inversion algorithm to invert dispersion curve and travel time dataset.

Table 2. Parameters of synthetic model A and search space.

Layer number	$V_S$ (m/s)	$V_P$ (m/s)	H (m)	Search space		
				$V_P$ (m/s)	$V_S$ (m/s)	H (m)
1	190	400	4	200-600	90-300	2-6
2	370	700	5	350-1050	150-550	2-7
3	220	430	5	200-600	100-300	2-7
4	700	1250	half space	700-2000	350-1000	-

Table 3. Mean model obtained from model A by different inversion algorithms.

Parameters	PSO Inv. (ReMi data)	PSO joint Inv.	NSGA-II
$V_{S1}$ (m/s)	192	197	227
$V_{S2}$ (m/s)	442	358	283
$V_{S3}$ (m/s)	208	251	212
$V_{S4}$ (m/s)	670	720	560
H1 (m)	4.4	4	4.05
H2 (m)	4.3	4.8	5.2
H3 (m)	5.5	5.3	5.4
$V_{P1}$ (m/s)	472	386	401
$V_{P2}$ (m/s)	668	664	705
$V_{P3}$ (m/s)	500	522	350
$V_{P4}$ (m/s)	1112	1119	965

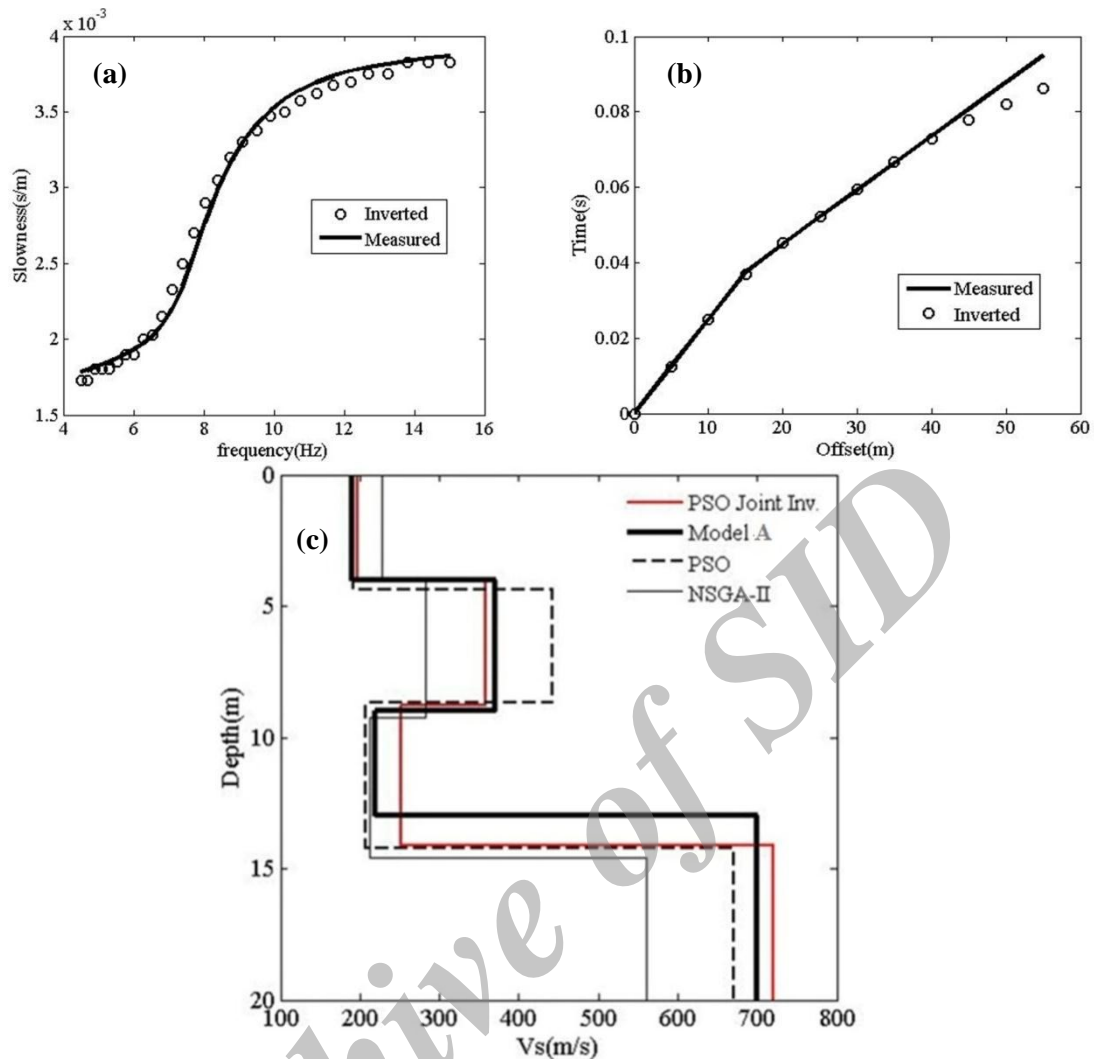


Figure 3. a) Inversion of dispersion curve using PSO joint inversion for model A b) Inversion of travel times using PSO joint inversion for model A Vs profile using PSO joint Inv., PSO, and NSGA-II.

Table 4. Parameters of synthetic model B and search space.

Layer number	V <sub>S</sub> (m/s)	V <sub>P</sub> (m/s)	H (m)	Search space		
				V <sub>P</sub> (m/s)	V <sub>S</sub> (m/s)	H (m)
1	285	700	3	350-1050	142-427	1-5
2	163	400	2	200-600	80-244	1-3
3	600	1470	10	700-2100	300-900	5-15
4	1328	2300	half space	1150-3400	664-1900	-

Table 5. Mean model obtained from model B.

Parameters	PSO Inv. (ReMi data)	PSO joint Inv.	NSGA-II
V <sub>S</sub> 1 (m/s)	290	298	270
V <sub>S</sub> 2 (m/s)	187	197	214
V <sub>S</sub> 3 (m/s)	642	628	661
V <sub>S</sub> 4 (m/s)	947	1326	1332
V <sub>P</sub> 1 (m/s)	539	610	661
V <sub>P</sub> 2 (m/s)	402	486	527
V <sub>P</sub> 3 (m/s)	1420	1134	1611
V <sub>P</sub> 4 (m/s)	2158	2195	1304
H1 (m)	2.6	2.8	3
H2 (m)	2.4	1.8	3
H3 (m)	9.1	9.6	9.6

