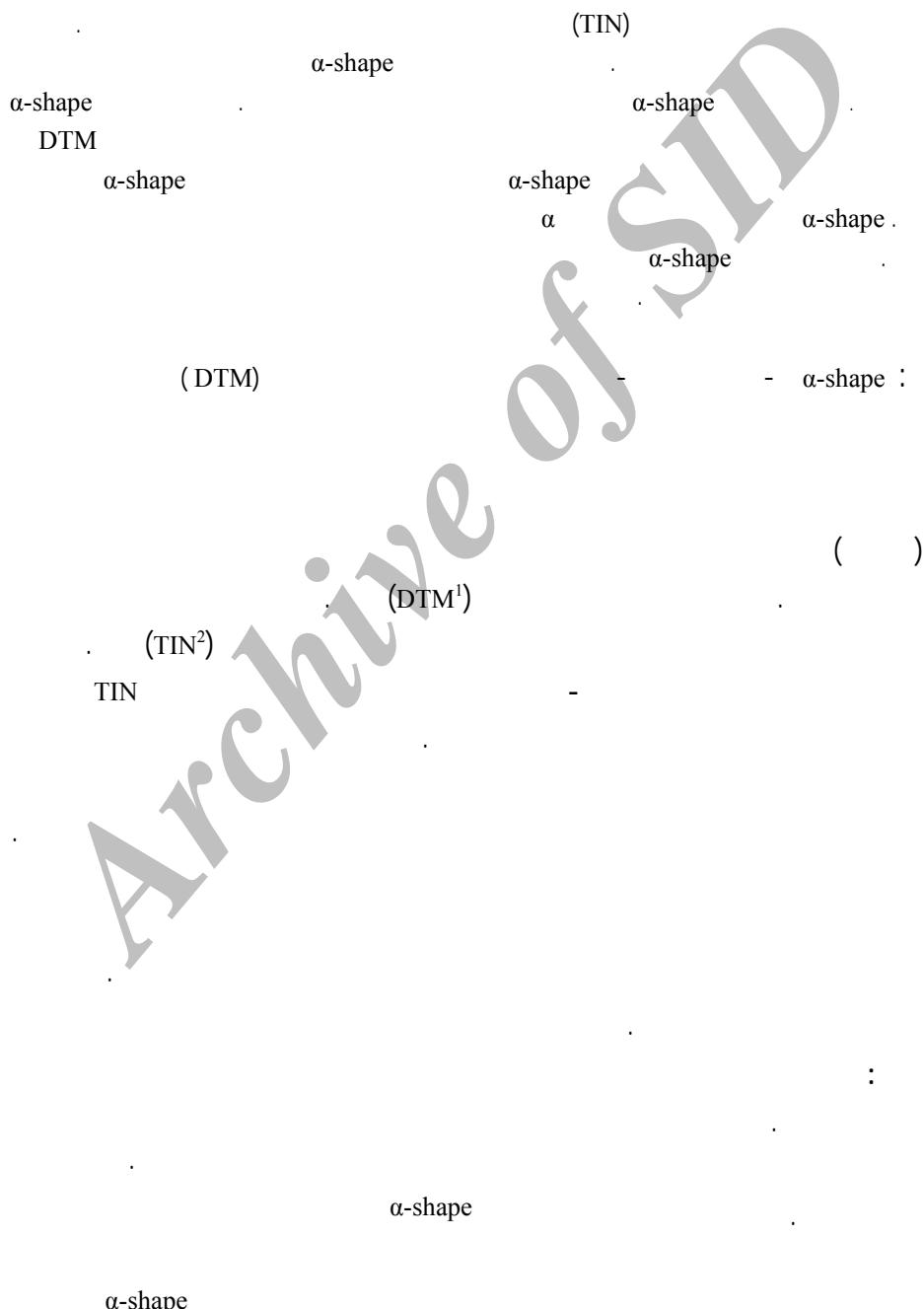
