



## Integration of Multi-period Vehicle Routing Problem and Economic Selection of Customers with the Objective of Optimizing Distribution, Sales and Discounts Planning

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### ABSTRACT

Making decisions about the economic selection of the customers plays a significant role in the sale and logistic management of the companies. Furthermore, another issue affecting the relationship between the suppliers and the customers is the proper and timely distribution of the products as well as the optimum mixing of the distribution routes to reduce transportation costs. In this paper, the issues of the integration of routing, and the economic selection of customers has been explored aiming at minimizing the transportation, maintenance, and discount costs and maximizing the products selling profits. In addition, to the amount of customer's purchasing, customers' collection period is effective to offer them discounts. The economic customers are selected due to three factors: the discount on the price of the product, the marginal profit of the requested products, and the distance from the supplier's warehouse. Games software was used for the exact solution of the model, and Simulated annealing algorithm was used to solve the model in larger dimension. The efficiency and applicability of the proposed model was approved comparing the optimum results with a high preciseness as 98.91 percent. Moreover, in the case study of Kalleh Company, the results revealed 14% increase in pure profits.

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## 1. INTRODUCTION

Selecting the proper set of customers and having continuous relationship with them is important and vital for a company to be successful. The main objective of the customers' selection process is to reduce the risk of sales, maximize the overall sales value, and develop long-term relationships between customer and supplier. Choosing appropriate customers can significantly decrease distribution, sales, and discounts costs and increase the competitive capabilities of the organization. Furthermore, vehicle routing problem arises to reduce the transportation cost and increase customer's satisfaction from the proper and timely distribution of the products. The vehicle routing problem arises, in many companies, while the goods should be transported

from the suppliers to the customers [1]; so that, the reduction of the transportation costs plays an important role in reducing the total price.

Those customers should be chosen that can provide the most benefits for the company due to the resources of the company as well as the supply and distribution costs used for them. This profitability is composed of a series of factors such as having fewer discounts, buying more, buying more profitable products, paying on time, and being close to the warehouse in order to reduce the distribution costs. The managers of the companies and factories need some tools to identify the economic customers to whom they can concentrate their time and money and avoid providing service to the customers who are unprofitable or return little benefit to the company spending the resources, funds, and time of the suppliers. Till now, many researches have been done concerning with multi-period routing, customer selection, discount on purchasing costs, reduction in

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transportation costs, maintenance of the inventory in the stock, increase in the profits of selling various products, and the capacities of the vehicles and warehouse, separately. However, we need an operational mathematical programming model with controllable complexity that considers all the above-mentioned cases together. In this paper, a mixed integer linear programming model is proposed for the integration of multi-period vehicle routing problem as well as the selection of the economic customers aiming at reducing the transportation and maintenance costs and increasing the benefits of selling the products. Moreover, to be more realistic, while selecting the customers, the marginal profits of the requested products and the payment period were taken into consideration besides the amount of the purchased products and the customers' distance from the warehouse.

In the second section of paper, a review of literature on routing, the economic selection of the customers, the discount on the price, the decrease in transportation and maintenance costs, and the increase in the profitability have been presented. The third section includes the definition and the hypotheses that are concerned with the problem as well as the related mathematical model. In the fourth section, to ensure the efficacy and applicability of the model and clarify its meaning, a small sample of the problem is taken into consideration and the effect of the priority of the intended functions on the optimal results is examined. In the fifth section, the steps of SA algorithm and the methods of codification of the answers are expressed. The sixth section shows the applicability of the proposed method using several real problems in different dimensions. In the seventh section, a case study is provided. Finally, the results of the study are explained in section 8.

## 2. LITERATURE REVIEW

Bakal et al. [2] established new dimensions in supply chain planning problems assuming that an inventory planning model, instead of having a specific definite or probable request, can have some demands from different markets or customers. This model includes the selection of appropriate markets and customers from the available requested basket. Geunes et al. [3], in their first study, in areas of simultaneous market selection and production planning, explored a model in which, a manufacturer, in the single phase production, encounters some demands from the customers that he can optionally choose or reject them. Rabbani et al. [4] studied (VRP) with multi middle depots and one origin depot. In which, distribution costs are minimized and the freshness of the products delivered to the customers and the expected total profit are maximized simultaneously in one objective. In the proposed model, some customer may not receive the service because of

reducing costs. Padasht et al. [5] proposed a model which has a three-level supply chain problem consists of suppliers, distribution centers and damaged areas. The objective is to determine a few relief distribution centers between candidate areas to minimize total costs. Zabihi et al. [6] developed a hybrid MCDM method for evaluating and selecting the marine container transshipment hub port. By using the results of this research, managers of shipping lines will be able to identify the Iranian container hub port and then make more precise decisions in determining the most cost effective voyage loop for their liners. Geunes et al. [7] presented a planning model of multi-period needs with a limited time period, in the single phase production, with some constraints in production capacity, and with a mixed integer programming formulation to express the relationship between the pricing of the product and making decisions about acceptance or rejection of the demands. Over the recent years, attention has been paid to multi-objective vehicle routing. The amount of goods transported in each route, the number of the customers transported in each route, the length of the paths, and the time needed for crossing the paths are among the objectives explored in these studies [8].

Ballou [9] estimated that the costs of maintaining the inventory in any situation, over a year, are 20-40% of the total value of inventory. However, the maintenance of the inventory is necessary to increase the level of service provision to the customer and reduce the supply and distribution costs. However, managing these inventories in a scientific way to keep a minimum inventory causes the reduction in total costs. Apte and Viswanathan [10] express that over 30% of goods price is incurred in distribution process. Thus, the efficient solution on inventory control and distribution management is a vital success factor for companies [11, 12]. Hua et al. [13] by exploring the discount and transportation costs in newspaper seller problem with random demand optimized the sale's price of the product and purchase quantity of the retailers simultaneously. The obtained results showed that having some discount in transportation costs, encourages the retailers to increase their purchases in each period to reduce the total price of the goods for the customer. Setak et al. [14] assumed a firm tries to determine the optimal price, vehicle route and location of the depot in each zone to maximise its profit.