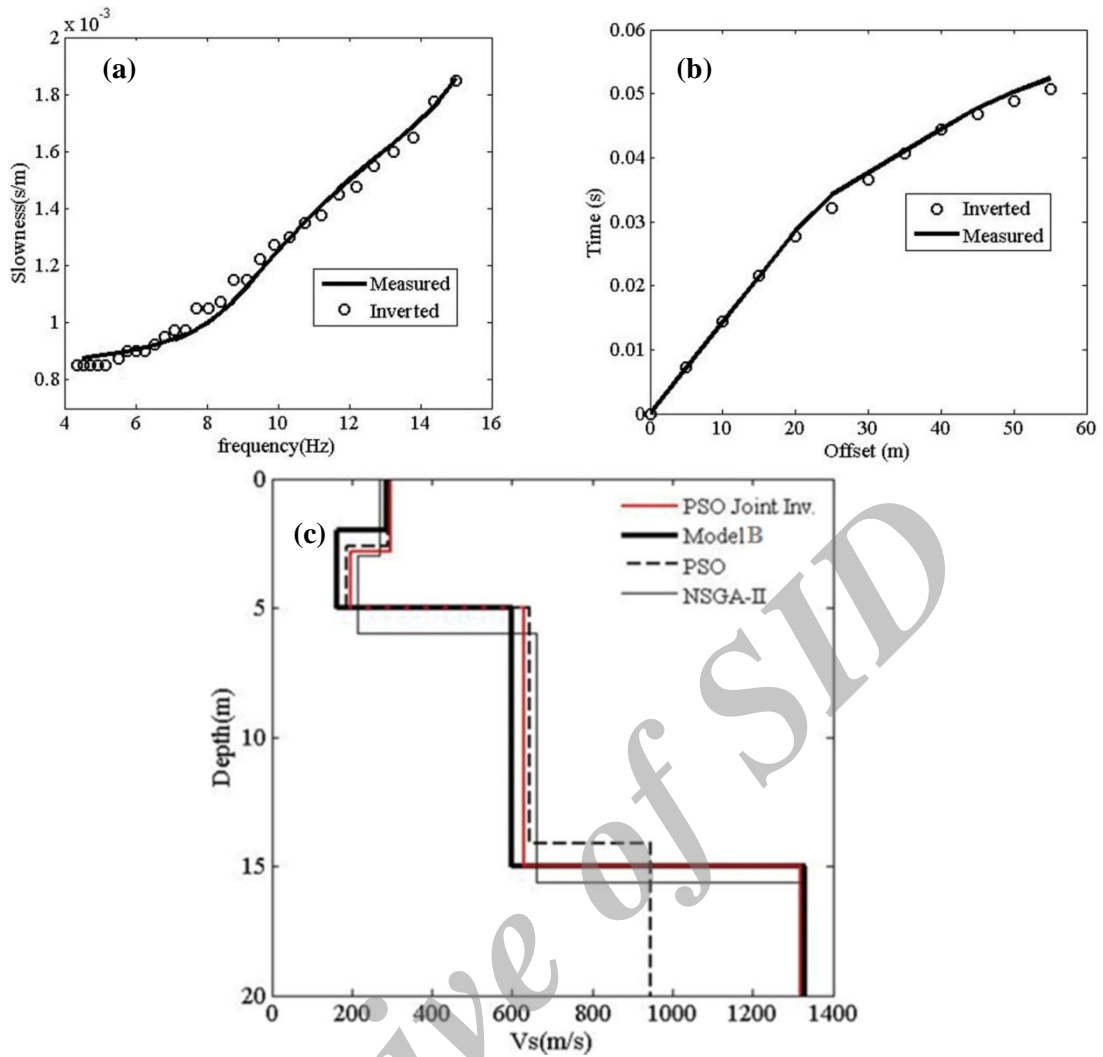


Figure 4. a) Inversion of dispersion curve using PSO joint inversion for model B, b) Inversion of travel times using PSO joint inversion