

## **Physical adsorption between mono and diatomic gases inside of Carbon nanotube with respect to potential energy**

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### **ABSTRACT**

In this paper we have done three theoretical studies by using Monte Carlo simulation and Mm+, AMBER and OPLS force field. The calculations were carried out using Hyper Chem professional, release 7.01 package of program. First we have studied the interaction of H<sub>2</sub> molecule and He atom with single-walled carbon nanotube at different temperatures. For doing this study we placed H<sub>2</sub> and He in the center and outside the nanotube, permitting them to close the nearest carbon atom from nanotube. Then we plotted the potential energy versus distance of interaction, and at minimum point of energy we calculated potential energy for physical adsorption process. Second we placed two H<sub>2</sub> molecules and two He atoms at two ends of nanotube separately, permitting them to close each other step by step then we calculated E<sub>kin</sub>, E<sub>pot</sub> and E<sub>tot</sub> for H<sub>2</sub>---H<sub>2</sub> and He---He interaction at different temperatures. In another activity we added 2 to 100 H<sub>2</sub> molecules and 2 to 100 He atoms across the nanotube and after each time increased the number of H<sub>2</sub> and He we have estimated the potential energy, then we plotted the potential energy versus the number of H<sub>2</sub> molecules and He atoms so that the shape of potential curve will be determined.

**Keywords:** Single walled-carbon nanotube; Physical adsorption; Monte Carlo simulation; Hydrogen; Helium

### **INTRODUCTION**

A theoretical and experimental understanding of carbon nanotubes have developed very rapidly over the last few years. The mechanical and electronic properties of carbon nanotube are interesting and give promise for useful nanotube applications in nano-engineering [1-4] and as catalyst supports [5]. The unique shape of carbon nanotube useful for physical adsorption, and this paper deals with this phenomenon.

Carbon nanotubes produced by the catalytic method are believed to have close

ends, composed of pentagonal and hexagonal carbon rings. The opening of the ends is achieved by cutting the tubes using an acidic and oxidizing solution with sonication [6]. Studying the interaction between CNTs and mono and diatomic gases (He, H<sub>2</sub>) could from fundamental point of view, significantly deepen our understanding on nanoscale devices physics. Single-walled carbon nanotube (SWNTs) are of interest as gas adsorbents because of their unique structural properties.

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There have been several works devoted to the investigation of the adsorption behavior of  $H_2$  on single-walled carbon nanotube and multi-walled carbon nanotube [7-9].

In most of these researches the methods of calculations are DFT and HF. As we observe on fig. 1, the total number of carbon atoms in SWNT that we chose for study is many much, the calculations very time consuming and we need supercomputers, for resolve this problem we considered the Monte-Carlo simulation as the base of study.

The purpose of this research is studying the physical adsorption of  $H_2$  molecule and He atom on single-walled carbon nanotube by means of Monte Carlo simulation. In this work we have modeled three different scenarios in our simulations.

In the first case, we modeled one  $H_2$  molecule and one He atom that are located in the center and outside of the nanotube, then permitted them to close the nearest carbon atom from nanotube. In the second case we located two  $H_2$  molecules (or two He atoms) at the ends of the nanotube and allowed them to close each other, then the  $H_2$ --- $H_2$  and He---He interaction at the different temperatures were determined separately. In the third case, we entered  $H_2$  molecules (or He atoms) to the nanotube, then the interaction energy of  $H_2$  molecules (or He atoms) with nanotube by Monte Carlo method were determined. These calculations also were carrying out with additional 2 to 100  $H_2$  molecules (2 to 100 He atoms) to nanotube.

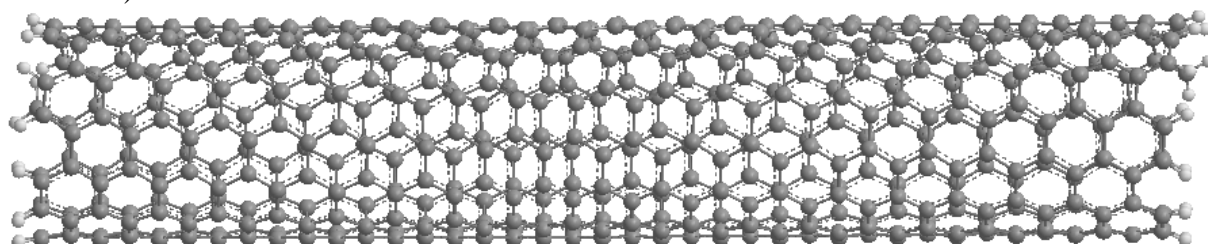


Fig. 1. The structure of carbon nanotube that we chose for study in this paper.

## THEORETICAL BACKGROUND

Adsorption is a process that occurs when a gas or liquid solute accumulates on the surface of a solid or a liquid (adsorbent), forming a molecular or atomic film (the adsorbate). It is different from absorption, in which a substance diffuses into a liquid or solid to form a solution. The term sorption encompasses both processes, while desorption is the reverse process.

Adsorption is operative in most natural physical, biological, and chemical systems, and is widely used in industrial applications such as activated charcoal, synthetic resins and water purifications. Similar to surface tension, adsorption is a consequence of surface energy, in a bulk material, all the bonding requirements (be they ionic, covalent or metallic) of the constituent atoms of the material are filled but atoms on the (clean) surface experience a bond deficiency, because they are not wholly surrounded by other atoms, that it is energetically favorable for them to bond with whatever happens to be available, the exact nature of the bonding depends on the details of the species involved, but the adsorbed material is generally classified as exhibiting physisorption or chemisorptions.