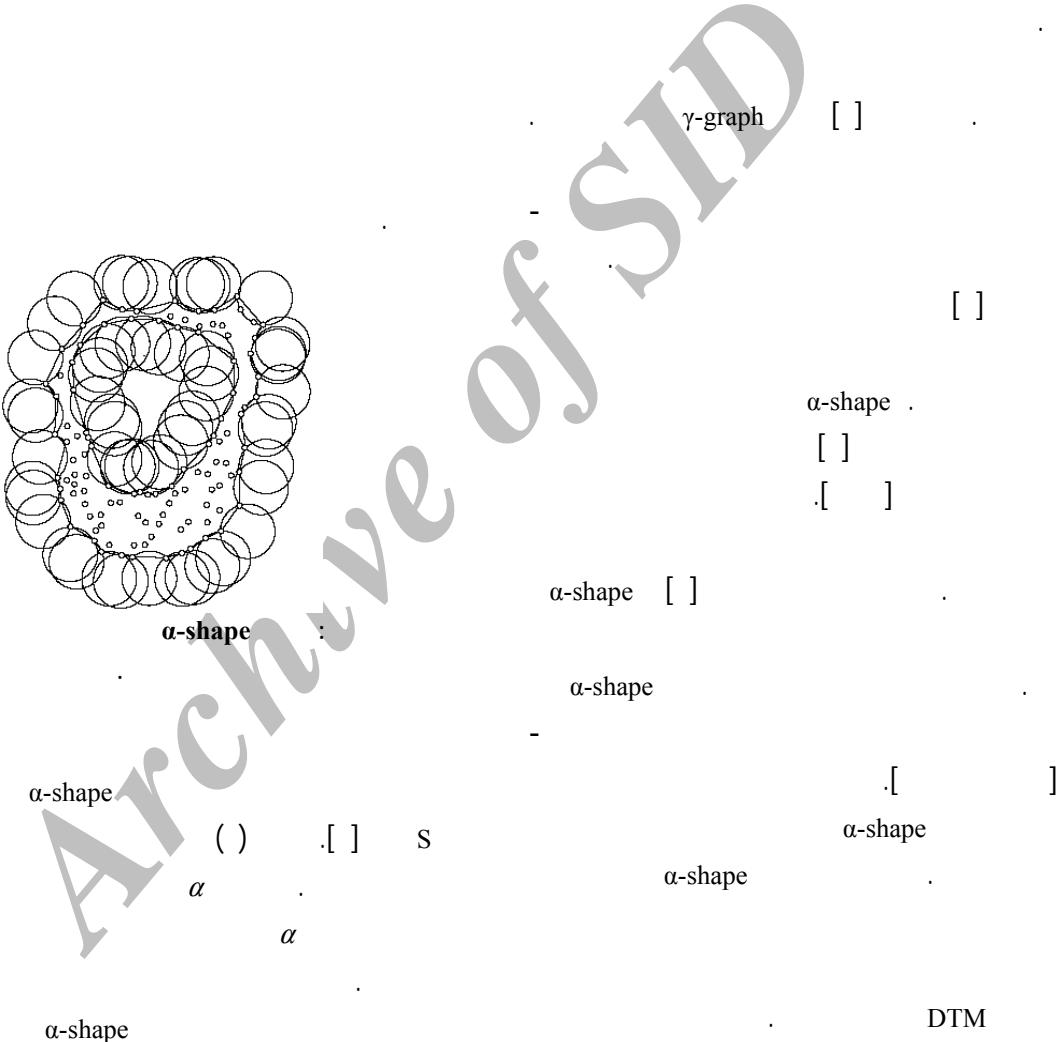


