

# An Investigation on Rheology of Peroxide Cross-linking of Low Density Polyethylene

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## ABSTRACT

One of the most important post-reactor modifications of polyethylene is cross-linking. It improves some properties of polyethylene such as environmental stress cracking resistance, chemical and abrasion resistance, and service temperature. In this study, the effect of peroxide cross-linking on the rheological behaviour of low density polyethylene was investigated by using a combination of creep test and differential scanning calorimeter (DSC) in isotherm condition. The used peroxide was di-cumyl peroxide and its concentration was 2 wt%. The experiments were carried out at 150, 160, and 170°C and the change of bulk viscosity due to network developing was determined. For delivering of local derivatives smoothing techniques were applied on creep data. The rate of increment of viscosity increased with increasing the temperature, and the major of this increment took place in the first stages of reaction.

### Key Words:

rheology;  
crosslinking;  
low density polyethylene;  
di-cumyl peroxide;  
DSC;  
creep test.

## INTRODUCTION

The rheologically tracking of developing network system (DNS) is very important in the design and optimization of flow process. The DNS includes a wide range of materials such as radiation curable monomers, more viscous two components, and

high viscous thermally curable fluids. Many researchers have investigated on rheological behaviour of cross-linking reaction of thermoset resins such as: epoxy, polyester, polyurethane, and phenolics. In these systems, according to the chemistry

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of reaction, by increasing the degree of reaction, viscosity increases dramatically up to the gel point. At this point the viscosity tends to infinity and liquid-solid transition occurs. [1-6].

In general, the production of cross-linked polyethylene (by organic peroxides) in form of cables, pipes, heat shrinkable articles, etc. is carried out in continuous operation and cross-linking reaction is completed during the different steps of the processing. Cross-linking reaction takes place in melt condition and network develops along the production line [7-11]. The rheological properties change with developing of network and it is often vital to know the trend of these variations and the time for reaching the gel point. [12-13].

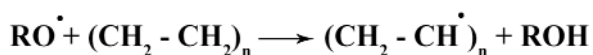
The DNS Viscosity depends on chemical structure, processing condition, and the characteristics of the growth of the network. Thus, the viscosity is expressed as function of temperature, pressure, time (conversion), and shear rate (14).

The dominant chemical reactions in peroxide cross-linking of polyethylene follows three steps namely peroxide decomposition, radical chain transfer, and combination of radicals. The schematic of these steps is shown in Figure (1). There are two methods for tracking the variation of viscosity in accordance with degree of cross-linking; (1) continuous measuring during cross-linking reaction and (2) step by step viscosity measurements by sampling of the cross-linked polymer.

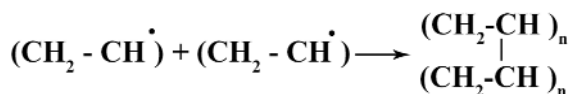
The aim of our work is to measure the viscosity versus degree of cross-linking reaction (during per-



Formation of free initiator radical



Chain transfer



Combination of chain transfer

Figure 1. A schematic of cross-linking reactions of polyethylene

oxide crosslinking reaction) of LDPE at isothermal condition using a combination of DSC and creep test.

## EXPERIMENTAL

### Materials

Low density polyethylene (LDPE), Lupolen 3020D (MFI = 1.5 g/10 min,  $d = 0.913 \text{ g/cm}^3$ ) from Bassel and di-cumyl peroxide (DCP) from Akzo Nobel (perkdox BC-FF trade name) with 98% purity were used.

### Instruments

The conversion of reaction was measured by DSC (Advanced Technology model DSC 1000). Stresstech controlled rheometer (Rheological Instruments AB) was used for creep test in plate/plate geometry ( $D = 20 \text{ mm}$ ). Special single use plate-plate geometry was used for easy and safe cleaning tests [14] (Figure (2))

### Method

Polyethylene and 2 wt% DCP were mixed in 60 cm<sup>3</sup> Brabender internal mixer at 130°C, under the safety temperature of DCP (140°C). The DSC and creep experiments carried out in isothermal condition at 150, 160, and 170°C. The levels of stress in creep test were 5000, 10000, and 15000 Pa.

