



## A New Empirical Model to Increase the Accuracy of Software Cost Estimation

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### ABSTRACT

We can say a software project is successful when it is delivered on time, within the budget and maintaining the required quality. However, nowadays software cost estimation is a critical issue for the advance software industry. As the modern software's behaves dynamically so estimation of the effort and cost is significantly difficult. Since last 30 years, more than 20 models are already developed to estimate the effort and cost for the betterment of software industry. Nevertheless, these algorithms cannot satisfy the modern software industry due to the dynamic behavior of the software for all kind of environments. On this study, an empirical interpolation model is developed to estimate the effort of the software projects. This model compares with the COCOMO based equations and predicts its result analyzing individually taking different cost factors. The equation consists one independent variable (KLOC) and two constants a, b which are chosen empirically taking different NASA projects historical data and the results viewed in this model are compared with COCOMO model with different values of scale factor. In this paper the author analyze more than 250 projects collected from PROMISE repository. The effort variance is very low and the proposed model has the lowest Mean Magnitude of Relative Error (MMRE) and RMSSE.

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## 1. INTRODUCTION

This paper focused to satisfy the need of today's software industry by estimating the cost and effort and challenging the various issues and variations occurred in software size. Accuracy and timely estimation of software efforts is one of the most critical activities to manage a software project [1, 2]. As both over estimate and under estimate of software is very harmful for modern software industry, this paper gives emphasis to predict the effort accurately and reliably. If the estimation is low then the software development team will be under pressure to finish the product and if the estimation is high then the most of the resources will be commuted to the projects [3, 4]. It is very critical to implement novel methods to improve the accuracy of a software projects. So now a days, many models are used to estimate the efforts. This model proposed an extensive COCOMO [5-7] model by changing the scale factors and constant values a, b to measure the software

effort. This paper structured as follows: Section 2 describes the overview of existing techniques, Section 3 describes a frame work to estimate the efforts as comparing with COCOMO model, and Section 4 relates the conclusion and future work.

## 2. OVERVIEW OF VARIOUS MODELS USED FOR SOFTWARE ESTIMATION

Since 1990 more than 20 different models are used to estimate the cost, effort, duration and productivity of the software [5, 8]. Standard models which are used to estimate the software efforts and costs are:

1. COCOMO
2. Halstead
3. Walston-Felix
4. Bailey-Basil
5. Doty (for KLOC >9)
6. SEL

### 2. 1. COCOMO Basic Model

This model was proposed by Boehm [9] and divided by three sub

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models i.e. Basic, Intermediate and detailed model [10,11] For different type of software’s basic model describes as follows (Table 1).

**2. 2. COCOMO Intermediate Model**

$$\text{Organic Effort (E)} = 3.2 \times (\text{KLOC})^{1.05} \times \text{EAF} \quad (1)$$

$$\text{Semi Detached Effort (E)} = 3.0 \times (\text{KLOC})^{1.12} \times \text{EAF} \quad (2)$$

$$\text{Embedded Effort (E)} = 2.8 \times (\text{KLOC})^{1.2} \times \text{EAF} \quad (3)$$

**2. 3. COCOMO II Model** This model formulate like:

$$\text{Effort (E)} = 2.9 \times (\text{KLOC})^{1.1} \quad (4)$$

**2. 4. SEL Model** Software engineering laboratory developed a model to estimate the software effort defined as follows.

$$\text{Effort(E)} = 1.4 \times (\text{KLOC})^{0.93} \quad (5)$$

$$\text{Duration (D)} = 4.6 \times (\text{KLOC})^{0.26} \quad (6)$$

**2. 5. Walston-Felix Model** Walston and felix developed a model to estimate the efforts taking 60 IBM projects and analyzing relationship between derived lines of codes, constitutes participation, customer oriented changes and new lines of code [11].