Mirzaee et al. [15] investigated a multi-product multi-period inventory-routing issue on a two-level supply chain system, to minimize the total costs, including the start-up, distribution, and inventory maintenance costs. Lee et al. [16] proposed an integer linear programming model for the price of their products, aiming at reducing the costs of purchasing, storing, ordering, and transportation in general extenuating circumstances. This model was intended to determine the level of replenishment of the materials.

They solved the model by genetic algorithm. Moreover, Lee et al. [17] explored the model considering the price with its detailed and general discount. In another similar study, Fereiduni et al. [18] presented a p-robust model for humanitarian logistics in emergency situations to minimize unsatisfied demands, the government's total cost and the suppliers' shipping costs, when the government of the affected area declines offers of aid from international organizations because of political constraints.

A review of the literature indicates that extensive research has been done in the area of vehicle routing and selection of the customers, separately; however, in the literature, there is no simultaneous investigation of these two issues aiming at reduction in the costs of transportation, the cost of maintenance of the inventory, transportation costs, discounts, and increase in the profits.

One of the key issues in the marketing (sales) and distribution organizations is the timely payment of the customers, because, normally, in high volume purchases, the customers do not pay in cash for the purchased products. Therefore, the money of the company will remain with the customers for some times. By increasing the collection period of the customers' receivables, the profit of the organization reduces. According to the above mentioned studies, this issue has not been studied as a factor influencing the right choice of the customers. Moreover, in the marketing organizations, discounts are considered to be part of the Sale Costs. Thus, one of the strategic objectives of the senior managers is to control the discounts offered to the customers and prevent unnecessary discounts in order to control the ratio of the prices to sales in the organization. Therefore, consideration of discounts offered to the customers as an influential factor in the selection of the customers is one of the innovations of this article. In the issues concerned with the sale and distribution of multi-products, one of the concerns of the organization is the increase in the profit margins. Different products have different profit margins. Therefore, the optimal combination of different products aiming at an increase in the profit of the organization has not been considered as a factor influencing the selection of customers in any of the studied articles.

In this paper, the issue of joint optimization of the planning of the distribution, marketing (sales), and discounts of multi-products in multi-periods have been explored in the issue of vehicle routing. To this end, a mixed-integer linear programming model is provided to have a simultaneous selection of the customers and vehicles routing. The collection period of the customers' receivables, the marginal profit of company, requested discounts, and distance from the supplier warehouses is considered as the factors influencing the choice of customers.

### 3. MATHEMATICAL MODEL

The integration of the economic selection of the customers and routing policies reduces the costs of the total system, considering the value of the currency. In this study, the last level of the supply chain, i.e. the sales branch of the organization, is taken into consideration. The supplier intends to collect the customers' orders for several future periods and design a selling plan for the products. The planning periods could be weekly, monthly, and so on. The orders are definite. If the orders are less than the goods stored in the warehouse, the goods will be maintained in the supplier's warehouse. The capacity of the supplier's warehouse is fixed and specified from the beginning. The inventory is considered to be zero at the beginning of the first planning period, and the inventory at the end of each period will be transferred to the next period. The suppliers offer an  $m \times n$  discounts level to encourage the customers to buy more, and each customer can invest merely in one discount level. Giving discounts to the customers is based on their amount of purchasing and their collection period. The seller does not have to send the products to all of the customers. He can select them based on the costs and the benefits they impose to the company. The capacity of the vehicles sent by the seller is limited, and the seller can use the vehicles with different capacities.

#### 3.1. The Parameters of the Model

$i$  : index of customers ( $i=0,1,2,\dots,I$ )  
 $m$  : index of discounts levels for the quantity of purchasing ( $m=1,2,\dots,M$ )  
 $n$  : index of discounts levels for the customer's collection period ( $n=1,2,\dots,N$ )  
 $t$  : index of planning period ( $t=1,2,\dots,T$ )  
 $v$  : index of vehicle ( $v=1,2,\dots,V$ )  
 $k$  : index of the type of product ( $k=1,2,\dots,k$ )  
 $g_t$  : The largest storage capacity in period  $t$   
 $h_{kt}$  : cost of maintaining the inventory of the product, type  $k$ , in period  $t$   
 $r_k$  : price of one unit of the product, type  $k$   
 $y_k$  : marginal benefits of one unit of the product, type  $k$   
 $d_{ikt}$  : order of customer  $i$  for product  $k$  in period  $t$   
 $c_{ij}$  : cost of travel from node  $i$  to node  $j$   
 $f_v$  : set up or application cost of the vehicle  $v$   
 $c_v$  : capacity of vehicle  $v$   
 $b_m$  : the lowest amount of discount span  $m$  for the price  
 $p_m$  : the highest amount of discount span  $m$  for the price  
 $a_n$  : the lowest amount of discount span  $n$  for the price  
 $w_n$  : the highest amount of discount span  $n$  for the price  
 $O_{ikt}$  : collection period for customer  $i$  to buy the product type  $k$  in period  $t$   
 $e_{imnkt}$  : the Discount percent given to the customer  $i$  for buying the product type  $k$  in period  $t$  in  $m$  price level and  $n$  collection period level.

$s_{kt}$  : quantity of the offers of the product type k in period t

$\alpha_j$  : weight of the target function j

### 3. 2. The Decision Variables

$x_{ijvt}$  : If vehicle v travels from the customer i to the customer j in period t, this variable is equal to one and otherwise it is zero.