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## **$\alpha$ -shape**

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alpha-shape

alpha-shape

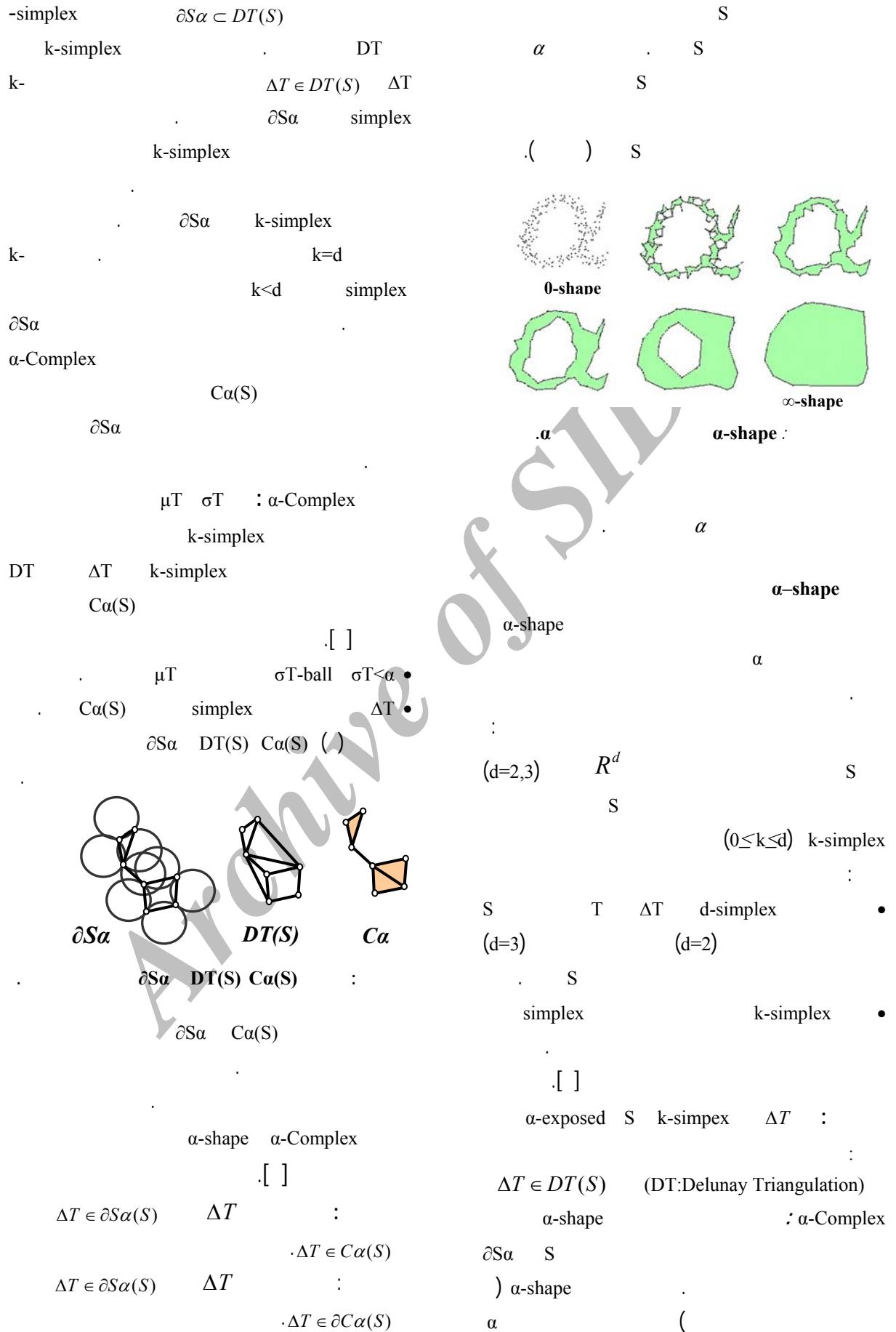
DTM

alpha-shape

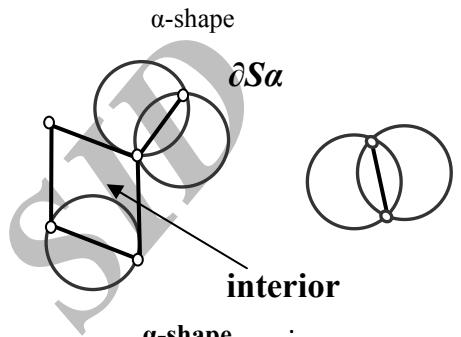
DTM

alpha-shape

			.....	
·	$b \cap S = \phi$			
$\alpha$ -exposed	k-simplex	$\therefore \alpha$ -exposed		
b	$\lambda$ -ball			
k-simplex	S	b		
	b	[ ]		
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$\alpha$ -		1-simplex	K+1	: k-simplex
		exposed	K	k-simplex K
o	o	.	( )	( )
o	o	.	.	
o	o	.	.	
o	o	.	.	
a-exposed	not $\alpha$ -exposed	.	.	
$\alpha$ -exposed	1-simplex	:	.	
$\alpha$ -	$R^d$	S	:	
$0 \leq k < d$	S	k-simplex	shape	
S	.	$\alpha$ -exposed	k-simplex	
		$\partial Sa$		
		[ ]		
$\partial Sa = \{\Delta T \mid T \in S,  T  \leq d \text{ and } \Delta T \text{ } \alpha\text{-exposed}\}$		( )		
.		$\partial Sa$		
		.	.	
simplex	(a)	simplex	.	
(b)	.	.	.	
simplex	;	;	.	
α-shape	;	;	.	
	$\alpha$		.	
	$\alpha$		.	
		$0 < \lambda < \infty$	$\lambda$	
		∞-ball	0-ball	
		b	$\lambda$ -ball	
		.	.	
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		.	.	
R <sup>d</sup>	S	:	.	
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.	S	;	S	
.	S	;	.	R <sup>3</sup>
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k-simplex	;	;	.	
$\Delta T$	T		.	
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				$\alpha$ -shape