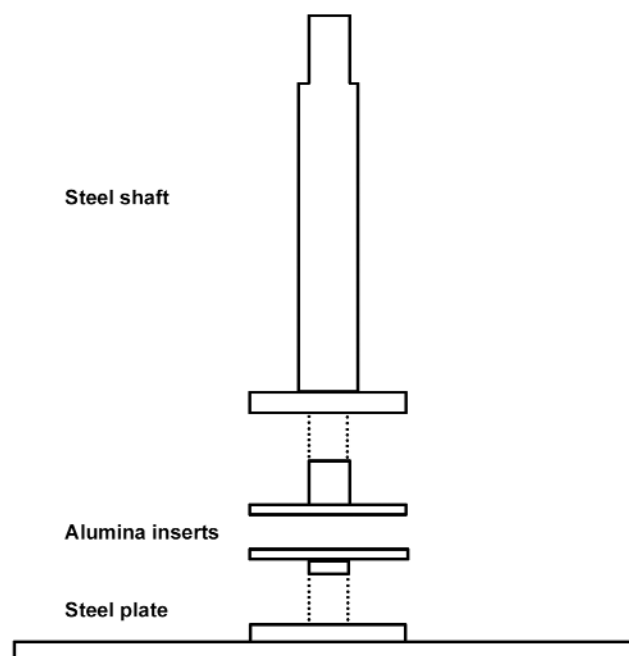


Figure 2. A schematic of the plate/plate geometry [14].

## RESULTS AND DISCUSSION

We considered viscosity as function of time (cross-linking reaction) and shear rate, so in isothermal shear deformation, the stress can expressed as :

$$\tau_{yx} = \eta_{yx} (t, \dot{\gamma}_{yx}) \dot{\gamma}_{yx} \quad (1)$$

At constant stress we may show that [14]:

$$\left(\frac{\partial \eta}{\partial t}\right)_{\sigma} = -\left[\frac{\eta}{\gamma_{yx}} + \left(\frac{\partial \eta}{\partial \gamma_{yx}}\right)_t\right] \left(\frac{\partial \dot{\gamma}_{yx}}{\partial t}\right) \tau_{\sigma} \quad (2)$$

Similarly, at constant time, we may drive the expression:

$$\left(\frac{\partial \tau_{yx}}{\partial \dot{\gamma}_{yx}}\right)_t = -\dot{\gamma}_{yx} \left[\frac{\eta}{\gamma_{yx}} + \left(\frac{\partial \eta}{\partial \gamma_{yx}}\right)_t\right] \quad (3)$$

With combining equations 2 and 3, we obtain:

$$\left(\frac{\partial \eta}{\partial t}\right)_{\sigma} = \frac{1}{\dot{\gamma}_{yx}} \left(\frac{\partial \tau_{yx}}{\partial \dot{\gamma}_{yx}}\right)_t \left(\frac{\partial \tau_{yx}}{\partial t}\right) \tau_{\sigma} \quad (4)$$

In the above equations  $\eta$ ,  $\tau$ ,  $t$  and  $\dot{\gamma}_{yx}$  are viscosity, shear stress, time and shear rate, respectively. Equation (4) relates the reaction dependence of viscosity to quantities measurable in a creep experiment. The conversion of cross-linking reaction ( $\alpha$ ) was determined according to eqn (5).

$$\alpha = \frac{H(t)}{H_u} \quad (5)$$

Where  $H(t)$  is heat released by the cross-linking reaction up to time  $t$  and  $H_u$  is the summation or ultimate heat of reaction. Hence the change in viscosity due to reaction can be expressed as

$$\left(\frac{\partial \eta}{\partial \alpha}\right)_{\dot{\gamma}_{yx}} = \left(\frac{d\alpha}{dt}\right)^{-1} \left(\frac{\partial \eta}{\partial t}\right)_{\dot{\gamma}_{yx}} \quad (6)$$

Where  $d\alpha/dt$  is determined from isothermal DSC experiments and  $(\partial \eta / \partial t)_{\dot{\gamma}_{yx}}$  is determined from creep experiments.