$I_{kt}$  : the inventory of the product type k at the end of period t

$q_{inkt}$  : If the collection period of the customer i in period t is in discount span n, the variable is equal to one and otherwise it is zero.

$L_{imkt}$  : If the demand of the customer i in period t is in discount span m, the variable is equal to one and otherwise it is zero.

$u_{jimmvkt} = q_{inkt} * x_{ijvt} * L_{imkt}$  (This binary variable was added to linearize the model)

$y_i$  : auxiliary variable to eliminate the sub tour

### 3. 3. The Mathematical Model of the Problem

$$\text{Max } \alpha_1.z_1 \quad \text{Min } \alpha_2.z_2 + \alpha_3.z_3 \tag{1}$$

$$z_1 = \sum_{i=0}^I \sum_{j=0}^J \sum_{t=1}^T \sum_{v=1}^V \sum_{k=1}^K x_{ijvt} . D_{ikt} . Y_k . r_k - \sum_{i=0}^I \sum_{m=1}^M \sum_{n=1}^N \sum_{t=1}^T \sum_{j=1}^J \sum_{v=1}^V \sum_{k=1}^K u_{jimmvkt} . e_{imkt} . D_{ikt} . r_k - \sum_{t=1}^T \sum_{k=1}^K S_{kt} . r_k \tag{1-1}$$

$$z_2 = \sum_{i=0}^I \sum_{j=0}^J \sum_{t=1}^T c_{ij} \sum_{v=1}^V x_{ijvt} + \sum_{i=0}^I \sum_{v=1}^V \sum_{t=1}^T f_v . x_{0jvt} \tag{1-2}$$

$$z_3 = \sum_{t=1}^T \sum_{k=1}^K h_{kt} . I_{kt} \tag{1-3}$$

$$\sum_{k=1}^K I_{kt} + \sum_{i=1}^I \sum_{j=1}^J \sum_{v=1}^V \sum_{k=1}^K D_{ikt} . x_{ijvt} = \sum_{k=1}^K S_{kt} + \sum_{k=1}^K I_{kt-1} \tag{2}$$

$t=1,2,\dots,T$

$$\sum_{m=1}^M L_{imkt} . b_m \leq D_{ikt} \leq \sum_{m=1}^M L_{imkt} . b_{m+1}; \tag{3}$$

$i=1,2,\dots,I \quad t=1,2,\dots,T \quad K=1,2,\dots,K$

$$\sum_{n=1}^N q_{inkt} . a_n \leq O_{ikt} \leq \sum_{n=1}^N q_{inkt} . a_{n+1}; \tag{4}$$

$i=1,2,\dots,I \quad t=1,2,\dots,T \quad K=1,2,\dots,K$

$$\sum_{m=1}^M L_{imkt} = 1; \tag{5}$$

$i=1,2,\dots,I \quad t=1,2,\dots,T \quad K=1,2,\dots,K$

$$\sum_{n=1}^N q_{inkt} = 1; \tag{6}$$

$i=1,2,\dots,I \quad t=1,2,\dots,T \quad K=1,2,\dots,K$

$$3 * u_{jimmvkt} \leq q_{inkt} + L_{imkt} + X_{ijvt};$$

$$u_{jimmvkt} \geq q_{inkt} - M (1 - L_{imkt}) - M (1 - X_{ijvt})$$

$$u_{jimmvkt} \geq X_{ijvt} - M (1 - L_{imkt}) - M (1 - q_{inkt})$$

$$u_{jimmvkt} \geq L_{imkt} - M (1 - X_{ijvt}) - M (1 - q_{inkt})$$

$i=1,2,\dots,I \quad m=1,2,\dots,M \quad n=1,2,\dots,N$   
 $t=1,2,\dots,T \quad K=1,2,\dots,K \quad v=1,2,\dots,V \quad j=1,2,\dots,J$

$$\sum_{i=1}^I \sum_{k=1}^K D_{ikt} . \sum_{j=1}^J x_{jivt} \leq cv \tag{8}$$

$t=1,2,\dots,T \quad v=1,2,\dots,V$

$$\sum_{i=1}^I x_{ijvt} \leq 1; \tag{9}$$

$t=1,2,\dots,T \quad v=1,2,\dots,V \quad J=1,2,\dots,J$

$$\sum_{i=1}^I x_{ipvt} - \sum_{j=0}^J x_{pjvt} = 0; \tag{10}$$

$p=1,2,\dots,I \quad t=1,2,\dots,T \quad v=1,2,\dots,V$

$$\sum_{i=1}^I \sum_{j=0, j \neq i}^J x_{ijvt} \leq M \sum_{j=1}^J x_{0jvt}; \tag{11}$$

$t=1,2,\dots,T \quad v=1,2,\dots,V$

$$\sum_{i=1}^I \sum_{v=1}^V x_{ijvt} \leq 1 \quad j=1,2,\dots,I \quad t=1,2,\dots,T \tag{12}$$

$$Y_i - Y_j + M * X_{ijvt} \leq M - 1; \tag{13}$$

$i=1,2,\dots,I \quad t=1,2,\dots,T \quad v=1,2,\dots,V \quad j=1,2,\dots,J$

$$0 \leq I_{kt} \leq g_{kt}; \quad t=1,2,\dots,T \tag{14}$$

$$y_i, I_t \in \text{Integer}; x_{ijvt}, L_{imkt}, q_{inkt}, u_{jimmvkt} \in \{0,1\} \tag{15}$$

$\forall i, j, v, m, n, k, t$

### 3. 4. Introducing the Target Functions of the Multi-product Problem

The target function, in the stated mathematical model, consists of three parts: The first part (1-1) of the function tries to maximize the

profit of selling the products and minimize the purchasing and discount costs. The second part of the target function (1-2), which has been used to reduce the number of vehicles and distances, demonstrates the travel costs. The third part of the target function (1-3), tries to minimize the maintenance costs of the products that remain in the stocks, at the end of the period.