for model B, and c)  $V_s$  profile of model B using PSO joint Inv., PSO, and NSGA-II.

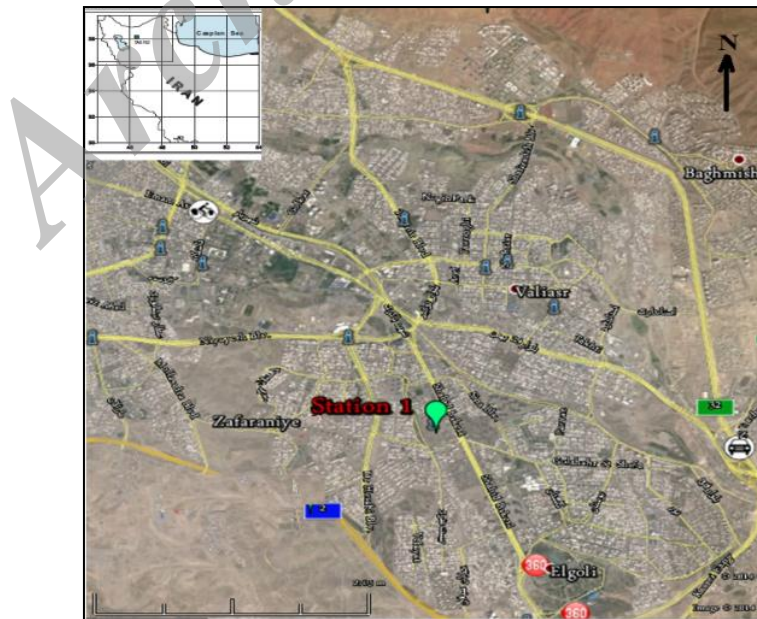
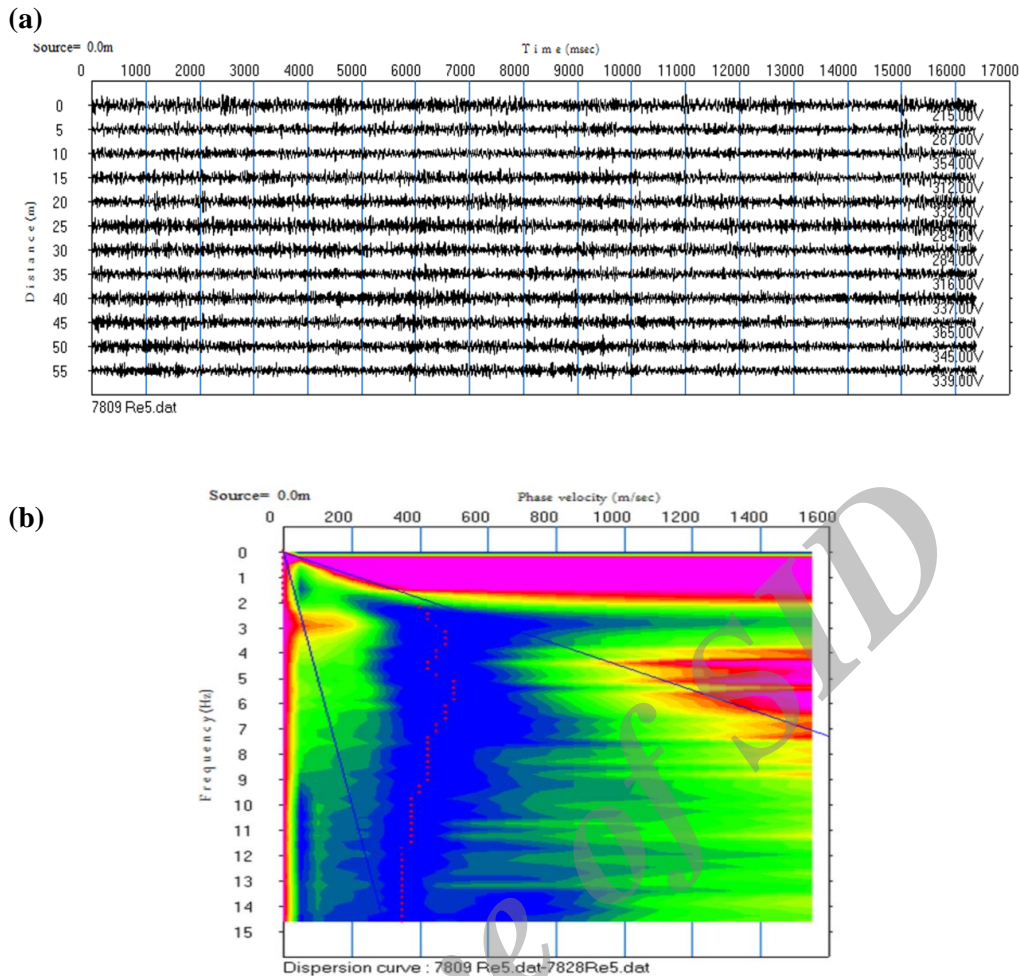