**Physisorption:** or physical adsorption is a type of adsorption in which the adsorbate adheres to the surface only through van der Waals (weak intermolecular) interactions, which are also responsible for the non-ideal behavior of real gases.

**Chemisorption:** is a type of adsorption whereby a molecule adheres to a surface through the formation of a chemical bond, as opposed to the van der Waals forces which cause physisorption.

Adsorption is usually described through isotherms, that is functions which connect the amount of adsorbate on the adsorbent, with its pressure (if gas) or concentration (if liquid). One can find in literature several models describing process of adsorption, namely Freundlich isotherm, Langmuir isotherm, etc.

### Theoretical details

1) as we know, in order to carrying out any quantum mechanical calculation in Hyper Chem 7.0 program package there are three steps [10]. first, prepare a molecule with an appropriate starting geometry. Second, choose a calculation method and its associated (set up menu) options. Third, choose the type of calculation (single point, geometry optimization, molecular dynamics, Langevin dynamics, Monte Carlo and vibrational analysis) with the relevant (compute menu) options.

These geometry optimization calculations can use either molecular mechanics or quantum mechanics to further refine the molecular geometry beyond that given by the Model Builder. Hyper Chem uses the Metropolis method [11], which chooses random configurations with this probability, to concentrate sampling of configurations in regions of space that make important contributions to the calculation of thermodynamic averages.

### Molecular Mechanics (Monte Carlo simulation)

2) Monte Carlo is a term used in many fields of science, engineering, statistics and mathematics to mean entirely different things, the one (and only) thing that all Monte Carlo methods is that they all use

random numbers to help calculate something.

Monte Carlo simulations are widely used in the field of chemistry, biology, physics and engineering in order to determine the structural and thermodynamic properties of complex systems at the atomic level. Thermodynamic averages of molecular properties can be determined from Monte Carlo methods, as can minimum-energy structures [12-13].

Also, it should be noted that constraining potentials (which keep the cluster components from straying too far from a cluster's center of mass) are sometimes used [14]. At finite temperature, clusters have finite vapor pressures and particular cluster sizes are typically unstable to evaporation. Introducing a constraining potential enables one to define clusters of desired sizes.

The Monte Carlo method is one of the most broadly and commonly used numerical techniques, with application in statistical physics, quantum mechanics, field theory and others [15]. Monte Carlo simulation, which can generate a canonical ensemble, is applied when systems have difficult integrals to be solved and should generate some random number to generate uniform independent values statistically [16-17]. In the Monte Carlo method a Metropolis algorithm is applied more than other algorithms because of its simplicity [18]. The accuracy of the algorithm is determined by random displacement in trivial displacements, all moves can be accepted, but in large cases the rate of acceptable moves is small.

In this investigation, the calculations of the interaction between mono and diatomic gases with single-walled carbon nanotube by MM+, AMBER and OPLS force fields have been performed. In this investigation Hyper Chem professional release 7.01 is used for the quantum chemical calculations, we have performed geometry

optimization and Monte Carlo simulation by this software.

## RESULT AND DISCUSSION

In the studies of H<sub>2</sub> on larger diameter carbon nanotube two adsorption states were reported. One is the physisorption and the other one is a chemisorption state [19-21]. In the chemisorption state the H<sub>2</sub> molecule dissociates and adheres on two adjacent C atoms on the outer wall of tube.

Before any calculation we must answer two questions (i) does H<sub>2</sub> like to be physically adsorbed on or to be chemically dissociated adsorbed on SWNTs? (ii) and if H<sub>2</sub> is dissociated adsorbed on tube, does it destroy the tube's structure?

In the recent years, several first principles calculations have shown that H<sub>2</sub> molecule is difficult to dissociate on graphene or nanotube. Arellano *et al.* simulated the reaction of H<sub>2</sub> on (5, 5) and (6, 6) tubes in details and found that the estimated energy barrier for H<sub>2</sub> dissociated on these tubes are greater than 2.5 eV [18-20]. Hence in this article we choose the H<sub>2</sub> physisorption for study. Theoretical calculations of H<sub>2</sub> adsorption on SWCNTs have been performed using various methods.

Ab initio simulations that indicate the potential for higher uptake are subject to tight-binding or density functional approximations is not expected to be accurate for physisorption [22-23].

In this research we placed H<sub>2</sub> molecule (and He atom) out of and inside of the SWCNT, then we chose nearest carbon atom from the wall of nanotube and while H<sub>2</sub>, step by step approaching to the nanotube, potential energy has been calculated. After this we have plotted potential energy as a function of distance, and at the minimum point of energy (D<sub>min</sub>) physisorption has been calculated by the following relation:

$$E_{ads} = E_{SWNT-H_2} - (E_{SWNT} + E_{H_2})$$

Where  $E_{SWNT-H_2}$  is the potential energy of the optimized SWNT-H<sub>2</sub>,  $E_{SWNT}$  is the potential energy of the optimized SWNT and  $E_{H_2}$  is the potential energy of the isolated H<sub>2</sub> molecule.

In table 1 and 2 we show the calculated potential energy of physisorption at different temperatures when H<sub>2</sub> and He placed inside and outside of the nanotube.