$$\text{Effort (E)} = 5.2 \times \text{KLOC}^{0.91} \quad (7)$$

$$\text{Duration (D)} = 4.1 \times \text{KLOC}^{0.36} \quad (8)$$

**2. 6. Bailey-Basil Model** Bailey and Basil formulate a relation to estimate the efforts [12].

$$\text{Effort (E)} = 5.5 \times \text{KLOC}^{1.16} \quad (9)$$

**2. 7. Halstead Models** Halstead formulate a relation to estimate as [13]:

$$\text{Effort (E)} = 0.7 \times (\text{KLOC})^{1.5} \quad (10)$$

**2. 8. Doty Model (KLOC>9)**

$$\text{Effort (E)} = 5.288 \times (\text{KLOC})^{1.047} \quad (11)$$

**3. PROPOSED MODEL AND METHODOLOGY**

Till now, none of the existing models can measure software efforts accurately in the modern software industry for all kind of software’s. In this paper, we analyze a new empirical model for effort estimation. The cost drivers vary from project to project, so we take different scale factor values and categories the cost drivers into project, product, personal and computer.

**3. 1. Data Collection** For this paper, data are collected from 60 NASA projects from different containers, 93 NASA projects from common NASA2 and 63 NASA projects from promise repository. These data sets are real project data sets and may be used for practical proposes and can be viewed from “The Promise Repository of Empirical Software Engineering Data”. <http://openscience.us/repo>. North Carolina State University, Department of Computer Science.

**3. 2. Description About Proposed Model** This model is based on empirical analysis of 216 NASA Projects of different repository and it includes the scale factors like personnel, complexity, environment, risks and constraints. It predicts effort, cost estimates and reliability using the statistical approaches like  $y = a \times (\text{KLOC})^b + d$  to evaluate the cost, effort and duration empirically analyzing 216 real projects data of NASA. In this model, we use a regression formula, with the parameters ‘a’ and ‘b’ which are derived from project dataset using deterministic and heuristic methods and optimizing the global solution. By the regression analysis, we express the relationship between two variables and to estimate the dependent variable (i.e. Effort) based on independent variable (i.e. LOC) using simulated annealing algorithm [14].

Simulated annealing algorithm might have been used to solve a wide range of optimization problems in artificial intelligence and other areas. In this study, we have used it as a simple way to implement the algorithm to derive the parameters a and b considering randomly chosen values. However, it would be inappropriate to solve a complex problem to illustrate how to use simulated annealing [15]. Thus, two variable function of Equation 12 will be used for instructive purposes. There may have other optimization methods, which are more appropriate to solve this second order equation, but this section is only trying to set the basics for proper use of simulated annealing [14, 16].

**TABLE 1.** Basic COCOMO Effort and Duration

Mode	Effort	Duration
Organic	$E = 2.4 * \text{KLOC}^{1.05}$	$D = 2.5 * (\text{PM})^{0.38}$
Semi Detached	$E = 2.4 * \text{KLOC}^{1.12}$	$D = 2.5 * (\text{PM})^{0.35}$
Embedded	$E = 2.4 * \text{KLOC}^{1.2}$	$D = 2.5 * (\text{PM})^{0.32}$

$$F(x, y) = x^2 + y^2 + 5xy - 4 \tag{12}$$

To get a better sense of the behavior of Equation (12), Figure 1 shows a plot of this equation.

Let suppose that the goal is to find the values of x and y that minimize f(x, y). Clearly, the solution is any point (x, y) that lies on the circle that intersects f(x, y) with the plane z = 0. We normally use simulated annealing when the solution has many variables, and finding or visualizing the solutions in these cases is much more difficult than interpreting the 3-D plot of Figure 1 [14, 16, 17].

### 3. 3. Proposed Algorithm Description

1. Start
2. Read the project KLOC and actual effort as E
3. Follow the equation  $E = n \times a \times (\text{KLOC})^b$  where a, b are constants and n is the no. of projects.
4.  $\sum \log(\text{KLOC}) + \sum \log E = nA + B \sum \log(\text{KLOC})$
5.  $\sum \log(\text{KLOC}) \times \sum \log E = A \sum \log(\text{KLOC}) + B (\sum (\text{Log}(\text{KLOC})))^2$  Where  $A = \log(a)$  and  $B = b+1$ .
6. Use the steps 4 and 5 to estimate the parameter Value of a and b by the method of statistical techniques using the data of real projects empirically
7. End.