Figure 5. Location of studied area in Tabriz (NW of Iran).





**Figure 6. Field dataset a) A sample record of ReMi data b) Dispersion curve (red points, maximum amplitudes on phase velocity-frequency plot).**

Also the sledge-hammer (12 kg) source was used to generate the seismic signals for the seismic refraction data. In case of the seismic refraction, both the forward and reverse shootings were carried out along with the profile over a lateral distance of 115 m. The seismic results obtained indicated that the area was composed of two main layers that were nearly lateral (Figure 7). For the joint inversion procedure, a line with a 55 m length was selected (Figure 8). Similar to the inverse strategy of synthetic cases, we considered  $V_S$ ,  $V_P$ , and thickness (H) of the layers, as the variables (Table 6). After a number of runs and considering different models, by paying attention to the observed dispersion curve, a 3-layer model

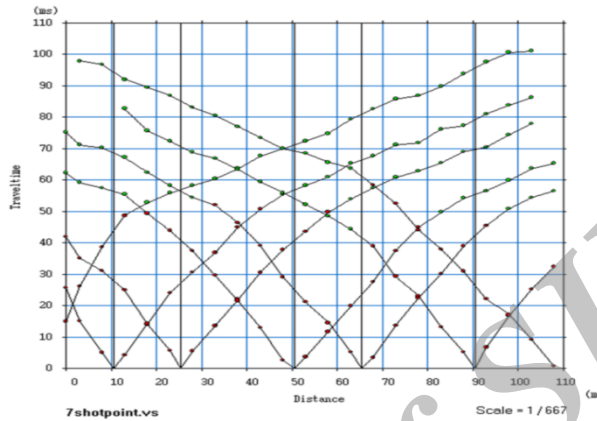
was adopted. The results obtained for the  $V_S$  profile were shown in Figure 9, in which there was a low velocity in depth (about 5 m). The results shown in Table 7 and Figures 9 and 10, have a good correlation with the geology. The upper layer made up of soil consisting of alluvium and sandy clay, and the second layer made up of clay soil and Tuff also there is water table in depth about 5m [38]. Moreover, the results obtained showed the  $V_P$  profile in detail, and detected a thin layer with a velocity of about 650 m/s (Figure 10). Moreover, the PSO joint inversion compared with the PSO inversion and NSGA-II approach.