**3. 5. Introducing the Limitations of the Model**

Limitation (2), in each planning period, estimates the offer of the intended period, based on the inventory remaining at the end of the previous period and the amount of production in the same period. If the total numbers of orders are more than the estimated offer in the intended period, the model omits the non-economic customers considering other limitations until the offer become equal to/greater than the total orders. Limitation (3) limits the amount of the orders at every price level to the upper and lower limits of that level. Limitation (4) limits the collection period at every collection level to the upper and lower limits of that level. Limitation (5) ensures that, in each period, each customer must receive the service at just one level of the offered discounts. Limitation (6) ensures that, in each period, the collection period for each customer must be just in one level of the offered discounts. Limitation (7) is the Linearization constraint. Limitation (8) states that the total demands of the customers in a path should not exceed the capacity of the vehicle allocated to that path. Limitation (9) states that each vehicle, in each period, should enter from maximum one node to the target node. Limitation (10) ensures that, in each period, if a vehicle enters a node, it must get out of it. Limitation (11) states that if the vehicle is going to switch between two nodes, it should, first, get out of the supplier's warehouse. Limitation (12) states that, in each period, it is just possible to enter the intended node from just one node and with just one vehicle. Limitation (13) is the sub tour elimination restriction. Limitation (14) states, in each period, it is not possible to store the goods over the storage capacity of the warehouse. Limitation (15) defines the binary and integer variables of the problem.

**4. NUMERICAL EXAMPLE**

In this section, in order to ensure the proper function of the model and clarify its meaning, a small sample of the problem will be examined. Then, solving the model will be explored by a meta-heuristic method; and the results of the solution will be compared, using the exact method and the meta-heuristic algorithm. For this purpose, suppose that the director of the supply section of a company decides to select from 10 customers who have ordered to the company, he should take into consideration the limitations in the offering of the

products, payment conditions, the quantity of the orders, and also their distance from the warehouse. Moreover, he should select the customers who can reduce the transportation, discount, and maintenance costs of the product being stored in the stock and increase the profits of selling products, for a 2-month planning period. The company supplies three products with different prices and different marginal profits. Table 1 reveals the price, marginal profit, and offering of each product, in each period. The offering of the products in various periods, is different. It is in such a manner to be possible to evaluate its impact on the maintenance cost of the products.

The seller has 2 vehicles to provide some services to the customers, in each period. The capacity of the first vehicle is 140 units, and the capacity of second one is 120 units. The cost of starting up for the vehicles is fixed, in each period, and the cost, for the first vehicle, is equal to 10 currency units and for the second one equal to 8 currency units. The maintenance cost is 2 currency units per each unit of the goods. Moreover, the capacity of the warehouse is fixed and equal to 100 units, in each period. The customers' distances from each other and the central depot are taken into consideration in a symmetric manner.

In Table 2, the orders and the collection period of each customer, in different periods, are proposed. For customers with higher average orders, higher collection period is considered. Therefore, the model can select the best customers both in terms of their orders and in terms of their collection period.

The suppliers consider three levels of discounts for the quantity of purchase and three levels of discounts for the duration of payment to encourage the customers to buy more quantity of the product and pay it in less time span. Thus, each customer will be faced with 9 levels of discounts. This means that if the customer's order is at m discount level and the collection period of the customer is at n discount level, then the customer can get e percent of discount. Discount intervals are shown in Table 3.

In this paper, GAMS22.2 linear programming software package is used to solve the problem. The mixed-integer programming optimization Packages like Gams can reach the general optimal answer or guarantee the answers with acceptable relative optimality gap.

**TABLE 1.** Price, margin of product and offer of each product in each period

product	price (currency unit)	margin (percent)	offer of first period	offer of second period
1	3	1.07	95	100
2	4	1.03	90	90
3	6	1.04	85	90

**TABLE 2.** Demand and collection period of customers in different periods

customer	collection period		product	demand	
	first period	second period		first period	second period
1	5	4	1	13	15
			2	20	17
			3	10	13
2	2	4	1	12	16
			2	8	12
			3	15	10
3	4	5	1	13	17
			2	11	11
			3	12	12
4	3	6	1	5	6
			2	10	15
			3	15	18
5	10	8	1	17	15
			2	11	10
			3	9	8
6	6	7	1	6	12
			2	7	13
			3	10	15
7	8	11	1	22	24
			2	18	19
			3	8	10
8	2	3	1	11	16
			2	8	10
			3	10	12
9	8	2	1	16	10
			2	17	12
			3	13	15
10	5	10	1	5	9
			2	12	12
			3	16	16

The inputs in this model include: the demand of the customers, the customer's collection period, the cost of transportation from depot to the customer and from a customer to another customer, the offer of each product in each period, the number of the vehicles in different types, the capacity of each type of the vehicles, the start up costs of any vehicle, the vendor's storage capacity, the number of the periods, the discount levels, the price and the marginal profit of any kind of product. The outputs of the model include: the selected customers in

each period to send the goods to them and the quantity of their purchase, the number of the required vehicles of any kind, the optimal route for shipping, identification of the point that which type of vehicle with what capacity should move towards which customers, the total distribution, discounts, and maintenance costs, the quantity of each type of product being sold, and the profits obtained from selling the products.

The results obtained by solving the model by Gams software are shown in Tables 4 and 5. Table 4 specifies the route of the vehicles in each planning period. Table 5 shows the number of the goods sold from each discount level in each planning period.