It is found from table 1 and 2, when temperature increases the potential energy of physical adsorption process, also increases and with change in the temperature and force field the position of minimum points also changes. Like wise in this article, in addition to the physical adsorption we have studied the H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Mm+, AMBER and OPLS force field in different temperature (290, 294, 298, 302, 306, 310). In order to do this, first we placed two H<sub>2</sub> molecules (and two He atoms) at the two ends of the nanotube, second we put them closer together step by step by GaussView software, then we calculated kinetic energy (E<sub>kin</sub>), potential energy (E<sub>pot</sub>) and total energy (E<sub>tot</sub>) by Monte Carlo simulation (see table 3,4,5). In (Fig. 2) E<sub>kin</sub> changes calculated versus different temperature by Monte Carlo simulation and Mm+, AMBER and OPLS force field.

As shown in (Fig. 2, 3) with increasing temperature, kinetic energy also increases, the largest amount of kinetic energy is observed at 310K and kinetic energy and potential energy for He---He interaction is greater than H<sub>2</sub>---H<sub>2</sub> interaction but in calculations with Mm+ force field, potential energy and kinetic energy for H<sub>2</sub>---H<sub>2</sub> interaction is greater than He---He interaction.

**Table 1.** E<sub>ads</sub> (in kcal/mol) in the adsorption process of H<sub>2</sub> and He on external wall of nanotube calculated by Monte Carlo and Mm+, Amber and Opls force field

Temperature(K)			250	270	290	310	330	350
H <sub>2</sub>	Mm+	D <sub>min</sub> (Å)	5	4.5	2.5	2	3	3
		E <sub>ads</sub>	342.18	381.31	451.14	422.37	466.12	504.26
	Amber	D <sub>min</sub>	4.5	3	4.5	3	3	3
		E <sub>ads</sub>	349.16	381.13	488.78	431.17	455.11	476.5
	OPLS	D <sub>min</sub> (Å)	2.5	2	4	2	5	4
		E <sub>ads</sub>	357.66	378.13	400.02	428.67	474.91	482.02
He	Mm+	D <sub>min</sub> (Å)	3.5	2.5	5	4	4.5	3
		E <sub>ads</sub>	382.06	399.05	423.18	448.91	488.82	523.36
	Amber	D <sub>min</sub> (Å)	3.5	1.5	1	1	2	3
		E <sub>ads</sub>	410.46	437.47	448.8	482.22	506.21	535.82
	OPLS	D <sub>min</sub> (Å)	3	1	2.5	3.5	3.5	3.5
		E <sub>ads</sub>	365.17	411.22	437.19	466.64	487.1	537.99

**Table 2.** E<sub>ads</sub> (in kcal/mol) in the physical adsorption process of H<sub>2</sub> and He on internal wall of nanotube calculated by Monte Carlo and Mm+, Amber and OPLS force field

Temperature(K)			250	270	290	310	330	350
H <sub>2</sub>	Mm+	D <sub>min</sub> (Å)	4.5	4	3	4.5	2	4
		E <sub>ads</sub>	357.79	371.41	393.72	434.9	472.16	489.27
	Amber	D <sub>min</sub> (Å)	3.5	3	4.5	3	2	1.5
		E <sub>ads</sub>	346.03	387.3	393.89	420.23	434.52	464.04
	OPLS	D <sub>min</sub>	2.5	3.5	4	1.5	4	3
		E <sub>ads</sub>	345.49	365.06	392.32	430.85	429.25	467.85
He	Mm+	D <sub>min</sub> (Å)	1.5	2	2.5	3	2	2.5
		E <sub>ads</sub>	356.81	368.88	404.01	455.4	459.29	477.74
	Amber	D <sub>min</sub> (Å)	4.5	4	2	2	3.5	2
		E <sub>ads</sub>	395.94	421.65	455.31	478.63	499.56	529.53
	OPLS	D <sub>min</sub> (Å)	1.5	4.5	3.5	1.5	1.5	3.5
		E <sub>ads</sub>	367.77	396.86	446.54	458.53	500.14	503.46

**Table 3.** The kinetic energy (E<sub>kin</sub>), potential energy (E<sub>pot</sub>) and total energy (E<sub>tot</sub>) calculated for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and Mm+ force field in different temperature

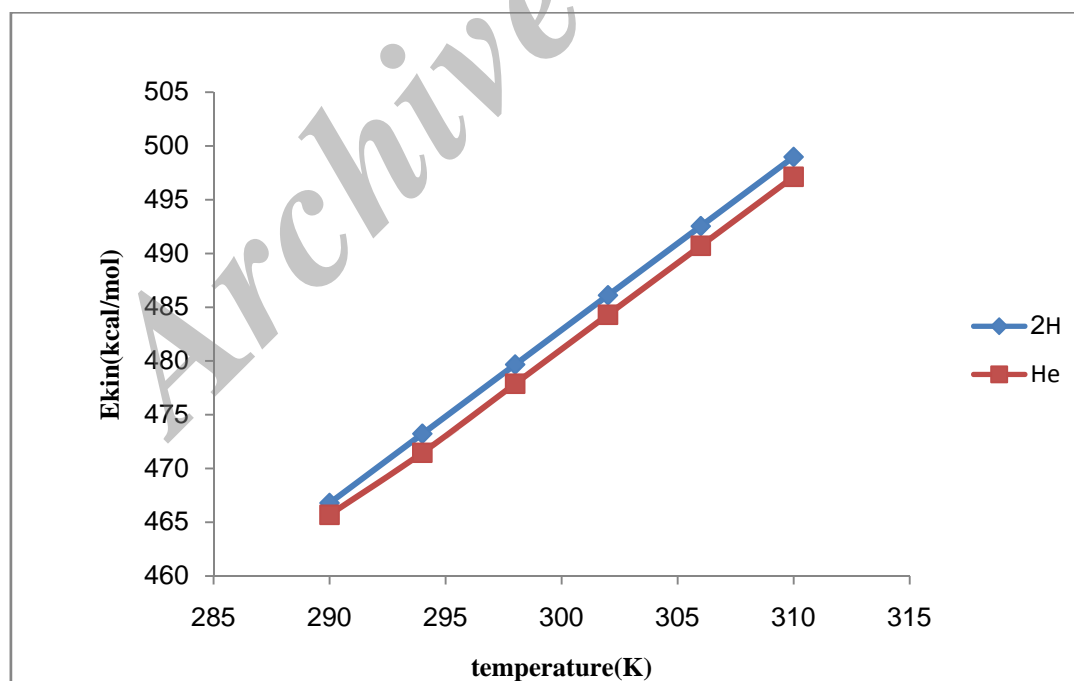
gases	Monte Carlo/Mm+						
	Temperature(K)						
	E(kcal/mol)	290	294	298	302	306	310
H <sub>2</sub>	E <sub>kin</sub>	466.79	473.23	479.67	486.11	492.54	498.98
	E <sub>pot</sub>	2359.77	2365.74	2381.64	2383.44	2387.64	2394.48
	E <sub>tot</sub>	2826.36	2838.98	28861.31	2869.55	2880.12	2893.47
He	E <sub>kin</sub>	465.7	471.47	477.89	484.31	490.72	497.14
	E <sub>pot</sub>	2368.84	2372.15	2371.5	2382.3	2395.15	2388.94
	E <sub>tot</sub>	2833.9	2843.63	2849.4	2866.61	2885.87	2886.08