In eqn (1) it is assumed that the time scale for the chemical reaction (cross-linking) can be separated from

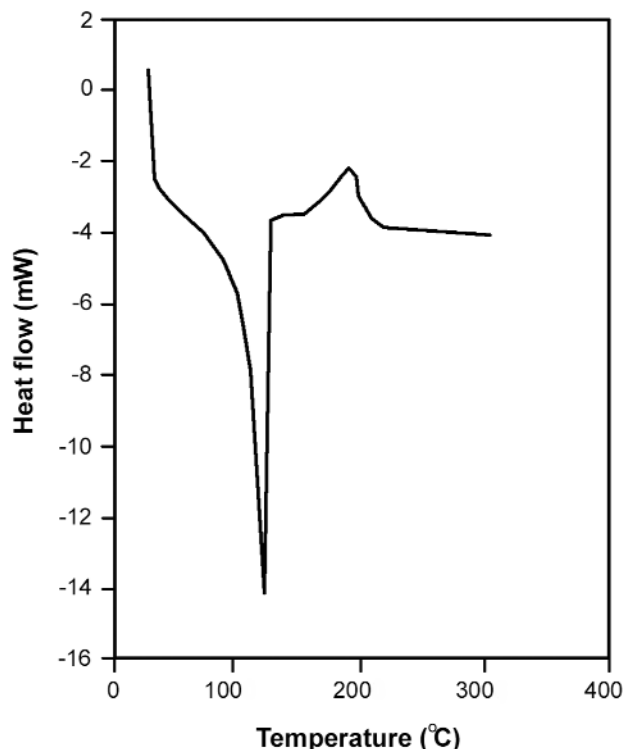


Figure 3. Dynamic DSC scan of LDPE with 2 wt % of DCP.

viscoelastic relaxation. Therefore, it needs to be determined in which condition the equation applies.

Figures 3-5 show the data obtained from dynamic and isothermal (160°C) DSC scans and  $H(t)$  for LDPE with 2 wt% of DCP, respectively. In Figure 3 the

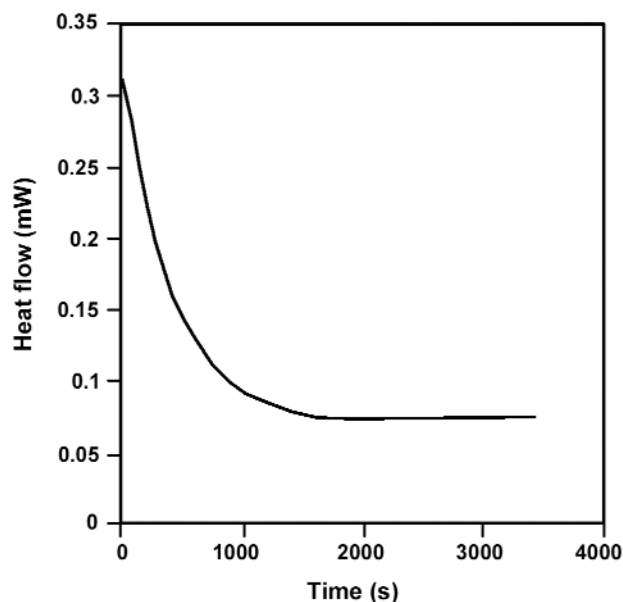
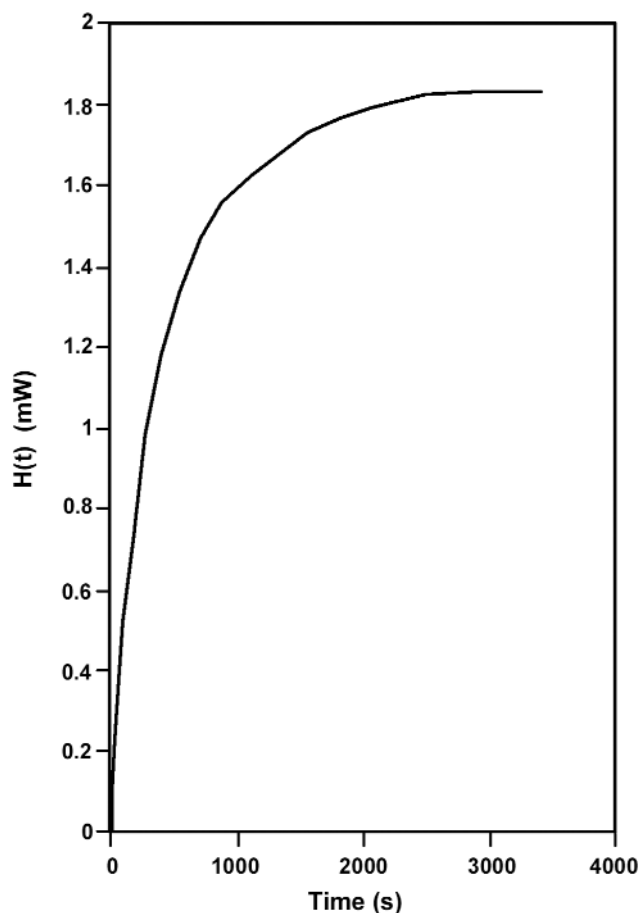