**TABLE 3.** Discounts level

discount level	demand ( $D_{imt}$ )	&	collection period ( $O_{mt}$ )	discount percent ( $e_{immt}$ )	discount parameter
1	$0 < D < 7$	&	$0 < O < 3$	0%	$e_{i11}$
2	$0 < D < 7$	&	$3 \leq O < 9$	0%	$e_{i12}$
3	$0 < D < 7$	&	$O \geq 9$	0%	$e_{i13}$
4	$7 \leq D < 14$	&	$0 < O < 3$	1.5%	$e_{i21}$
5	$7 \leq D < 14$	&	$3 \leq O < 9$	1%	$e_{i22}$
6	$7 \leq D < 14$	&	$O \geq 9$	0%	$e_{i23}$
7	$D \geq 14$	&	$0 < O < 3$	2%	$e_{i31}$
8	$D \geq 14$	&	$3 \leq O < 9$	1.5%	$e_{i32}$
9	$D \geq 14$	&	$O \geq 9$	0%	$e_{i33}$

**TABLE 4.** Shipping route of vehicles

row	from customer	to customer	vehicle	planning program	
				first	second
1	i0	j4	v2	1	
2	i0	j6	v2		1
3	i0	j7	v1	1	1
4	i4	j9	v2	1	
5	i7	j3	v1		1
6	i7	j6	v1	1	
7	i6	j10	v1	1	
8	i6	j10	v2		1
9	i9	j1	v2	1	
10	i10	j3	v1	1	
11	i10	j4	v2		1
12	i3	j1	v1		1
13	i1	j0	v1		1
14	i1	j0	v2	1	
15	i3	j0	v1	1	
16	i4	j0	v2		1

The results indicate that the customers 1, 3, 4, 6, 7, 9 and 10 are selected in the first period in such a way that the vehicle 1 gets out of the warehouse and goes, respectively, toward the customers 7, 6, 10 and 3, and finally returns to the warehouse. On the other hand, the vehicle 2 gets out of the warehouse and goes, respectively, toward the customers 4, 9 and 1, and finally returns to the warehouse. In the second period, the customers 1, 3, 4, 6, 7 and 10 are selected. The process is in such a way that the vehicle 1 gets out the the warehouse and goes, respectively, toward the customers 7, 3 and 1, and finally returns to the warehouse. On the other hand, the vehicle 2 gets out of the warehouse and goes, respectively, toward the customers 6, 10 and 4, and finally returns to the warehouse.

In order to explore the effect of the priority of the target functions on the optimal results, seven different ways of priority determination of the target functions will be studied. The target function is considered as the gross profit, minus the transportation and maintenance costs. It is worth noting that the gross profit includes the income gained from selling the products, minus the cost of purchasing the products and the discounts cost.

Table 6 shows that the customers who are selected and the number of them are different based on the priorities of the target functions in each problem. The model selects the customers and the best routes for them in the planning stage, counterbalancing and considering the priority of the target functions.

According to the results of Table 6, it can be considered that when it is intended to reduce the maintenance costs, the customers that have much larger orders and will result in more sales will be selected.

In the problem 3, the goal is merely to maximize the gross profit (selling revenue minus the costs of purchasing and discounts). The best policy, in these problems, is to have larger order sizes with greater marginal profit. The variations in the target functions in order to create a balance between seven problems, mentioned above, are shown in Figure 1. Figure 1 shows that, if the maintenance costs are disregarded, these costs will increase severely, and even they will be equal with the shipping costs. It is obvious in the problems 2, 3 and 5. Comparing the problems 2 and 3, the importance of paying attention to the transportation costs is highlighted. This figure also shows that paying attention to the transportation costs can reduce the total cost, almost as much as the costs of purchasing and discounts.

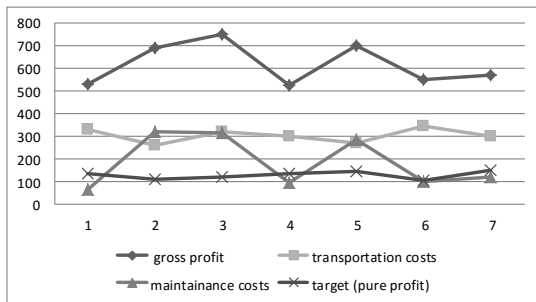
The minimum pure profit is related to the problem 6, in which the buyers merely pay attention to the costs of purchasing the product, discount, and maintenance. In the problem 5, the simultaneous attention to the transportation, purchasing, and discounts costs as well as the marginal profit can increase the pure profit significantly. The optimum solution will be obtained when all the costs are taken into account, equally (problem 7).

TABLE 5. Amount of the goods sold from each discount level in each planning period

customer	product	planning period				customer	product	planning period			
		first		second				first		second	
		order quantity	discount level	order quantity	discount level			order quantity	discount level	order quantity	discount level
	1	13	5	15	8	1	6	2	12	5	
1	2	20	8	17	8	6	2	7	5	13	
	3	10	5	13	5	3	10	5	15	8	
	1					1	22	8	24	9	
2	2					7	2	18	8	19	
	3					3	8	5	10	6	
	1	13	5	17	8	1					
3	2	11	5	11	5	8	2				
	3	12	5	12	5	3					
	1	5	2	6	2	1	16	8			
4	2	10	5	15	8	9	2	17	8		
	3	15	8	18	8	3	13	5			
	1					1	5	2	9	6	
5	2					10	2	12	5	12	
	3					3	16	8	16	9	

**TABLE 6.** Numerical results for balancing due to the weight of the objective function on various problems

problem	1	2	3	4	5	6	7
gross profit	532	690	752	528	700	552	570
transportation costs	330	260	320	300	270	345	300
maintainance costs	66	320	313	95	285	102	120
target (pure profit)	136	110	119	133	145	105	150



**Figure 1.** The objective function changes to create a balance between seven problems

In general, we can say that to reduce the price of the goods or services and increase the satisfaction in the customer, a logical exchange between different costs should be established.