		[ ]	$\Delta T \in \partial C\alpha(S)$	$\Delta T$
				: $\Delta T \in \partial S\alpha(S)$
	<b><math>\alpha</math>-shape</b>		$\cdot \partial C\alpha(S) \in \partial S\alpha(S)$	:
				$\alpha$ -shape $\alpha$ -Complex
$\alpha$ -				: $\alpha$ -shape
		shape		
DT	$\Delta T$	simplex	$\cdot : C\alpha$	$\alpha$ -shape
$\mu T$		$\sigma T$ -ball		( )
		$\Delta T$	$\sigma T < \alpha$	$\alpha$ -
$\alpha$ -test		)	$C\alpha$	shape
d-		$\cdot : C\alpha$	( .	
		$S\alpha$	$C\alpha$	$\alpha$ -shape
		simplex	$S\alpha$	$\alpha$ -
			( .	
$\sigma T$ -	$\alpha$ -test	( .		
P			ball	
( .		T	S	$\alpha$ -shape      k-simplex
simplex				
		$\Delta T$	$C\alpha$	$\Delta T \quad \Delta T \in \partial C\alpha(S) \quad :$
simplex				$\alpha$ -shape $\Delta T$ $\alpha$ -shape
		$\Delta T$	:	( )
$C\alpha(S)$	simplex	$\Delta T$	$\Delta T \in \partial Conv(S)$	
$C\alpha(S)$				
		$\Delta T$	:	
$\Delta T$		$DT(S)$	simplex	
			$C\alpha(S)$	
		$\Delta T$	k-simplex	$\alpha$
				$\alpha$ -Complex $\alpha$
$C\alpha(S)$	$C\alpha(S)$	simplex		
		$C\alpha(S)$		
		:		
$\Delta T$ is	$\left\{ \begin{array}{ll} \text{not in } C\alpha & (\text{for } \alpha < a) \\ \text{in } \partial C\alpha & (\text{for } \alpha \in (a, b)) \\ \text{interior to } C\alpha & (\text{for } \alpha \in (b, \infty)) \end{array} \right.$	$\cdot S\alpha_1(S) \subset S\alpha_2(S)$	$C\alpha_1(S) \subset C\alpha_2(S)$	$\alpha_1 \leq \alpha_2 \quad :$
				$\alpha$ -shape $C\alpha(S)$