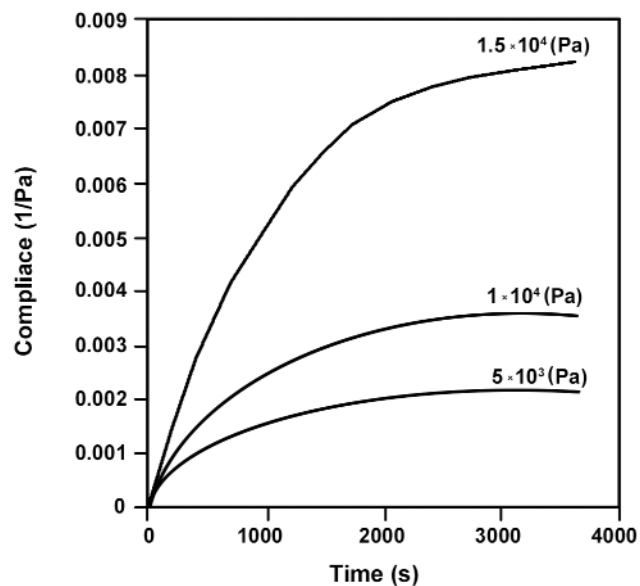
Figure 4. Isothermal DSC scan of LDPE with 2 wt% of DCP at 160°C.



**Figure 5.** Heat of reaction up to time  $t$  for LDPE with 2 wt% of DCP at  $160^{\circ}\text{C}$ .

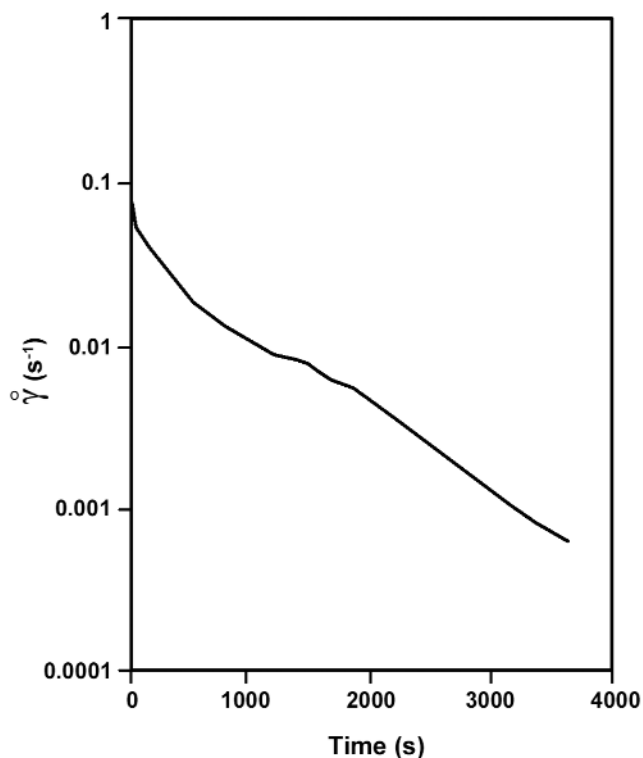
exothermic peak after the melting point is relevant to the cross-linking reaction. By increasing of DCP wt%, the area under the peak and the rate of reaction increase. By doing the dynamic scan after isothermal experiments on the same sample, there was no exothermic peak and it seems that cross-link reaction has been completed.

Figure 6 shows the creep compliance,  $J_c$  versus time at three levels of stress at  $160^{\circ}\text{C}$ . Below the 5000 Pa the data were very noisy and beyond the sensitivity of instrument. According to above equations for obtaining of  $\dot{\gamma}$  and  $\partial\dot{\gamma}_{yx}/\partial t$  for determining the dependency of viscosity to degree of reaction, we should determine derivatives of creep compliance for two times. Because of small-scale fluctuation in these data, we were not able to obtain any derivative by simple difference scheme. For manipulation of data smoothing the average of five point technique was applied. This simple technique can eliminate noises [15].