In the problem 2, the goal of which is to minimize the transportation costs, the determiner must reduce the number of transports and select the customers with larger order size and lower distance from the warehouse to reduce the number of the vehicles used and the distance traveled. In the problem 3, in which the determiner's attention is focused on the marginal profit of the customer's demand, the supplier gets confused. This is because of the fact that when the customers with higher marginal profit in their overall demands are selected, the gross profit increases, but the pure profit decreases sharply. Thus, the results of excessive attention to the marginal profits of the product and inattention to the cost of transportation can be revealed clearly. The results show that considering all the target functions can increase the pure profit 21%, as an average, compared with the time when only some of them are taken into consideration. It seems that the best ordering policy can be achieved by paying attention to all the costs together, because inattention to one of the costs causes the increase in the costs and decrease in the final profit.

**5. THE SA PROPOSED SOLUTION**

The VRP problem is among the NP-hard problems that require the innovative approaches to solve it in large-

scale [19]. Therefore, an efficient meta-heuristic algorithm based on simulated annealing (SA) is proposed. This algorithm works efficiently on a neighborhood search within the solution space. Moreover, one of the advantages of this algorithm is that it can escape from being trapped in local optima and move toward the target function [20].

The basic steps of the proposed SA algorithm are shown in Figure 2. Before mentioning the steps of SA algorithm, we initially define the input parameters of the problem:

EL = the length of Markov chain (the number of the accepted answers, in each temperature, or the criteria of going out of the inner ring).

MTT = Maximum transitions in the temperature (Stopping the algorithm or the criteria of going out of the inner ring).

T0 = The initial temperature

$\alpha$  = Temperature reduction coefficient

X = Feasible solution

C(X) = the target function value for feasible solution.

M = the counter counting the number of the accepted answer at any temperature.

K = the counter counting the number of the temperature transmissions

**5. 1. The Algorithm Producing the Initial Solution**

Producing the initial solutions is the first step in any meta-heuristic approach. In order to produce the initial solution, the following innovative approach is used:

```

k = 0, T = T0, Xbest = ∅
Generate X0
Xbest = X0
Do (Out Side loop)
    m = 0
    Do (In Side loop)
        Select a operator (1-Opt or 2-Opt)
        Randomly and run over Xm as : Xm → Xnew
        ΔC = C(Xnew) - C(Xbest)
        If ΔC < 0 Then
            Xbest = Xnew and m = m+1 and Xm = Xnew
        Else
            Generate y → U(0.1) Randomly
            Set Z = e-ΔC / Tk
            If y < Z Then m = m + 1 and Xm = Xnew
        End if
    Loop While (m < EL)
    k = k+1
    Tk = Tk-1 - α × Tk
Loop While ( k < MTT and Tk > 0 )
Print Xbest
    
```

**Figure 2.** Basic steps of SA algorithm



1. The formation of the new route: select a car (like  $v$ ) from the available vehicles, by chance, and send it towards a customer (the customers that their total orders for all the products are not more than the capacity of the vehicle).
2. Determining the neighboring nodes: find the closest node to the node  $i$  (such as node  $j$ ) in a way that their total orders for all the products are not greater than the remaining capacity of the vehicle. If such a node is found, send the car  $v$  from the node  $i$  to  $j$ ; Otherwise, send it back to the warehouse.
3. Route completion: Repeat the second step as many times as there remain no customers with his total orders not exceeding the remaining capacity of the car.
4. Tours completion : Then among the available cars, choose another car, randomly. And in the same way mentioned above, a random tour is created for the car. Naturally, the customers who have received the services by the previous car, in the previous step, should be omitted from selection process at this step.
5. Service completion : The process of selecting the car and its corresponding tour, for the first period, continues until either all the customers are serviced or all the cars are selected.
6. When the selections for the first period finished, the same process will exactly continue for the subsequent periods. When, the cars and the corresponding tours are selected for all of the periods, the first stage of producing the initial answer is finished.

### 5. 2. Modifications

The answer produced according to the stages mentioned above, may be unjustified. That can be the result of overstepping from the source (the amount of production in each period). So at this stage, the initial answer will be modified.

For all the periods and in each period for all the machines that are used in the same period, the following process is done:

**Exploring the Limitations in the Capacity of the Car:** If the capacity of the car is violated, select a customer from the corresponding tour of the car, randomly, and omit it. The random selection and omission of a customer from the tour should be continued until the capacity of the car isn't violated.

**Exploring the Limitations in the Produced Recourses:** First, check whether it is possible to provide services to the customers selected for the first period, according to the amount of production, in the same period. If this is not possible, select one of the cars used in the first period, randomly, and select a customer from the corresponding tour by chance, and omit it. Selecting a vehicle and a customer from the corresponding tour, continued until the picked customers could be serviced, due to the production constraints. Then, the remaining productions, move to the next period. Besides, the same activities should be done for the next period.

After producing the initial answers, the value of the corresponding target function is calculated. Calculating the target function the discount level can be calculated, considering the selected customers in each period, the orders, and the collection period of them. Regarding the tours of the cars, the transportation cost is calculated. The maintenance costs are calculated based on the inventory moved from one period to the next. According to the kind of cars used in the answer, the set-up cost of vehicles is calculated.

### 5. 3. How to Produce Neighborhood

Six operators are used to produce neighborhood. Each time producing the neighborhood, one of the operators is randomly selected.

**The first operator:** exchange two customers from two different tours: First of all, a period is chosen, randomly. Then, two cars (which have been used in that period) will be chosen by chance. A customer is selected from the tour corresponding to each vehicle. At last, the two customers are replaced with each other.

**The second operator:** Replacement of two customers in a tour: First of all, a period is chosen, randomly. Then, a car from the same period, is randomly selected. Next, from the tour corresponding to that car, two customers are chosen randomly and are replaced with each other.

**The third operator:** replacement of the vehicles: a period is chosen randomly and a car from the same period is selected by chance. Then, the selected car will be replaced with one of the available vehicles (that was not used in the answer).