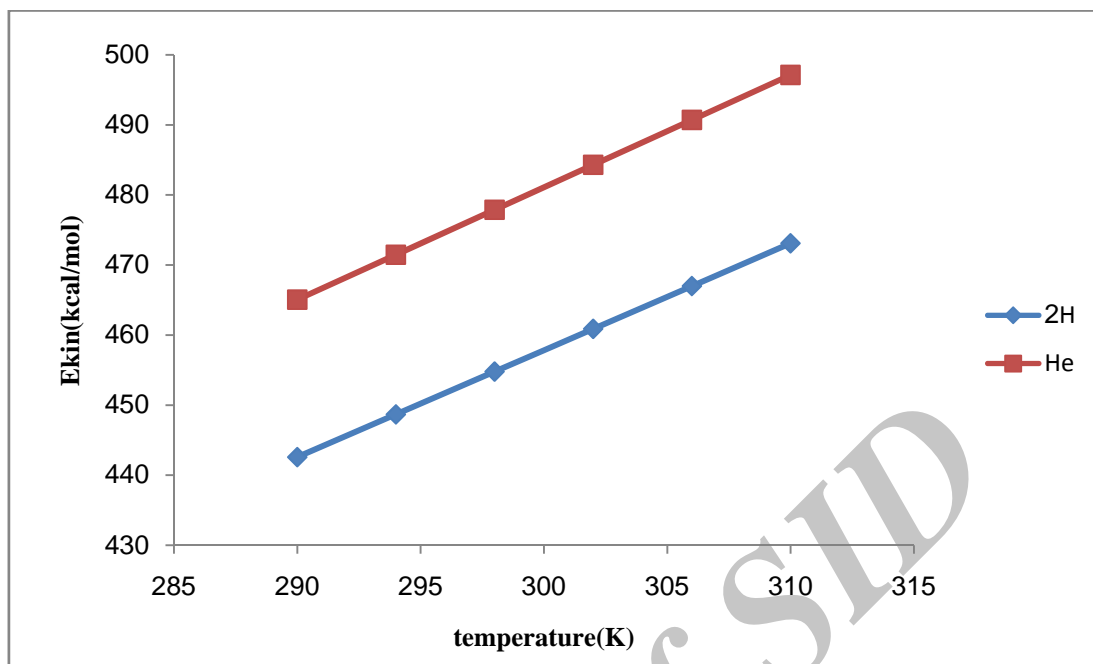
**Table 4.** The kinetic energy ( $E_{kin}$ ), potential energy ( $E_{pot}$ ) and total energy ( $E_{tot}$ ) calculated for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and Amber force field in different temperature

gases	Monte Carlo/Amber						
	Temperature(K)						
	E(kcal/mol)	290	294	298	302	306	310
H <sub>2</sub>	E <sub>kin</sub>	442.59	448.69	454.8	460.9	467.01	473.11
	E <sub>pot</sub>	1099.7	1104.52	1095.83	1103.08	1136.2	119.611
	E <sub>tot</sub>	1542.29	1553.21	1550.63	1563.98	1603.2	1592.72
He	E <sub>kin</sub>	465.06	471.47	477.89	484.31	490.72	497.14
	E <sub>pot</sub>	1144.73	1157.16	1158.57	1168.86	1162.35	1178.25
	E <sub>tot</sub>	1609.78	1628.64	1636.46	1653.17	1653.07	1675.4

