

Mathematical Model of Dam Reservoir Sediment Flushing by Low Level Outlet

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Abstract

Sediment accumulation in reservoirs of storage dams and methods of sediment removal are significant for reservoir operation planning and increase of the dam useful life. Flushing of sediments in reservoirs is considered as one of the most important methods of sediment removal because the energy of the water flow is utilized to remove accumulated deposits. In this paper a one-dimensional mathematical model has been developed to simulate the process of sediment flushing. The model is able to predict reservoir bed profile variation during the process of flushing. The developed differential equation has been solved by the finite difference method using the control volume approach. The calibration of the model has been done by using results obtained by other researchers and then it was validated for the reservoir of Dashidaira dam. The agreement of the results obtained from the developed model has been compared with those obtained from other models.

Key words: Flushing, Finite difference, Control volume, Thomas algorithm, Boundary conditions.

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$$C_s = f\left(\frac{\gamma}{\gamma_s - \gamma}, \frac{u^3}{g \cdot \omega \cdot h}\right) \quad (1)$$

$$C_s = k_0 \times \frac{\gamma}{\gamma_s - \gamma} \times \left(\frac{u^3}{g \cdot \omega \cdot h}\right)^m \quad (2)$$

$m \quad k_0$

$$q_s = u \cdot h \cdot C_s \quad (3)$$

$$q_s = \frac{k_0 \cdot u^{3m+1} \cdot h^{1-m}}{(sg - 1)g^m \omega^m} \quad (4)$$

sg
 u

$$q_s = \frac{k_0 \cdot h^{m+\frac{5}{3}} \cdot S^{\frac{3m+1}{2}}}{(sg - 1) \cdot g^m \cdot \omega^m \cdot n^{3m+1}} \quad (5)$$

$$(1-p) \times \frac{\partial Z}{\partial t} + \frac{\partial q_s}{\partial x} = 0 \quad (6)$$

$$\frac{\partial q_s}{\partial x} = \dots \quad (7)$$

$$\frac{\partial q_s}{\partial x} = \frac{k_0 \cdot h^{m+\frac{5}{3}} \cdot (3m+1) \cdot S^{\frac{3m-1}{2}}}{(sg - 1) \cdot g^m \cdot \omega^m \cdot n^{3m+1} \cdot 2} \cdot \frac{\partial S}{\partial x} \quad (8)$$

$$h = \left(\frac{n \cdot q}{S^{\frac{1}{2}}}\right)^{\frac{3}{5}} \quad (9)$$

$$C_s = f(u, h, g, \gamma, \gamma_s - \gamma, \omega) \quad (10)$$

$$\frac{\partial q_s}{\partial x} = \frac{k_0 \cdot q^{0.6m+1} \cdot (3m+1) \cdot S^{1.2m-1}}{(sg - 1) \cdot g^m \cdot \omega^m \cdot n^{2.4m} \cdot 2} \cdot \frac{\partial S}{\partial x} \quad (11)$$

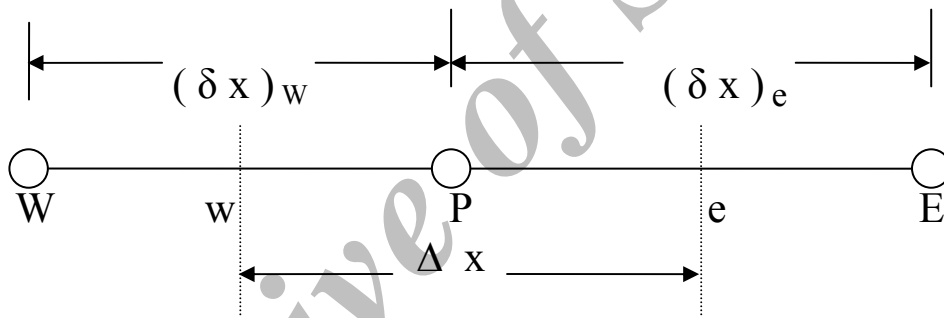
$$S = - \left| \frac{\partial Z}{\partial x} \right| \quad (12)$$

$$\frac{\partial S}{\partial x} = -\frac{\partial^2 Z}{\partial x^2} \quad ()$$

$$\frac{\partial Z}{\partial t} - \Gamma \frac{\partial^2 Z}{\partial x^2} = 0 \quad ()$$