**3. 4. Evolution of Proposed Algorithm** Here, the authors make a convenient way to estimate the effort and the new cost driver values are taken empirically as shown in Table 3. The proposed approach provides more accurate estimation with the comparison of COCOMO model. Researchers may redefine the value of cost drivers further for better result. Individually analyzing organic, semi detached and embedded projects empirically we got the parameter value a, b as shown in Table 2.

The formula used to calculate the effort is:

$$\text{Effort (E)} = a \times (\text{KLOC})^b \times \prod_{i=1}^{15} \text{NEAF} + \left( \prod_{i=1}^{15} \text{NEAF} + \prod_{i=1}^{15} \text{CEAF} \right) \tag{13}$$

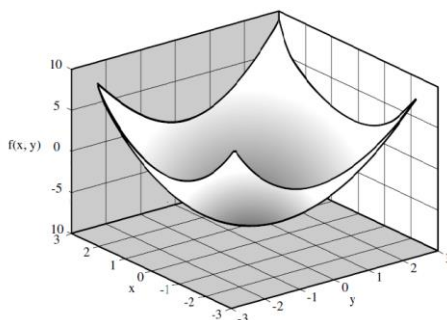


Figure 1. Example of a simulation

TABLE 2. (Predicted parameters for proposed model)

Type	A	B	a	B
Organic	0.3560	2.03	2.27	1.03
Semi-Detached	0.4623	2.14	2.9	1.14
Embedded	0.4471	2.20	2.8	1.2

where, NEAF is the new effort adjustment factors, which are new cost drivers calculated by the author in this paper empirically. CEAF are the COCOMO cost drivers, which are the COCOMO effort adjustment factors.

Effort Variance = (actual value – estimated value)/actual value.

The two main activities to calculate the effort and duration to estimate the cost of the software .This estimated effort will be converted to a dollar cost by calculating an average salary per unit time of the staff involved and multiplying this by the estimated effort required. Thus, cost of project is \$ (Effort \* Monthly Wages) \* Total months. Table 3 describes the new effort multipliers calculated by the author to estimate the effort. Practically, it is found that the today’s software is very complex. That is why it is need of change in the cost driver value for better result and for further research the value of cost drivers may be changed for better performance.

**3. 5. Performance of the Proposed Model** Table 4 Shows the result of effort estimation by the proposed model as comparison to COCOMO model and Table 5 shows the effort variance of different model in accordance with the data of 15 given projects and measure the performance to validate the outcome. The Performance Graph COCOMO Vs Proposed Model is shown in Figure 2, the graph of proposed model effort vs. Actual effort is shown in Figure 3 and Effort Estimation Graph of different models is shown in Figure 4.

### 3. 6. Evaluation Criteria and Error Analysis

There are so many statistical approaches which are used to estimate the accuracy of the software effort. We are using methods like MRE, MMRE, RMSE, and Prediction [18]. Boehm [9] suggested a formula to find out the error percentage as shown below:

$$\text{Error\%} = \frac{\text{Predicted\_Effort} - \text{Actual\_Effort}}{\text{Actual\_Effort}} \tag{14}$$

MRE (Magnitude of relative error): We can calculate the degree of estimation error for individual project.

$$\text{MRE} = \frac{|\text{Actual\_Effort} - \text{Predicted\_Effort}|}{\text{Actual\_Effort}} \tag{15}$$

RMSE (Root Mean Square Error): we can calculate it as the square root of the mean square error and can be defined as:

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (Actual\_Effort - Predicted\_Effort)^2} \tag{16}$$