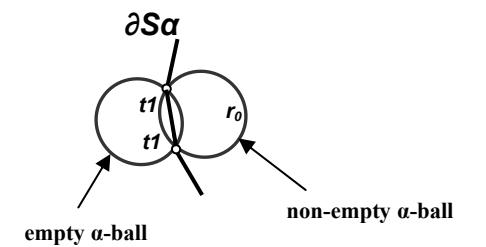


$\alpha$ -shape      k-simplex

$\Delta T \quad \Delta T \in \partial C\alpha(S) \quad :$

$\alpha$ -shape       $\Delta T$        $\alpha$ -shape

$\Delta T \quad \alpha$ -ball



$\alpha$

$\alpha$ -Complex       $\alpha$

$\alpha_1 \leq \alpha_2 \quad :$

$\cdot S\alpha_1(S) \subset S\alpha_2(S) \quad C\alpha_1(S) \subset C\alpha_2(S)$

$\alpha$ -shape       $C\alpha(S)$

$\alpha$	$\alpha$	$\alpha$	$\alpha \in I = [a, \infty]$	$\Delta T \in S\alpha$
$\alpha$	$($	$)$		simplex
			$\alpha$ -shape	
$\alpha$	$\alpha$ -shape			
$\alpha$	$\vdots$		b a	simplex
			d-simplex	b a
			a-	d-simplex
			d-	$\cdot ($ $\alpha$ -test $)$
			$a=b=\sigma T$	Complex
			$C\alpha$	
			d-simplex	
			k-simplex	b a
			b a	
				$k < d$
				(k+1)-simplex
			(k+1)-simplex	$\Delta T$
			$\Delta T$	k-simplex
			$\Delta T$	$\Delta V$ $\Delta U$
			$\Delta T$	$\Delta T$
			$\Delta T$	
$\alpha$ -shape	$\alpha$ -shape	$\alpha$ -shape	$\alpha$ -shape	
$\alpha$ -shape	$\alpha$ -shape	$\alpha$ -shape	$\alpha$ -shape	
$\alpha$	$[ ]$	$\alpha$ -shape(	$\alpha$ -shape(	
			DT(S)	k-simplex
			$\Delta T$	
			(k+1)-	Bu
				$k < d$
			DT(S)	$\Delta U$
				simplex
				$\Delta U \in C\alpha$
			$a = \min \{au \mid Bu = (au, bu), \Delta U \text{ (k+1)-Simplex } T \subset U\}$	
			$\alpha \in (a, \infty)$	$\Delta T \in C\alpha$
			C $\alpha$	k-simplex
			$\Delta T$	
			(k+1)-	Bu
				$k < d$
			DT(S)	$\Delta U$
				simplex
				$\Delta U \in C\alpha$
			$b = \max \{au \mid Bu = (au, bu), \Delta U \text{ (k+1)-Simplex } , T \subset U\}$	
			$\alpha \in (b, \infty)$	$\Delta T \in \partial C\alpha$
			$\alpha$ -shape	
$\alpha$ -shape		$\alpha$ -test		
$[ ]$				
		$( )$		
$\alpha$ -shape	$( - )$	$[ ]$		
				$\alpha$ -shape