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$$\Gamma = \frac{k_{0,q}^{0.6m+1} \cdot (3m+1)}{2(1-p)(sg-1)g^m \cdot \omega^m \cdot n^{2.4m}} \cdot S^{1.2m-1} \quad ()$$



$$+\theta \left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^{n+1} - Z_i^{n+1}) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^{n+1} - Z_{i-1}^{n+1}) \right] \Delta t$$

$$= (Z_i^{n+1} - Z_i^{n+1}) \Delta x \quad ()$$

$$\int_t^{t+\Delta t} \int_w^e \Gamma \frac{\partial^2 Z}{\partial x^2} dx dt = \int_t^{t+\Delta t} \Gamma_P \left(\frac{\partial Z}{\partial x} \right) \Big|_w^e dt$$

$$= \left[\Gamma_P \frac{Z_e - Z_P}{(\delta x)_e} - \Gamma_P \frac{Z_P - Z_w}{(\delta x)_w} \right] \Delta t \quad ()$$

$$\frac{\Delta x}{\Delta t} = \alpha$$

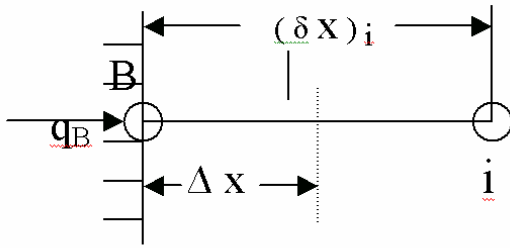
$$\int_t^{t+\Delta t} \int_w^e \frac{\partial Z}{\partial t} dx dt = \int_w^e (\Delta Z) \Big|_t^{t+\Delta t} dx = (Z_P^{n+1} - Z_P^n) \Delta x \quad ()$$

$$() \quad \alpha$$

$$() \quad P, W, E, w, e$$

$$A_i Z_{i-1}^{n+1} + B_i Z_i^{n+1} + C_i Z_{i+1}^{n+1} = D_i \quad ()$$

$$((1-\theta) \left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^n - Z_i^n) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^n - Z_{i-1}^n) \right]) \Delta t$$



$$A_i = \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_w} \quad ()$$

$$B_i = -\frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_e} - \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_w} - 1 \quad ()$$

$$C_i = \frac{\alpha \cdot \theta \cdot \Gamma_i}{(\delta x)_e} \quad ()$$

$$D_i = -\alpha(1-\theta) \quad ()$$

$$\left[\frac{\Gamma_i}{(\delta x)_e} \cdot (Z_{i+1}^n - Z_i^n) - \frac{\Gamma_i}{(\delta x)_w} \cdot (Z_i^n - Z_{i-1}^n) \right] - Z_i^n \quad ()$$

$$Z = Z(0, t) \quad ()$$

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$$\Gamma_i = \frac{k_0 \cdot q^{0.6m+1} \cdot (3m+1)}{2(1-p)(sg-1)g^m \cdot \omega^m \cdot n^{2.4m}} \quad ()$$

$$\frac{Z - Z_{i-1}}{2\Delta x_i}^{(1.2m-1)} \quad ()$$

$$B_n = 1, \quad A_n = 0, \quad D_n = Z(0, t), \quad C_n = 0 \quad ()$$

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$$h \quad ()$$

$$: \quad ()$$

$$\frac{\partial Z}{\partial x} = -\left(\frac{q_s \cdot (sg-1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \quad ()$$