**TABLE 3.** New effort adjustment factors assigned by the proposed approach

Sl No	Cost Driver	Very Low	Low	Nominal	High	Very High	Extra High
1	Required Reliability	0.75	0.97	1	1.15	1.18	2
2	DB Size	0.86	0.96	1	1.01	1.18	1.9
3	Product complexity	0.7	0.99	1	1.19	1.2	1.23
4	Time constraint	0.78	0.85	1	1.35	1.38	1.86
5	Main Memory constraint	0.7	0.85	1	1.01	1.22	1.76
6	Machine volatility	0.8	0.93	1	1.01	1.3	1.55
7	Turnaround Time	0.8	0.93	1	1.09	1.34	-
8	Analyst Capability	1.46	1.19	1	0.86	0.78	-
9	Application experience	1.29	1.23	1	0.95	0.94	-
10	Programmer capability	1.42	1.17	1	0.96	0.95	-
11	Virtual Machine	1.34	1.01	1	0.82	-	-
12	Language experience	1.02	0.98	1	0.92	-	-
13	Modern programming practice	1.24	1.14	1	0.94	0.81	-
14	Use of software tools	1.19	1.14	1	0.93	0.82	-
15	Schedule constraint	1.23	1.03	1	1.08	1.1	-

**TABLE 4.** Effort Estimation by different Models

P no	KLOC	Actual Effort	CCOMO Basic	COCOMO Inter	Proposed	25	32.6	170	144.02	144.02	175.8
1	25.9	117.6	100.86	100.86	121.78	26	35.5	192	158.44	158.44	193.61
2	24.6	117.6	95.21	95.21	114.94	27	5.5	18	17.78	17.78	22.38
3	7.7	31.2	25.92	25.92	31.96	28	10.4	50	36.3	36.3	44.25
4	8.2	36	27.81	27.81	34.20	29	14	60	50.64	50.64	61.34
5	9.7	25.2	33.57	33.57	41.02	30	6.5	42	32.28	32.28	36.21
6	2.2	8.4	6.37	6.37	9.10	31	13	60	61.01	61.01	66.54
7	3.5	10.8	10.72	10.72	13.98	32	90	444	360	360	451.8
8	66.6	352.8	290.5	290.5	349.55	33	8	42	35.42	35.42	39.27
9	7.5	72	40.9	40.9	68.71	34	16	114	85.45	85.45	112.77
10	20	72	32.98	32.98	62.66	35	177.9	1248	1152	1152	1346.46
11	6	24	10.52	10.52	16.95	36	302	2400	1641.5	1641.5	2378.9
12	100	360	200	200	386.8	37	282.1	1368	1139.4	1139.4	1301.3
13	11.3	36	27.9	27.9	36.49	38	79	400	279.8	279.8	357.51
14	15	48	29.35	29.35	46	39	423	2400	1143.68	1143.68	2406.2
15	19.7	60	72.24	72.24	89.65	40	47.5	252	194.24	194.24	218.66
16	29.5	120	116.6	116.6	140.9	41	11.4	98.8	63.66	63.66	88.32
17	15	90	62.21	62.21	92.39	42	19.3	155	114.8	114.8	158.32
18	38	210	182.5	182.5	231.12	43	101	750	602.67	602.67	700.61
19	50	370	288.6	288.6	421.5	44	219	2120	1509.48	1509.48	2258.2
20	10	48	30.95	30.95	38.2	45	0.9	8.4	2.34	2.34	4.49
21	15.4	70	62.17	62.17	76	46	70	458	606.44	471.6	438.75
22	48.5	239	224.7	224.7	273.3	47	60	409	497.9	387	485.7
23	16.3	82	66.26	66.26	80.96	48	32	1350	1557.5	1211	1145.25
24	12.8	62	50.54	50.54	61.96	49	41	599	358	278.47	608.5
						50	24	430	188.29	146.45	321.84