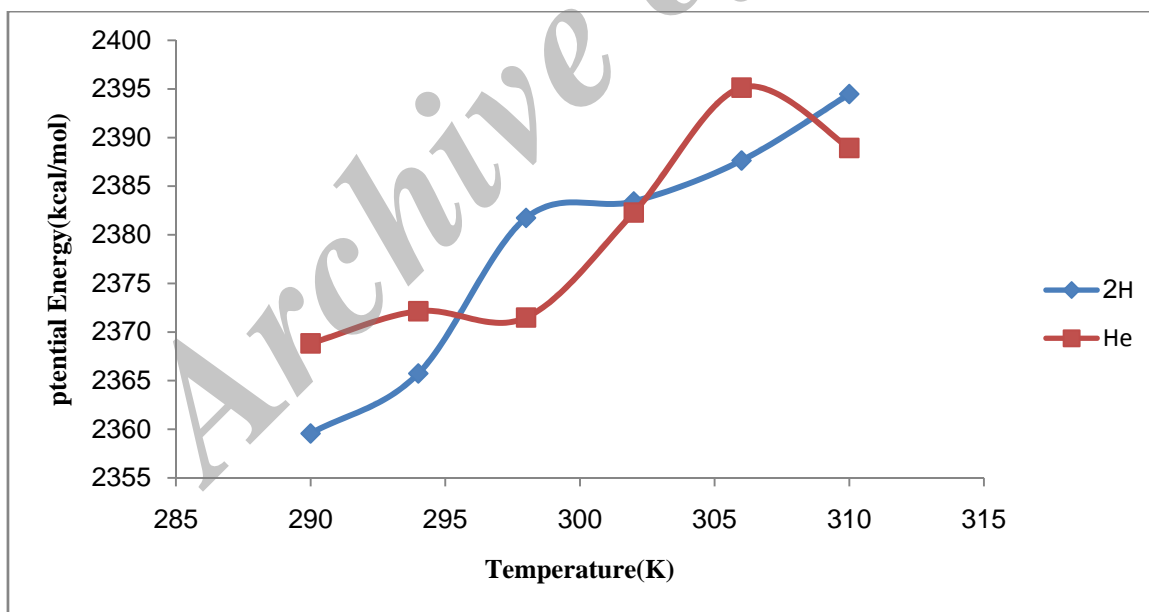
**Table 5.** The kinetic energy ( $E_{kin}$ ), potential energy ( $E_{pot}$ ) and total energy ( $E_{tot}$ ) calculated for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and opls force field in different temperature

gases	Monte Carlo/opls						
	Temperature(K)						
	E(kcal/mol)	290	294	298	302	306	310
H <sub>2</sub>	E <sub>kin</sub>	442.59	448.69	454.8	460.9	467.01	473.11
	E <sub>pot</sub>	1586.11	1593.24	1612.94	1608.23	1613.64	1630.39
	E <sub>tot</sub>	2028.7	2041.93	2067.74	2069.13	2080.65	2103.5
He	E <sub>kin</sub>	465.06	471.47	477.89	484.31	490.72	497.14
	E <sub>pot</sub>	1613.87	1616.6	1623.8	1630.54	1633.18	1624.12
	E <sub>tot</sub>	2078.93	2111.52	2101.69	2114.85	2123.9	2169.16

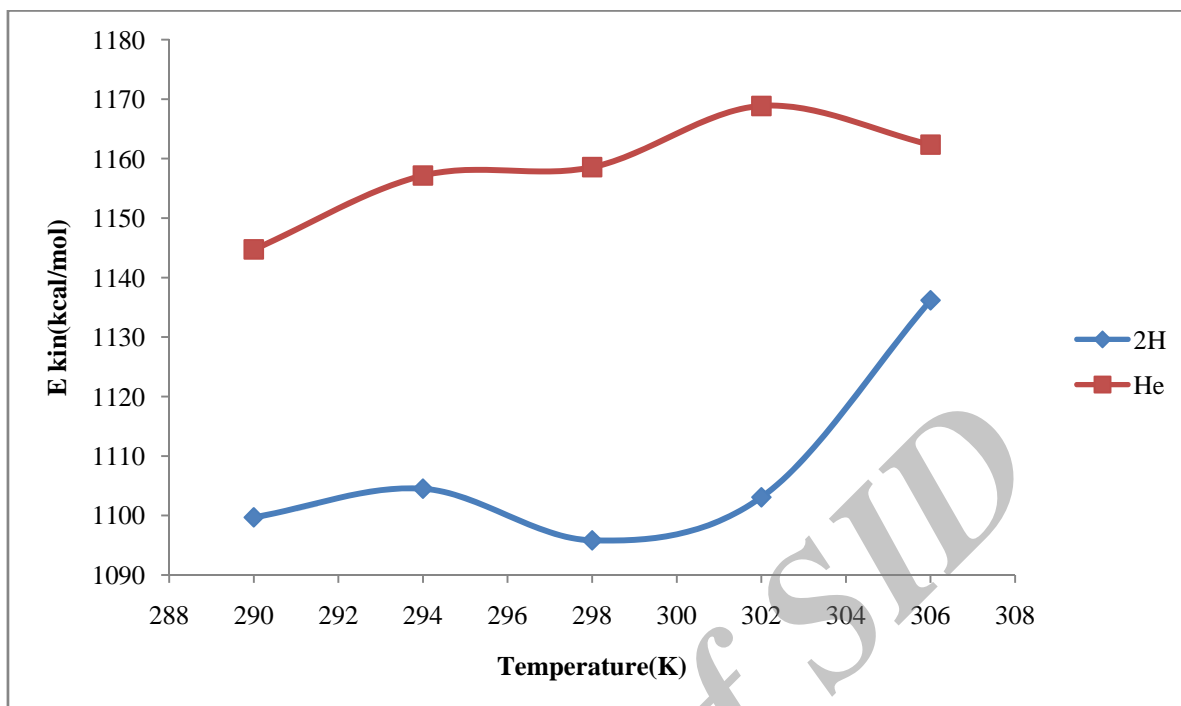
**Fig. 2.**  $E_{kin}$  changes (kcal/mol) calculated versus temperature for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and Mm+ force field.