**The fourth operator:** Shift a customer of a tour to another tour: First of all, a period is chosen randomly. Then, in that period, a car is chosen randomly and a customer from the corresponding tour of that car is selected. Then, another car is chosen from the same period. At last, the selected customer is eliminated from his previous position and moved to a random position in the tour of the second car.

**The fifth operator:** a period is chosen randomly. Then, a customer from the customers, who were not serviced, is chosen randomly. A car from the same period is selected. Finally, the selected customer is placed in a random position in the tour of that car.

**The sixth operator:** a period is chosen randomly .A customer who was not serviced in that period is chosen randomly. He is replaced with one of the customers who are served during this period. (For choosing the customer, first, a car is selected randomly and then a customer from its corresponding tour is chosen).

### 5. 4. Alignment of the Parameters of SA Algorithm

Alignment and allocation of appropriate parameters may affect the quality of the answer of the algorithm; So Taguchi algorithm is used in this case.

Table 7 shows the factors affecting the answer of the simulated annealing algorithm, which have been considered at three levels:

The experiments were planned based on L9 taguchi orthogonal array. All test results have been estimated in Figure 3.

As it is apparent in Figure 3, the optimal levels for the parameters are: A(2), B(2), C(1), D(1). The final configurations of the parameters for sa algorithm are represented in Table 8.

In all the represented results and the examples of the samples, the parameters have been considered as above.

**6. VALIDATION OF THE MODEL**

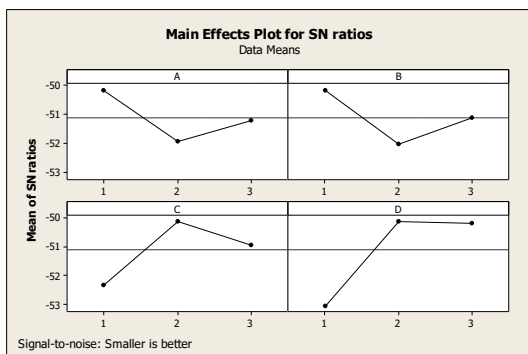
Considering the items designed in the model and the expansions in SA solving methods, a program is written using MATLAB software. Based on the proposed model and its solution using SA Algorithm, in this section, several real problems with various dimensions are selected and it is attempted to solve these problems to show the efficiency and applicability of the model comparing the results of the program written in MATLAB with the answers of Gams software.

**TABLE 7.** Input for simulated annealing method

Factor	symbol	level		
		1	2	3
number of neighbours per iterations	A	3	4	5
number of neighbours per point	B	10	15	20
maximum number of iterations	C	100	70	50
geometric annealing factor	D	0.95	0.9	0.85

**TABLE 8.** Confirmation parameters of simulated annealing algorithm

parameter	A(2)	B(2)	C(1)	D(1)
The optimal value	4	15	100	0.95



**Figure 3.** S/N diagram of simulated annealing

The dimensions of the problem have been determined using I.T.MN.V.K equation, in which I represents the number of the customers, T shows the number of the periods, MN reveals the number of the discount levels, V provides the number of the vehicles, and K presents the number of the products in different kinds. The target function being the profit (the revenue minus the costs of purchasing the product, discounts, shipping, and maintenance) and the time required in order to get to the answer are shown in Table 9.

Comparing the results of SA with the optimum results of Gams, it can be concluded that the software used based on the SA algorithm has the capability to come to the optimum answer while solving problems. On the other hand, estimating the time required for solving the problem in both the SA and Gams models, it is revealed that there is severe increase in the time needed for solving the problem in Gams model, while the time needed to solve the problem by SA algorithm increases slightly in high dimensions. Studying the increase in the time needed for solving the problem, the impact of increasing the variety of the products in increasing the required time could be observed. The results provided in Table 8 show that the answers of the suggested method deviate from the optimal answers 3.93 percent, as an average.

**7. CASE STUDY**

In order to explore the efficacy of the proposed algorithm, a real problem has been studied. The case study in this paper is Kalleh Company, one of the largest producers and distributors of dairy, meat, and drinks in Iran. The products of this company are offered to the market in more than 400 various types. Kalleh Company has a marketing representation in Shiraz. This branch sells the products to more than 2000 customers.

Providing the services to these customers is done using 20 Isuzu trucks with the capacity equal to 2000 kg and 2 Nissan trucks with the capacity equal to 1000 kg. Kalleh Company has been unprofitable in selling their products in one of the lines during some frequent months. However, there is a better solution. This company believes that some of the customers are not profitable enough, considering the costs that they impose to the company for visitors, distributor, sending the car, and etc.

Therefore, the company decided to eliminate the customers whose purchase is less than a certain amount per each period (months). The weight or the cost of the purchase is just one aspect of this problem. Many items have not been considered in this decision. One of these items is the customer's collection period, since the money remaining in the customer's pocket for a long time maybe the reason of loss in the company.