**TABLE 5.** Effort variance (%) by different Models (Data of 15 projects out of 93 NASA data)

KLOC	Actual Effort	COCOMO Basic %	COCOMO Inter%	Proposed%
25.9	117.6	14.23	14.23	3.55
24.6	117.6	19.03	19.03	2.26
7.7	31.2	16.9	16.9	2.43
8.2	36	2.27	2.27	5
2.2	8.4	24.16	24.16	8.3
66.6	352.8	17.65	17.65	0.92
11.3	36	22.5	22.5	1.36
15	48	38.5	38.5	4.1
15	90	30.8	30.8	2.65
16.3	82	19.19	19.19	1.2
14	60	15.76	15.76	2.2
16	114	25.04	25.04	1.07
423	2400	52.34	52.34	0.2583
19.3	155	25.9	25.9	2.14
41	599	40.23	53.51	1.58

MMRE (Mean Magnitude of Relative Error): It is another way to measure the performance and it calculates the percentage of absolute values of relative errors. It is defined as:

$$MMRE = \frac{1}{n} \sum_{i=1}^n \frac{|Predicted\_effort - Actual\_Effort|}{Actual\_Effort} \quad (17)$$

PRED (N): This criteria is used to calculate the average percentage of estimates that were within N% of the actual values i.e. the percentage of predictions that fall within p % of the actual, denoted as PRED (p). Where k is the number of projects in which MRE is less than or equal to p, and n is the total number of projects. It is defined as PRED (p) = k / n.

For project 1 having KLOC =25.9, the actual effort is 117.6 Man-Month and calculated effort for Basic COCOMO and Intermediate COCOMO is 100.86 MM and by the proposed model is 121.78 MM. Similarly, for project 2 KLOC=24.6, the actual effort is 117.6 MM and calculated effort for Basic COCOMO and Intermediate COCOMO is 95.21 MM and by the proposed model is 114.94 MM. Now, we can calculate the % of error using the Equation (5). For project 1, the error % for Basic COCOMO and Intermediate COCOMO is (-14.23) % and error % for proposed model is (+3.55) %. Similarly, For project 2, the error % for Basic COCOMO and Intermediate COCOMO is (-19.03) % and error % for proposed model is (-2.26) %. Here, the negative % indicates the under estimation of

the project and positive % error indicates the project is over estimate. Big under estimate gives extra pressure to the developing staff and leads to add more staffs which causes the late to finish the project. According to Parkinson’s Law of “Work expands to fill the time available for its completion”, Big over estimation reduces the productivity of personnel [19]. So, during the estimation, researchers should have to give emphasis to reduce the big over or under estimation of the project.

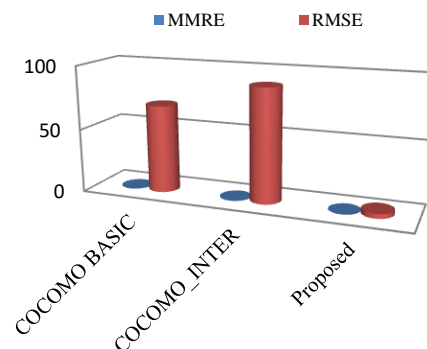
**3. 7. Comparison with COCOMO Models** In software estimation, COCOMO model is a regular and standard model to estimate the effort developed by Barry Boehm. However, in the proposed model the researcher used a basic regression formula, with parameters which are derived from historical project (NASA software). Here, we are estimating the effort based on the actual project characteristic data and better result predicts as compare to MMRE and RMSE as shown in the graph. Considering the data, the researcher changed the cost driver value and the parameters [20].

**3. 8. Advantages of Proposed Model**

- ✓ It Is reusable
- ✓ It calculates software development effort as a function of program size expressed in Kilo Lines of code (KLOC)
- ✓ It predicts the estimated effort with more accuracy.