$\alpha$ -shape

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$\alpha$ -shape

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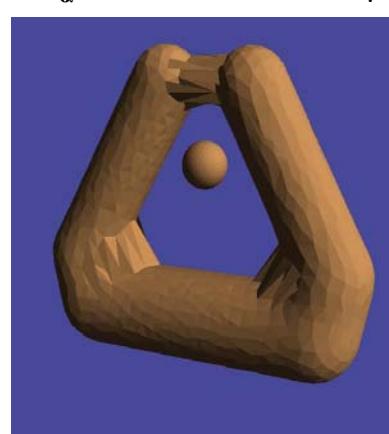
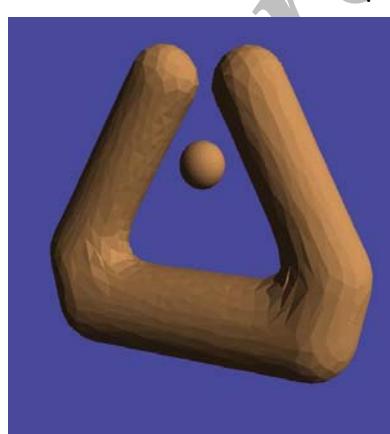
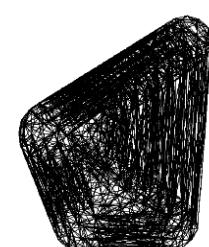
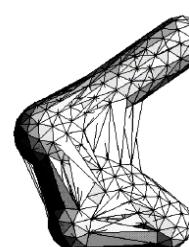
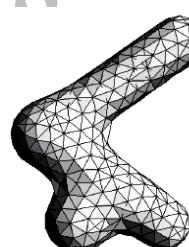
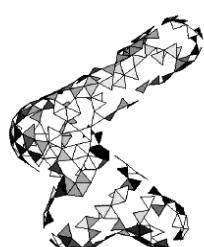
$\alpha$ -ball

shape

DTM

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$\alpha$ -shape



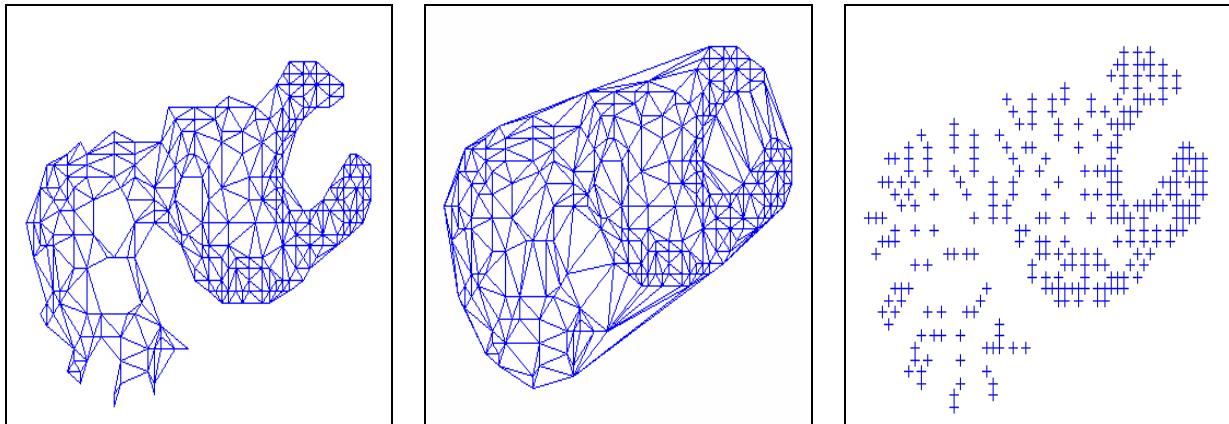
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$\alpha$ -shape