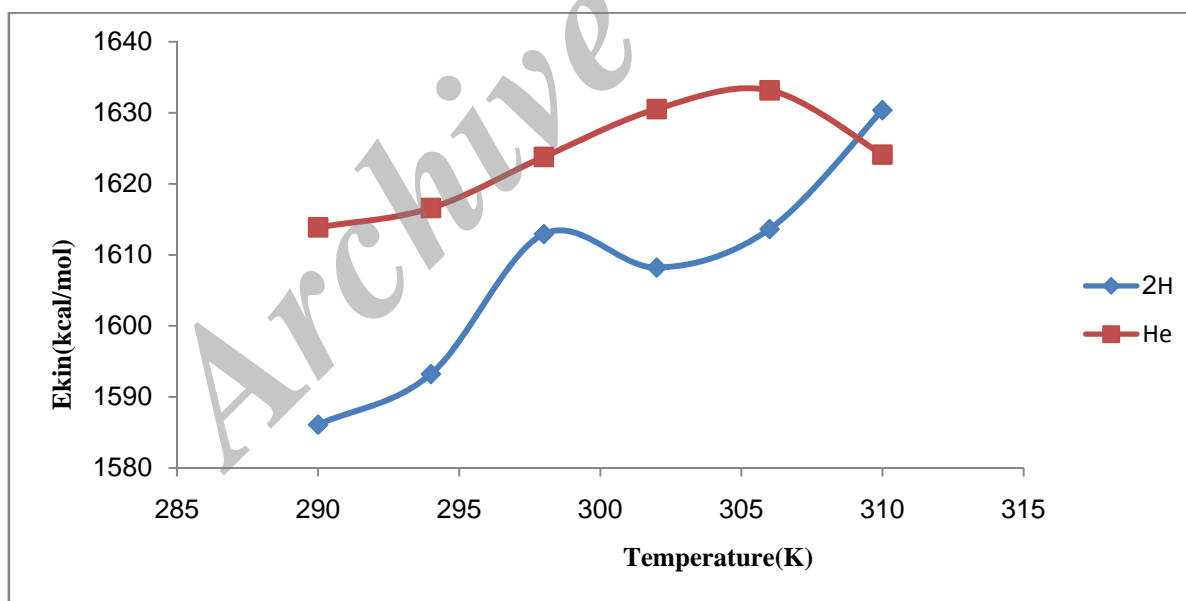
**Fig. 3.**  $E_{kin}$  changes (kcal/mol) calculated versus temperature for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation with Amber and opl's force field.



**Fig. 4.**  $E_{pot}$  changes (kcal/mol) calculated versus temperature for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and Mm+ force field.



**Fig. 5.**  $E$  pot changes (kcal/mol) calculated versus temperature for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and Amber force field.



**Fig. 6.**  $E$  pot changes (kcal/mol) calculated versus temperature for H<sub>2</sub>---H<sub>2</sub> and He---He interaction inside of SWNT by Monte Carlo simulation and opls force field.

In another activity, we placed from 2 up 100 H<sub>2</sub> molecules (2 up 100 He atoms) across the SWCNT, and after each time we increased the H<sub>2</sub> and He, we have estimated

the potential energy by the following relation:

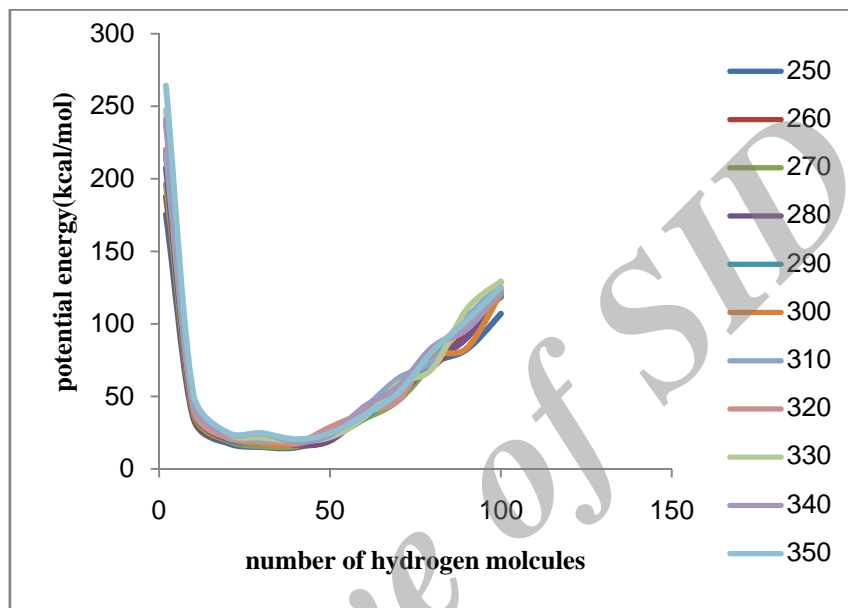
$$Ep = \frac{(E_{SWCNT-nH_2}) - E_{SWCNT}}{n}$$