$$D_s$$

$$: \quad () \quad ()$$

$$\frac{Z_2 - Z_1}{(\delta x)_c} = -\left(\frac{q_s \cdot (sg-1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \quad ()$$

$$\omega = \sqrt{\frac{4gD_s}{3C_D}(sg-1)} \quad ()$$

$$C_D = \frac{24}{R_e} + \frac{3}{\sqrt{R_e}} + 0.34 \quad ()$$

$$R_e = \frac{\rho \omega D_s}{\mu} \quad ()$$

$$C_1 = 0, \quad B_1 = 1, \quad A_1 = 0$$

$$D_1 = \left(\frac{q_s \cdot (sg-1) \cdot g^m \cdot \omega^m \cdot n^{2.4m}}{k_0 \cdot q^{0.6m+1}} \right)^{\frac{0.833}{m}} \times \frac{(\delta x)_e}{2} \quad ()$$

$$m \quad k_0$$

$$= sg$$

$$()$$

$$= D_s$$

$$/$$

$$= R_e$$

$$/$$

$$= \rho$$

$$[]$$

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$$()$$

$$\omega = \frac{g}{18\mu} (sg - 1) \cdot D_s^2 \quad ()$$

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|-----|------|-----|------------|-------|---------|--|
| 40 | 0.18 | 8.6 | 0.00000216 | 0.064 | 0.02 | |
| 30 | 0.0 | 9 | 0.0 | 0.1 | 0.00487 | |