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$\alpha = /$

**$\alpha$ -shape**

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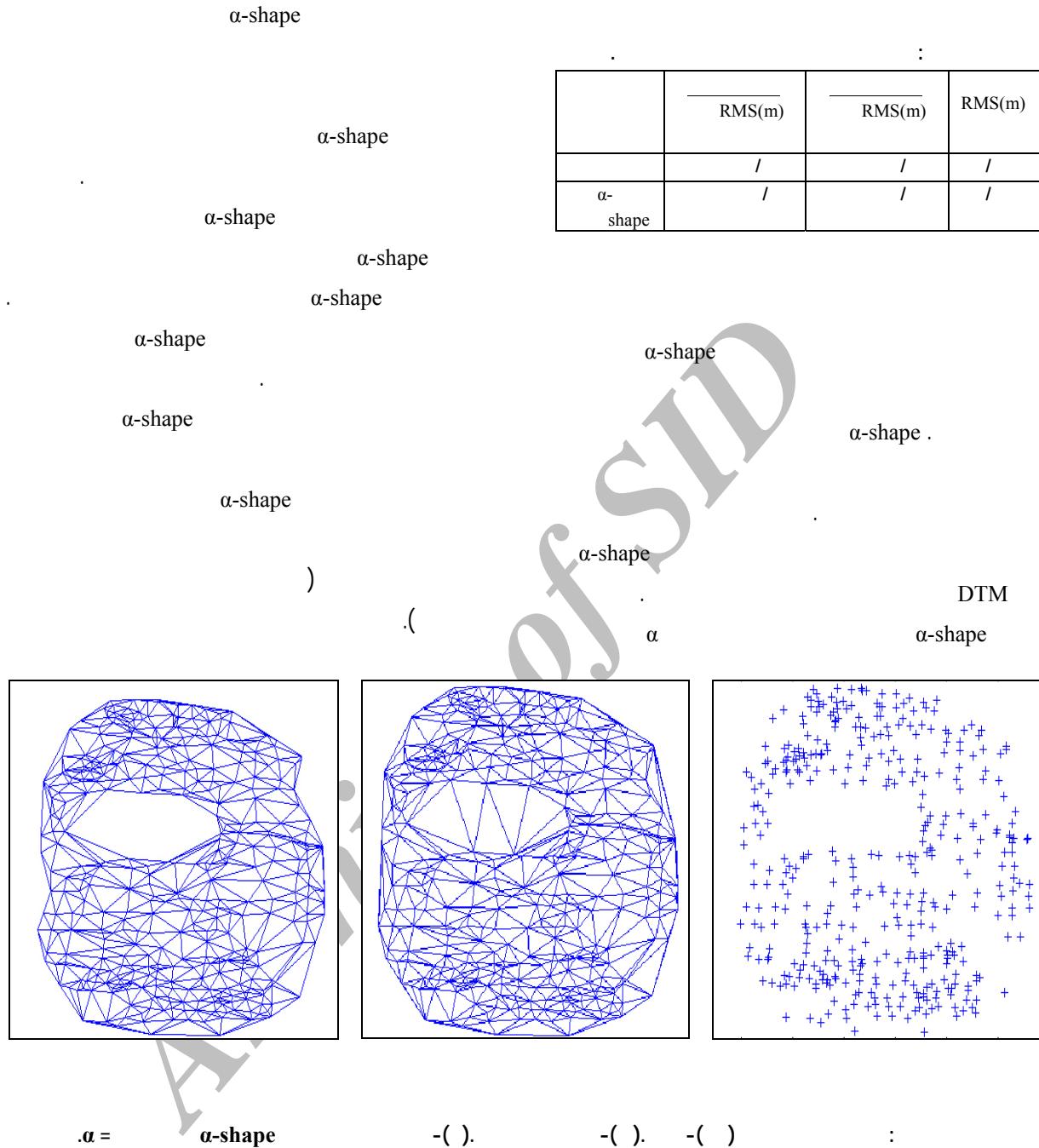
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$\alpha$ -shape

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- 1 - DTM =Digital Terrain Model  
2 - TIN = Triangles Irregular Networks  
3 - ex-Hull  
4 - Boissennat  
5 - Veltkamp  
6 - Hoppe  
7 - Zero-Contour  
8 - Edelsbrunner  
9 - Bernardini  
10 - Convexity  
11 - Concave  
12 - General Position  
13 - Boundary  
14 - Tiechmann  
15 - Capps