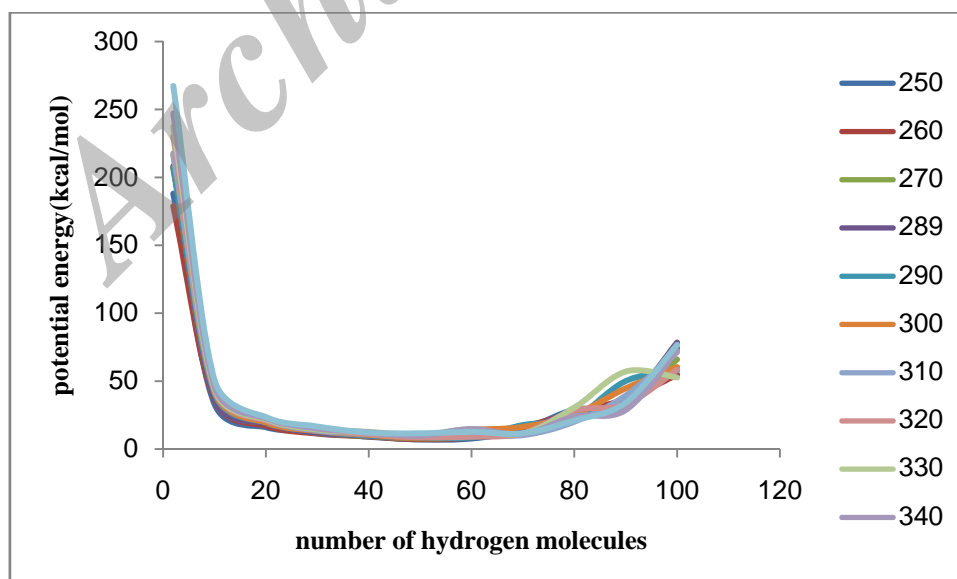
Where  $E_{SWNT-nH_2}$  is the potential energy of the single-walled nano tube with  $H_2$  molecules or with He atoms,  $E_{SWCNT}$  is the potential energy of the optimized single-walled nanotube and  $n$  is the number of  $H_2$  molecules or He atoms added to the nanotube. after that, we plotted the

potential energy versus the number of  $H_2$  or He, so that the kind of potential curve will be determined, (see fig. 7-10).

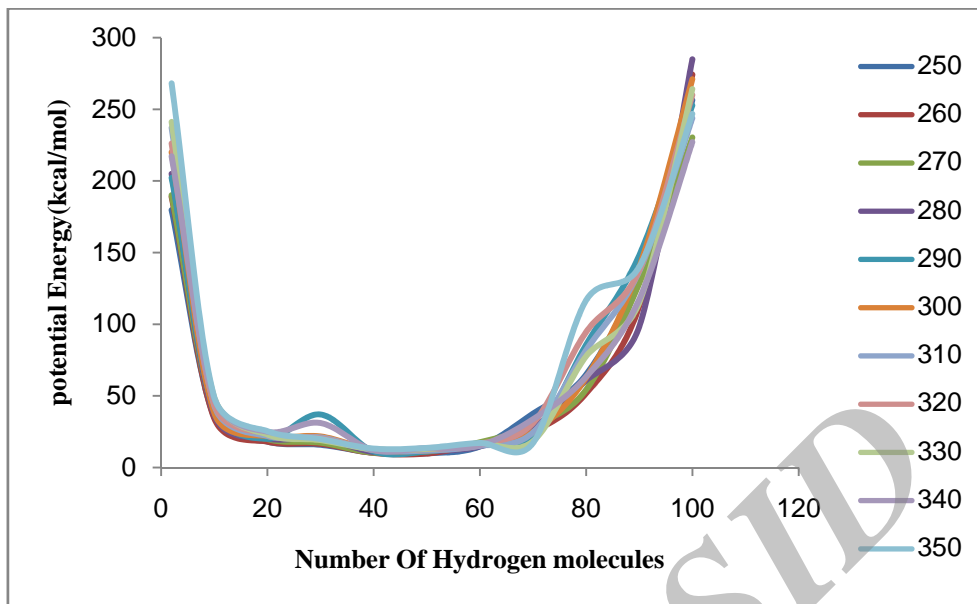
Paying careful attention to the diagrams reveals that changes of temperature do not cause any considerable changes in potential energy.



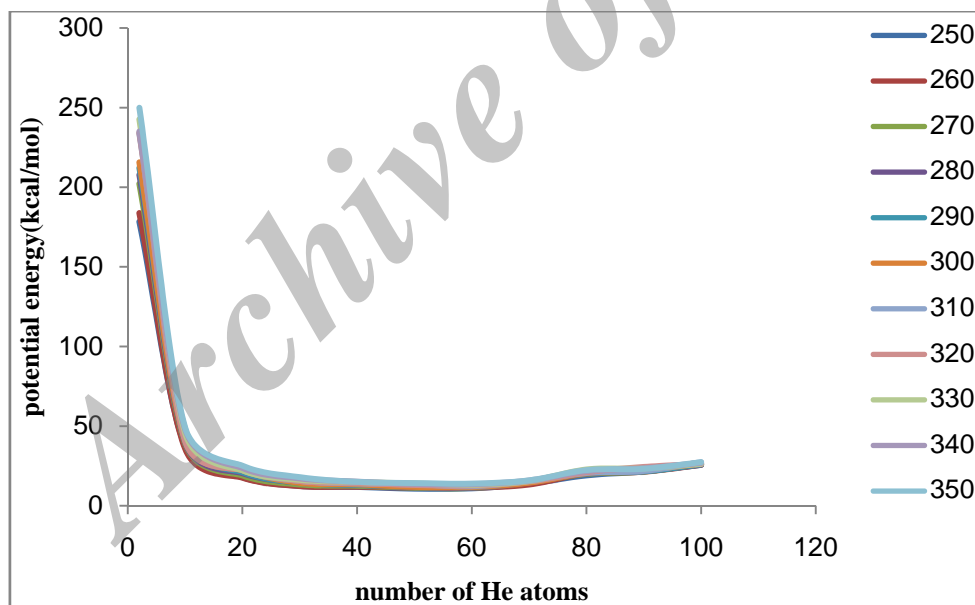
**Fig. 7.** potential energy curve versus number of  $H_2$  molecules added to SWCNT by Monte Carlo simulation and Mm+ force field.