**Figure 6.** Creep compliance of LDPE with 2 wt % of DCP at  $160^{\circ}\text{C}$  and different stress levels.

Figures 7 and 8 show an approximation of shear rate value and its time derivative at  $160^{\circ}\text{C}$  and  $10^4$  Pa, respectively. Figure 9 shows  $(\partial\eta/\partial t)\dot{\gamma}_{yx}$  versus time at  $160^{\circ}\text{C}$  and  $10^4$  Pa. The rate of cross-linking reaction increases via increasing temperature which is revealed



**Figure 7.** Shear rate at  $10^4$  Pa and  $160^{\circ}\text{C}$ .

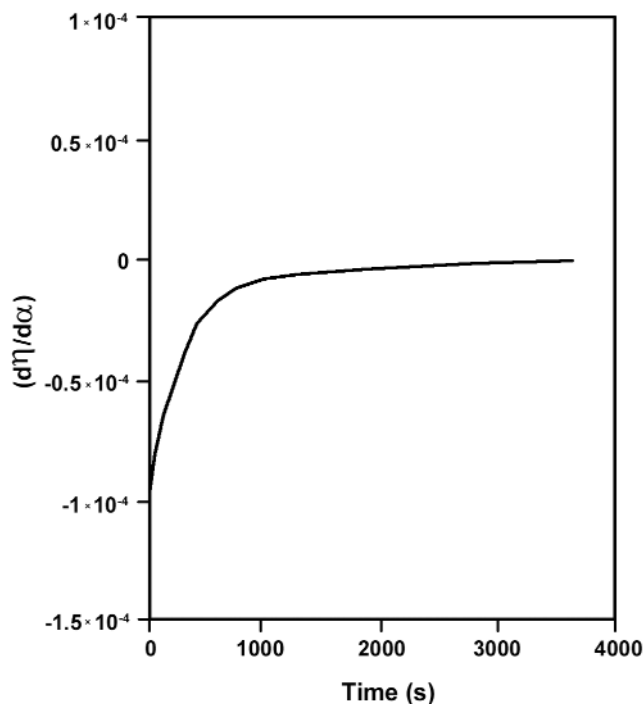


Figure 8. Time derivative of shear rate at  $10^4$  Pa and  $160^\circ\text{C}$ .

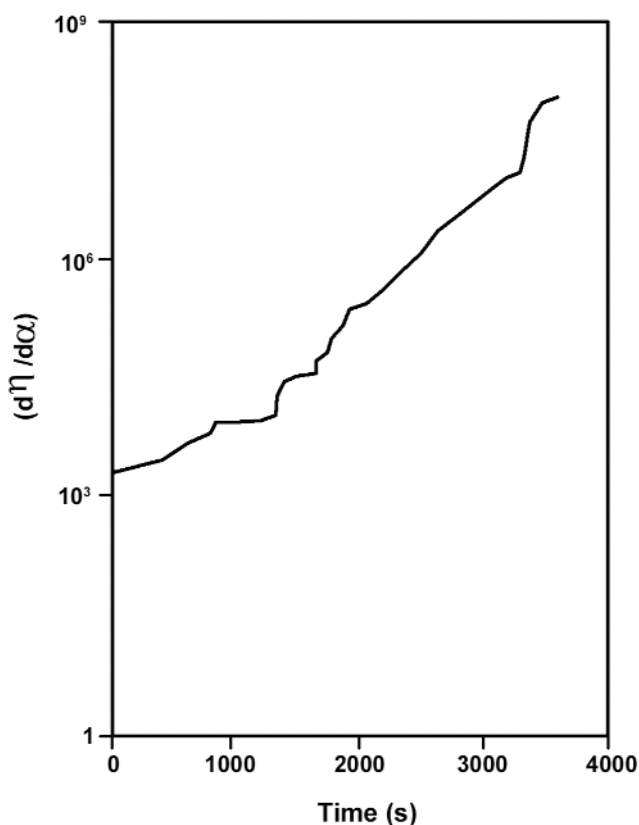


Figure 9. Variation of  $(d\eta/d\alpha)_0$  vs. time at  $10^4$  Pa and  $160^\circ\text{C}$ .

in the slope of the curves. It is obvious that by preceding the cross-linking reaction, viscosity increases and the major increment takes place in the first stage of reaction.

## CONCLUSION

During peroxide cross-linking reaction of LDPE, by combining DSC and creep experimental data one can determine the dependency of viscosity on the degree of cross-linking reaction. The analysis would be more accurate if plenty of creep tests could be conducted under variety of stress levels.

Without employing smoothing operation on data, the derivatives cannot be represented by simple difference scheme, it seems that, noise elimination is necessary to continue the analysis by this method.

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