**TABLE 9.** Comparing the results of SA and Gams

problem dimensions	Elapsed runtime (minute)		target function (Rial)		comparison of elapsed runtime and answer of two methods (%)	
	optimum answer	proposed method	optimum answer	proposed method	reduction in time solution	deviation from optimum answer
I.T.MN.V.K						
3*2*3*2*2	9	0.086	255668	255668	99.04	0
5*2*3*2*2	11.84	0.113	426112	426112	99.05	0
8*2*3*2*2	14.47	0.176	532641	532641	98.78	0
10*2*3*3*3	15.95	0.253	681780	659690	98.41	3.24
15*2*3*2*3	19.56	0.294	810106	790560	98.5	2.41
10*3*3*2*3	17.45	0.159	778080	759157	99.09	2.43
20*3*3*2*2	37.43	0.556	1166203	1117688	98.51	4.16
25*2*3*3*2	68.19	0.867	1287754	1224603	98.73	4.90
20*3*3*3*3	41.42	0.66	1093316	1006767	98.41	7.92
25*3*3*3*3	70.19	0.783	1341979	1241176	98.88	7.51
30*2*3*2*2	105.25	0.935	1430057	1332098	99.11	6.85
35*4*3*2*4	198.04	1.586	1716068	1655490	99.2	3.53
45*4*3*3*4	386.15	2.734	2574103	2433299	99.29	5.47
35*4*3*3*4	245.37	1.812	1767550	1660056	99.26	6.08
50*4*3*3*3	721.18	4.321	2651326	2535007	99.4	4.39
60*5*3*4*4	-	7.106	-	2797299	-	-
70*5*3*4*4	-	12.081	-	3636489	-	-
85*5*3*4*4	-	20.744	-	4363788	-	-
100*5*3*4*4	-	34.79	-	5454734	-	-
110*5*3*4*3	-	44.228	-	6272944	-	-
115*5*3*3*4	-	72.365	-	7715722	-	-
120*6*3*5*5	-	114.73	-	8718765	-	-
average	-	-	-	-	98.91	3.93

**TABLE 10.** Comparing the results of the proposed method and the current status in case study

	Pure profit (currency unit)	serving time (minute)	solution time (second)
proposed method	5854584	1072/344	2/061
existing condition	4404214	1320	-

During this period, the company not only loses the benefits from the circulation of the money, but also is obliged to borrow some money from the bank to cover its operating costs. Another issue is related to the inopportune discounts that are given to the customers only because of customer's insistence, regardless of various factors. If the discounts could be controlled, it would prevent a large number of additional costs. The next factor is concerned with the lack of inclusion of the

transportation and maintenance costs at this decision. Therefore, according to the needs of the company in proper selection of the economic customers, the proposed model was designed and applied in the company. This study is conducted on the data obtained from the purchases of the customers in the past 36 months. In this research, a crossroads, in the middle of the target area, was selected as the origin of the coordinates. Then, the characteristics of the customers and the depot were determined based on that origin. It is clear from the first planning period that how much product should be sold to which customers, in each period. In addition, it is determined that the vehicles should choose which routes to move toward the customers, taking into consideration their capacities.

The proposed method was programmed using MATLAB coding software. The registered program was implemented by a computer with the processor

specifications Corei3 cpu2.13 GH and a memory equal to 4GB RAM. The responses obtained from the proposed method have been compared with the existing data from the current method, and the results are represented in Table 10.

As the results reveal, applying the proposed model, in this company, resulted in 14% increase in the pure profit of selling. Besides, the availability of the specified optimized routes to move from the depot to the customers resulted in some reduction in the time spent for service provision.

## 8. CONCLUSION

In this study, it is attempted to propose a method to joint optimization of the planning of the distribution, marketing, and discounts of multi-products in multi-periods in the issue of vehicle routing. In order to simultaneous selection of the customers and vehicles routing, a mixed integer linear programming model was designed to minimize the transportation, maintenance, and discount costs and maximize the profits obtained from selling the products. To expand the proposed model, the discount given to each customer was taken into consideration based on the quantity of his purchase and the collection period. In addition, the type of the products that the consumers purchase and the marginal profit has been involved in the selection of the customers. For the exact solution of the model, Gams software is used, and for solving it in larger dimensions, the simulated annealing algorithm is used. The applicability of the proposed method is examined in a case study and several problems with different dimensions. The application of this method at Kalleh Company, in Shiraz, caused 14 percent increase in the profit and no delay in the process of service provision by proper selection of the economic customers and the optimum routes. Comparing the answers provided by SA algorithm, with the optimum solutions, 3.93 percent deviation, in average, was observed. However, the time needed for coming to the intended results, in this way, reduced at least 98% compared to the ones obtained using Gams software. Further research can be done (improving this method) considering the limitations in time spans for sending and receiving the goods, the costs of shortcomings in the target function, and multi-depot instead of one depot. This model can be improved entering the fuzzy or probable parameters in the model.

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## Integration of Multi-period Vehicle Routing Problem and Economic Selection of Customers with the Objective of Optimizing Distribution, Sales and Discounts Planning

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تصمیم گیری در مورد انتخاب اقتصادی مشتریان نقش قابل توجهی در فروش و مدیریت لجستیک شرکت ها دارد. همچنین، یکی دیگر از موضوعات تاثیرگذار در روابط میان تامین کنندگان و مشتریان، توزیع صحیح و به موقع محصولات و ترکیب بهینه از مسیرهای توزیع جهت کاهش هزینه های حمل و نقل است. در این مقاله به مسئله یکپارچه سازی چند دوره ای، چند محصولی مسیریابی و انتخاب اقتصادی مشتریان با هدف حداقل نمودن هزینه های حمل و نقل، هزینه های نگهداری موجودی در انبار، هزینه های تخفیف و حداکثر نمودن سود حاصل از فروش محصولات، پرداخته شده است. علاوه بر حجم خرید مشتریان، مدت زمان پرداخت مشتریان در میزان ارائه تخفیف به آنها موثر است. مشتریان اقتصادی با توجه به سه عامل تخفیف قیمت کالا، حاشیه سود محصولات درخواستی و فاصله از انبار تامین کننده انتخاب می شوند. برای حل دقیق مدل از نرم افزار گمز و برای حل در ابعاد بزرگتر از الگوریتم شبیه سازی تبرید استفاده شده است. کارایی مدل پیشنهادی با مقایسه جواب های بهینه با دقت بالای ۹۸/۹۱ درصد می باشد. همچنین در مطالعه موردی شرکت کاله شیراز، نتایج حاصل، کاهش ۱۴ درصدی در هزینه های این شرکت را نشان می دهد.

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