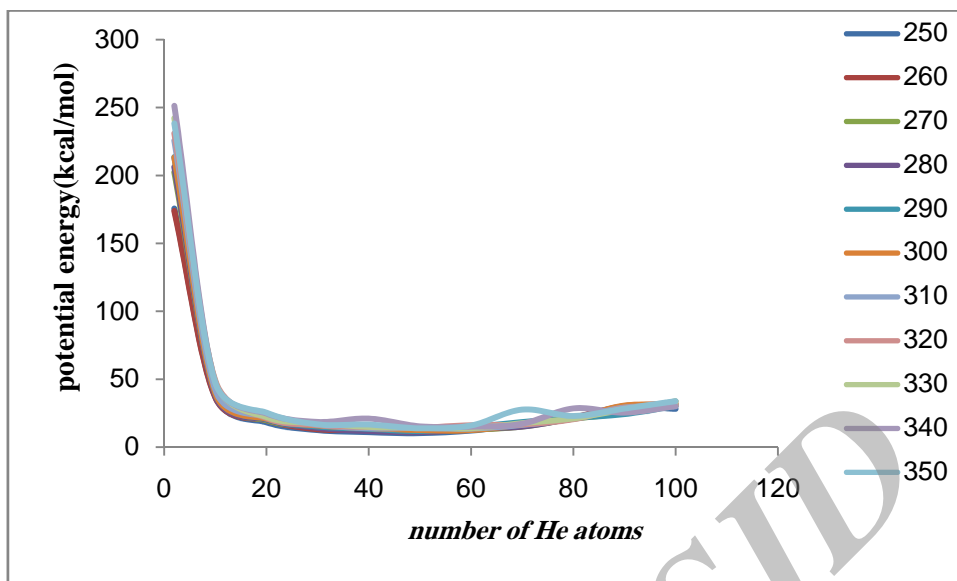
**Fig. 8.** potential energy curve versus number of  $H_2$  molecules added to SWCNT by Monte Carlo simulation and Amber force field.



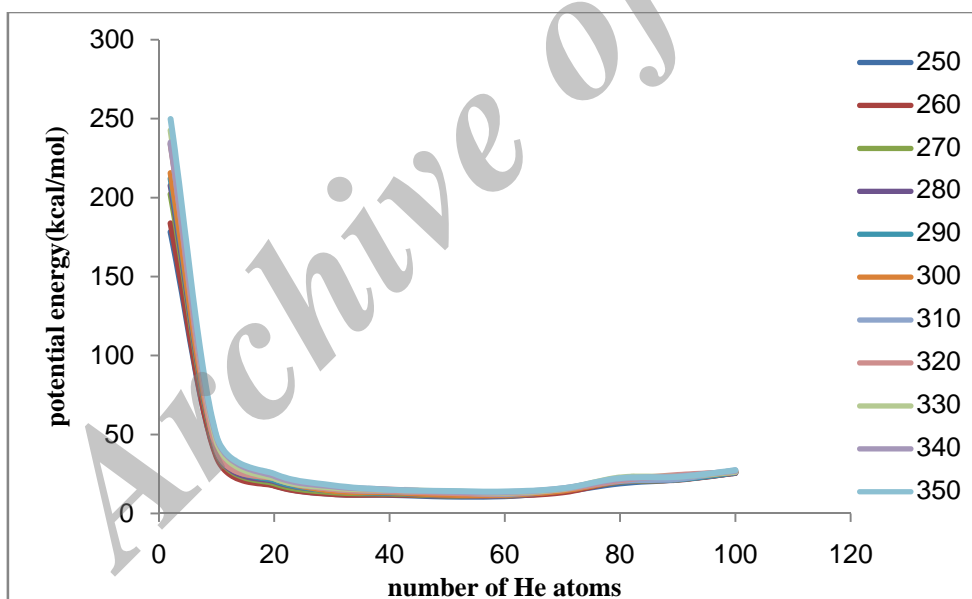
**Fig. 9.** Potential energy curve versus number of H<sub>2</sub> molecules added to SWCNT by Monte Carlo simulation and OPLS force field.



**Fig. 10.** Potential energy curve versus number of He added to SWCNT by Monte Carlo simulation and Mm+ force field.



**Fig. 11.** Potential energy curve versus number of He added to SWCNT by Monte Carlo simulation and Amber force field.



**Fig. 12.** Potential energy curve versus number of He added to SWCNT by Monte Carlo simulation and opls force field.

## CONCLUSION

In this paper physical adsorption properties for H<sub>2</sub> and He on single walled carbon nanotube have been investigated using Monte Carlo simulation and different force field (AMBER, OPLS, Mm+). the calculated parameters are the potential

energy of H<sub>2</sub> and He with inside and outside wall of single walled carbon nanotube. It is found that the interaction of H<sub>2</sub> and He with SWNT is depend to changes of temperature, but changes of force field does not cause any considerable

change in potential energy. In addition of H<sub>2</sub> to SWNT the diagrams indicate that when the number of He atoms increase the interaction between tube and He atoms decreases, but in the case of H<sub>2</sub> the interaction energy first decreases and then increases.

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