**TABLE 6.** Performance of Different Models

Performance	COCOMO Basic	COCOMO Inter	Proposed
MMRE	0.2436	0.25185	0.0249
RMSE	69.07	89.22	3.586
PRED (12%)	0.16	0.25	0.69



**Figure 2.** Performance Graph COCOMO Vs Proposed Model

#### 4. CONCLUSION AND FUTURE WORK

This proposed model can be useful to estimate the software effort with better accuracy which is very important when software pays a lot in every industry. In this paper, the author analyzes more than 250 projects collected from PROMISE repository. The predicted result shows there is very close values between actual and estimated effort. The effort variance is very less and the proposed model has the lowest MMRE and RMSSE and prediction values of 0.0249 and 3.586 and 0.69, respectively. So, the proposed model may able to provide good estimation capabilities for today's software industry

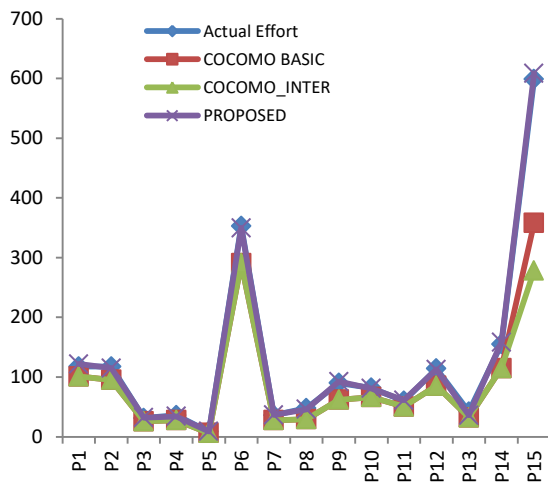


Figure 3. Proposed effort vs. Actual effort

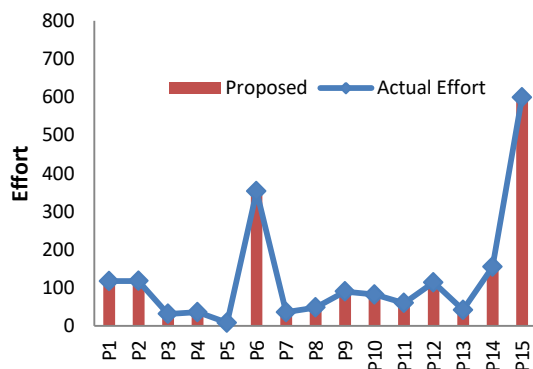


Figure 4. Effort Estimation Graph of different models

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Mean Magnitude of Relative Error

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ما می توانیم بگوییم یک پروژه نرم افزاری زمانی موفق است که آن به موقع، در حدود بودجه و با حفظ کیفیت مورد نیاز تحویل داده شود. با این حال، امروزه برآورد هزینه نرم افزار یک مسئله مهم برای صنعت نرم افزار پیشرفته است. همانطور که نرم افزار مدرن به طور پویا رفتار می کند، بنابراین برآورد هزینه ها و تلاش بسیار مشکل است. از ۳۰ سال گذشته، بیش از ۲۰ مدل برای ارزیابی تلاش و هزینه برای بهبود صنعت نرم افزار توسعه یافته است. با این وجود، این الگوریتم ها نمی توانند صنعت نرم افزار مدرن را با توجه به رفتار دینامیکی نرم افزار برای همه نوع محیط برآورده سازند. در این مطالعه، یک مدل درون یابی تجربی برای برآورد تلاش پروژه های نرم افزاری به وجود آمده است. این مدل با معادلات مبتنی بر COCOMO مقایسه می شود و نتیجه آن را با تجزیه و تحلیل جداگانه با در نظر گرفتن عوامل مختلف هزینه پیش بینی می کند. معادله، شامل یک متغیر مستقل (KLOC) و دو ثابت  $a$  و  $b$  است که به طور تجربی از داده های قبلی پروژه های مختلف ناسا انتخاب شده و نتایج مشاهده شده در این مدل با مدل COCOMO با مقادیر مختلف فاکتور مقیاس مقایسه می شود. در این مقاله، نویسنده بیش از ۲۵۰ پروژه را که از مخزن PROMISE جمع آوری شده، تحلیل می کند. واریانس تلاش بسیار کم است و مدل پیشنهادی دارای کمترین میانگین خطای نسبی (MMRE) و RMSSE است.

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