$$m \quad k_0$$

$$/$$

$$[]$$

$$k_0 = 1.456 \times 10^{-6}$$

$$m = 1$$

$$() ()$$

$$D_s = 0.3mm$$

$$p = 0.4$$

$$\gamma_s = 2640 kg / m^3$$

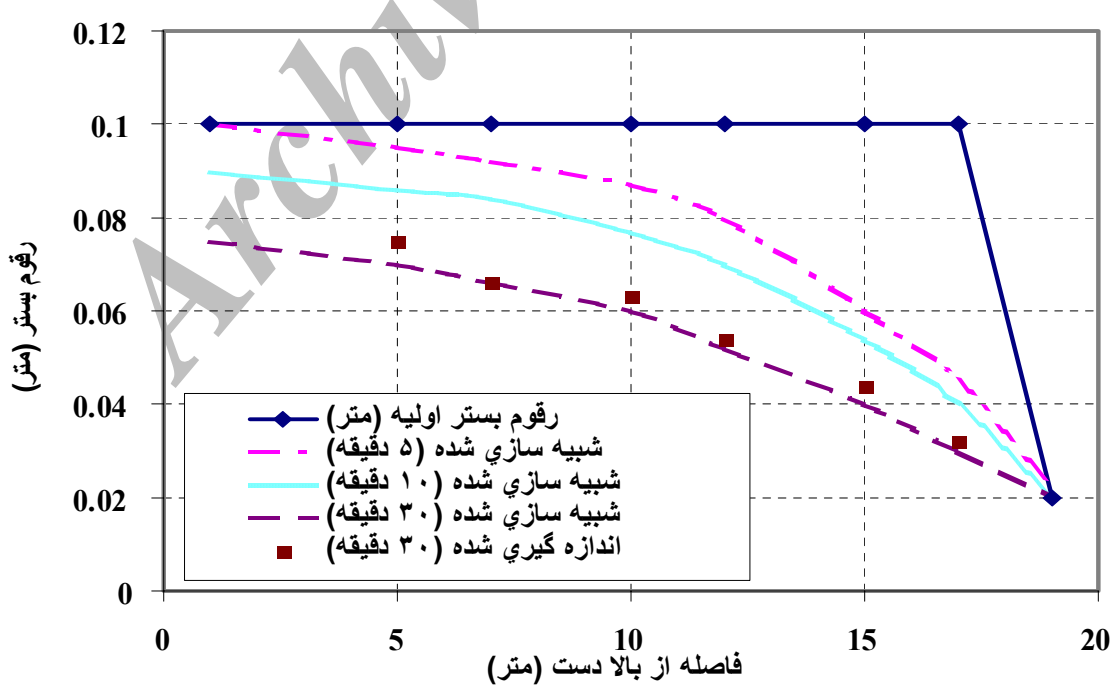
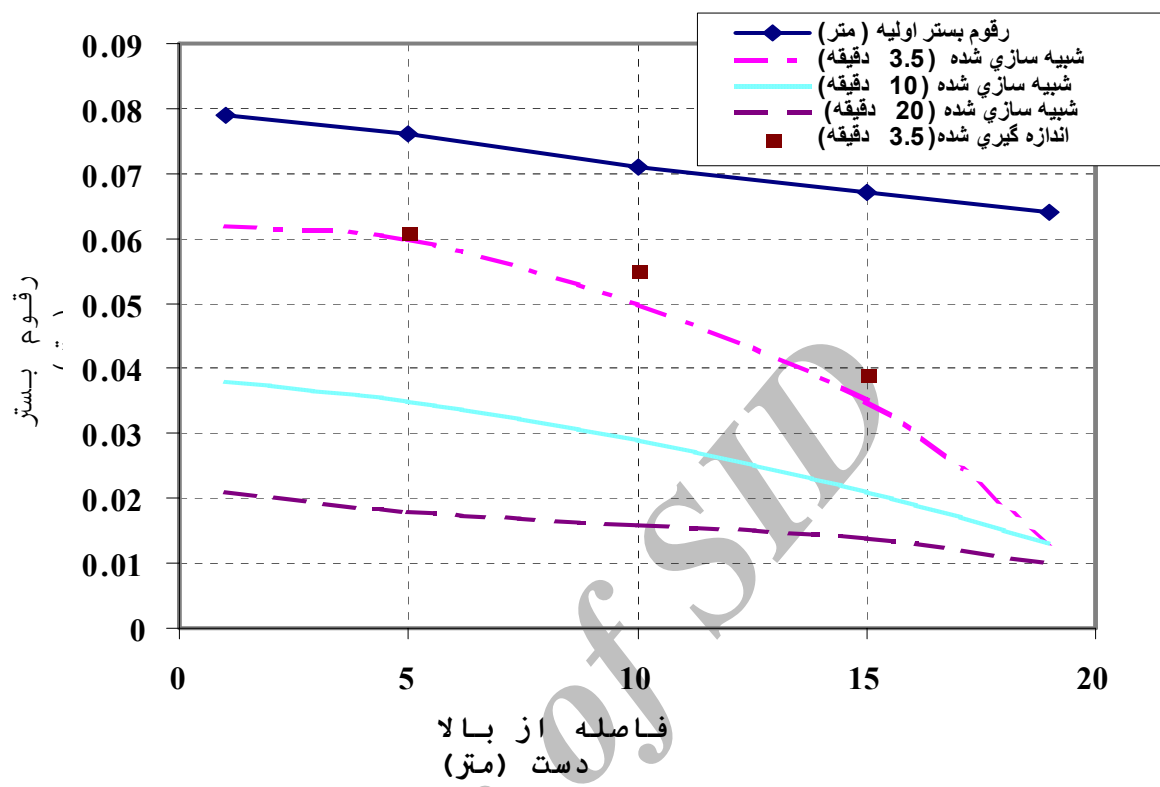
$$n = 0.03$$