**Table 6. Search space for PSO joint inversion of field dataset.**

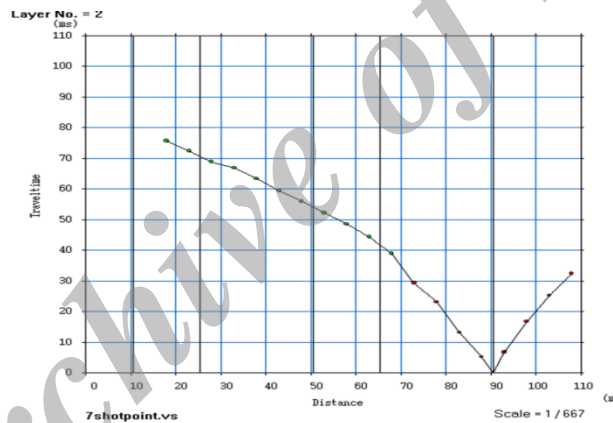
Layer number	Search space		
	thickness(m)	P-wave velocity (m/s)	S-wave velocity (m/s)
1	2-7	400- 700	150- 450
2	1-5	450- 900	200- 550
3	-	800-1600	350-750

**Table 7. Mean model obtained from field dataset.**

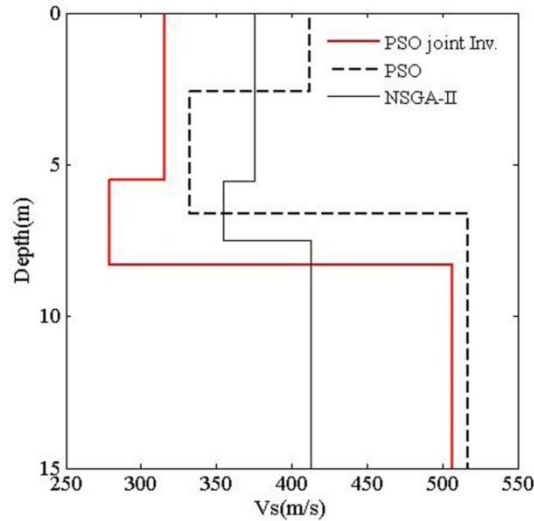
parameters	PSO Joint Inv.	NSGA-II	PSO
H1 (m)	5.5	5.53	2.6
H2 (m)	2.8	1.98	4
V <sub>p1</sub> (m/s)	507	523	680
V <sub>p2</sub> (m/s)	657	509	473
V <sub>p3</sub> (m/s)	1455	1114	1350
V <sub>s1</sub> (m/s)	316	385	412
V <sub>s2</sub> (m/s)	280	373	332
V <sub>s3</sub> (m/s)	512	405	517



**Figure 7. Time-distance plot of refraction field dataset.**



**Figure 8. Travel time selected for PSO joint inversion algorithm.**



**Figure 9. S-wave structure obtained from experimental dataset using PSO joint inversion of ReMi and seismic refraction data (PSO joint Inv.), PSO inversion of ReMi data (PSO), and NSGA-II algorithm in joint inversion of ReMi and seismic refraction data (NSGA-II).**

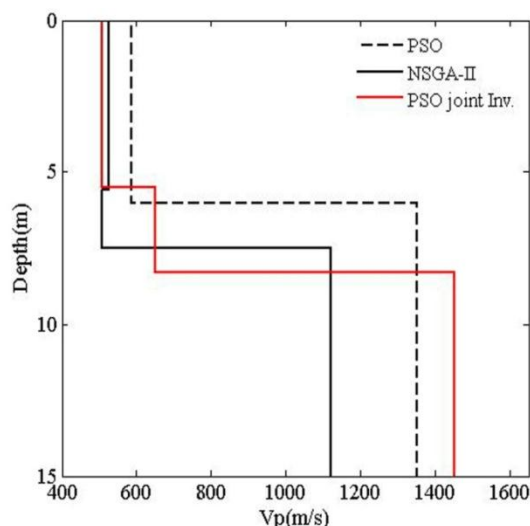


Figure 10.  $V_p$  structure obtained from experimental dataset using PSO joint inversion of ReMi and seismic refraction data (PSO joint Inv.), PSO single inversion of seismic refraction data (PSO) and NSGA-II algorithm in joint inversion of ReMi and seismic refraction data (NSGA-II).