$$Q = 50 m^3 / s$$

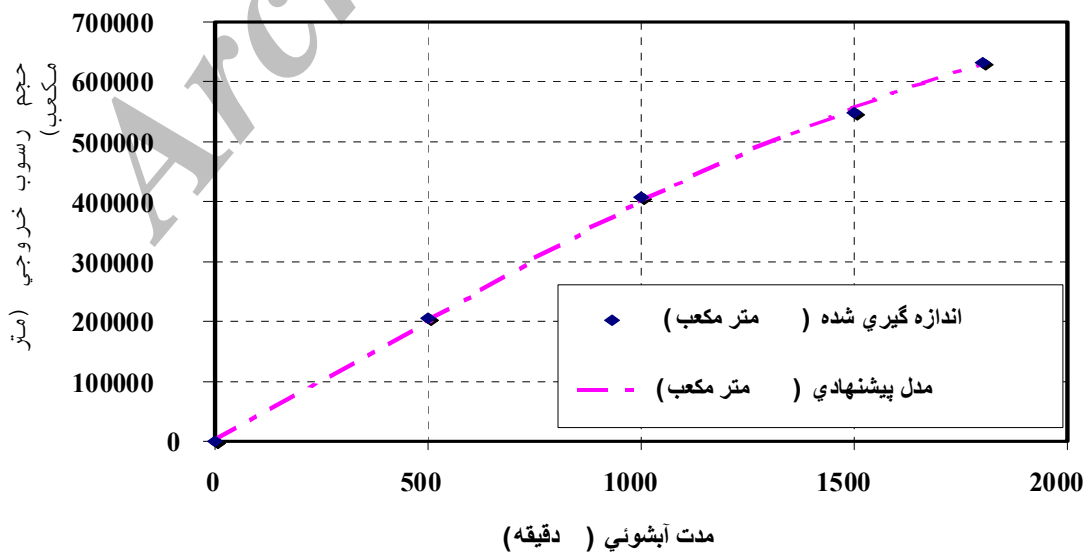
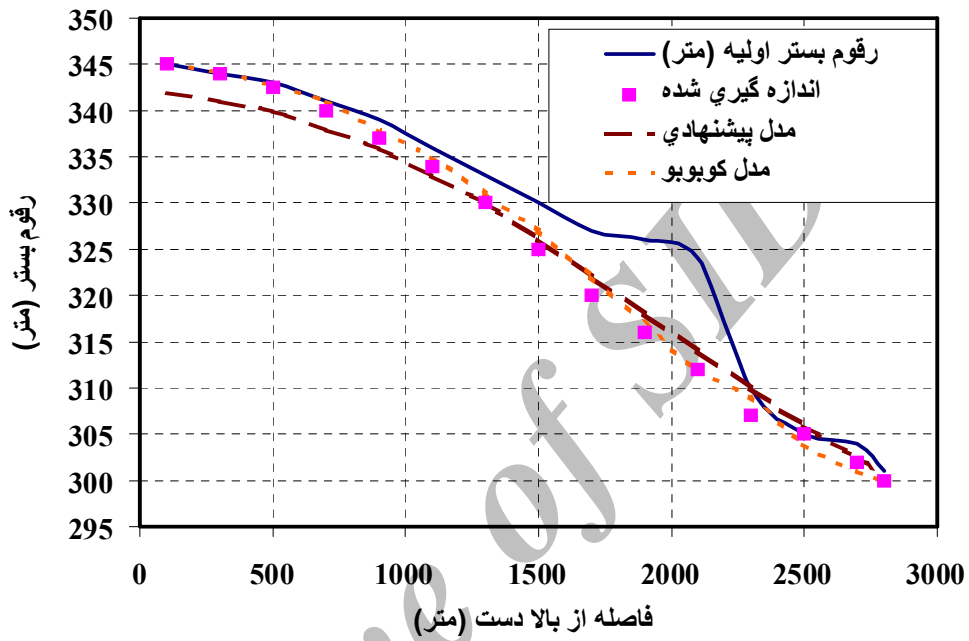
$$Z(0, t) = 29.8 m$$

$$\Delta t = 600 \text{ sec.}$$

$$\Delta x = 100 m$$



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μ q q_s x T Δt θ Z u h ω P k_0 C_D R_e S ρ D_s

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