### 3. Discussion

Surface wave studies and seismic refraction technique are two main seismic methods in engineering geology and geotechnical studies. The surface wave dispersion analysis is an appropriate tool for a near-surface seismic characterization. However, the main problem is related to the non-uniqueness of the nature of the dispersion curve inversion. To overcome this problem, we need a careful strategy for the inversion of the dispersion curve. On the other hand, the seismic refraction studies also suffer from the hidden layer and non-uniqueness of the solution.

PSO algorithm is one of the global optimization methods that belong to a group of metaheuristic searching algorithm. In the proposed method, the refraction microtremor and seismic refraction data was concurrently inverted. This method was investigated by means of two synthetic datasets, and also by a real dataset. The PSO joint inversion algorithm was compared with the PSO single inversion and NSGA-II algorithm. Our findings show that the PSO joint inversion used in estimating the  $V_s$  and thickness of the layers is more accurate than the PSO single inversion algorithm. Also the PSO joint inversion is more accurate, easier, and faster than NSGA-II. For more probe, the PSO joint inversion was investigated by the actual dataset performed in a part of Tabriz city in the NW of Iran. The results obtained show that the studied area is composed of two main layers. The first layer is made up of a soil consisting of alluvium and sandy clay soil, the intermediate layer is a mixture of clay and sand with moisture, and the last layer is made up of clay soil and Tuff.

### 4. Conclusions

Shear-wave velocity ( $V_s$ ) is the main parameter for site characterization in geotechnical engineering. However, dispersion curve inversion is challenging for most inversion methods due to its high non-linearity and mixed-determined trait. In order to overcome these problems, in this study, a joint inversion strategy was proposed based on the particle swarm optimization (PSO) algorithm.

Therefore, in processing the geophysical data that suffer from non-uniqueness, especially when dealing with field datasets (necessarily including a variable amount of noise) by joint inversion, the final results appeared to be quite robust. The proposed PSO joint inversion algorithm is a high-performance approach in the joint inversion of the seismic data.

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## وارون همزمان منحنی پاشش امواج میکروترمور و امواج انکساری با استفاده از بهینه‌سازی الگوریتم ازدحام ذرات

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### چکیده:

مطالعه و مدل‌سازی ویژگی‌های سرعتی مناطق نزدیک سطح زمین به دلیل ارتباط مستقیم آن با تأسیسات شهری واقع بر روی آن، از لحاظ ژئوتکنیکی و مهندسی زلزله از اهمیت خاصی برخوردار است. در سال‌های اخیر میکروترمور شکست مرزی (ReMi) برای تخمین منحنی‌های پاشش و در نهایت مدل‌سازی سرعت موج برشی، به دلیل هزینه پائین و سرعت بالای برداشت داده‌ها مورد استقبال قرار گرفته است؛ اما مشکل اساسی در پردازش این داده‌ها وارون‌سازی منحنی پاشش جهت تخمین سرعت امواج برشی است. در مقاله حاضر سعی شده است با پیشنهاد وارون‌سازی همزمان امواج ReMi (امواج ری‌لی) و امواج انکساری (زمان سیر امواج) با روش بهینه‌سازی الگوریتم ازدحام ذرات، تخمینی از ساختار سرعت موج برشی ارائه شود. برنامه الگوریتم مذکور در محیط متلب نوشته شده است. روش پیشنهاد شده در ابتدا به‌وسیله مدل‌های مصنوعی مورد ارزیابی قرار گرفت و در ادامه برای ارزیابی بیشتر روی داده‌های تجربی اعمال شد. بدین منظور یک ایستگاه در تبریز برداشت شد. نتایج وارون‌سازی به‌دست آمده در مورد مدل‌های مصنوعی و هم داده‌های تجربی، بیانگر عملکرد قابل‌قبول الگوریتم پیشنهاد شده، به‌عنوان یک روش مؤثر در وارون‌سازی همزمان داده‌های ژئوفیزیکی، در مقایسه با سایر روش‌های مرسوم است. این الگوریتم یک راهکار مناسب در کاهش عدم یکتایی نتایج وارون‌سازی است.

**کلمات کلیدی:** سرعت موج برشی، وارون‌سازی همزمان، میکروترمور انکساری، الگوریتم ازدحام ذرات، زمان رسید.