

## **The Transportation Index of Different Provinces In the Country**

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### **Abstract**

The objective of this study is to define an index for ranking the provinces (states) of our country in terms of transportation facilities. This index which is aimed to represent the potential of transportation facilities in each province, is a dimensionless number. By the potential of transportation facilities we mean factors such as length of highways and railways, number of airports and harbors, the population of vehicles, the tonnage of goods and number of passengers. A mathematical approach rather than a statistical one is suggested this index, as the transportation industry is very vast with different variations, and presentation of mere statistical figures would not be helpful. In this regards, three indices are presented, which are hoped to assist the government, investors and the planners in evaluating the transportation facilities of the provinces for their planning purposes.

**Key words: Index, Transportation, Province, Ranking, Iran.**

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(Multiple Criteria Decision Making)

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468	321	1063	292	810	126	107	29	22.5	-	3582	45481
88	288	1790	61	640	104	102	-	7.5	-	2689	37463
-	281	264	283	494	50	36	-	15	-	1258	17888
649	100	511	2165	798	149	581	78	22.5	-	4226	107027
-	127	689	215	368	-	26	-	7.5	-	526	20150
-	128	1661	11	160	79	46	-	30	16.1	801	23168
531	48	385	175	666	172	260	148	45	-	12040	19196
-	14	93	170	704	313	25	-	7.5	-	820	16201
658	339	2582	2492	1937	238	190	-	45	-	6515	302966
384	413	1432	920	1165	588	381	-	52.5	16.9	4036	63213
193	169	450	255	124	205	32	110	-	-	1117	21841
1034	35	570	178	173	216	408	-	7.5	-	5402	96816
96	591	2596	646	1080	609	13	-	37.5	1.32	1855	178431
-	188	2110	1457	1635	352	125	-	45	-	4112	121825
122	145	434	50	357	145	21	165	7.5	-	1043	15491
307	13	135	95	88	69	105	139	-	-	919	11237
-	247	685	403	291	-	3	-	7.5	-	1450	28817
700	188	1989	932	1728	-	170	27	52.5	-	2159	181714
-	308	959	435	335	86	178	-	15	-	1916	24641
-	65	358	520	98	275	3	-	7.5	-	586	15563
65	21	111	210	381	454	144	-	-	0.55	1536	20893
-	128	812	309	269	61	185	-	15	0.73	2415	13952
215	130	488	129	550	140	164	-	7.5	-	1706	28392
213	125	686	622	459	53	311	13	30	1.31	2803	23833
352	95	578	174	388	72	168	-	-	-	1323	29406
313	119	1662	474	169	100	34	8	7.5	14.75	1144	71193
-	174	309	420	385	142	298	-	7.5	-	1807	19547
553	17	662	1051	635	-	151	-	15	-	808	73467

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-	120	548	-	-	330	725	8210	3775
-	120	205	-	-	550	110	2310	3619
-	100	103	-	-	-	-	2170	1264
620	2150	1023	-	-	10750	308	21440	6532
-	100	13	-	-	-	-	720	424
-	1270	438	4650	10.41	-	-	980	1014
18650	55600	6824	-	-	3660	3915	25390	22574
-	100	16	-	-	-	-	530	1815
8850	120	1888	-	-	1450	4212	10140	4828
12500	12250	1318	34100	7.57	4200	1052	16520	2485
-	-	-	-	-	520	817	1470	992
8450	-	-	-	-	1380	615	5630	1697
-	100	417	3450	2.67	300	98	2770	1476
-	200	1239	-	-	-	-	13560	3334
150	-	-	-	-	140	330	2720	1972
-	-	-	-	-	3000	118	1280	2702
-	100	11	-	-	-	-	1820	2681
-	1150	388	-	-	580	215	5420	1141
-	1500	318	-	-	-	-	2440	3795
-	200	-	-	-	-	-	300	624
1150	-	25	300	3.11	100	110	3550	1670
130	120	103	3300	7.81	-	-	4190	2342
620	100	19	-	-	300	941	3540	2072
-	120	42	2200	-	500	315	4920	2953
-	-	-	-	-	1350	1117	6180	2461
-	1100	1585	55000	52.12	4500	523	10780	983
-	120	30	-	-	-	-	3820	3311
-	650	238	-	-	6850	309	4520	1038

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1.5	48	10	4.8	4.8	( )
	24	4.8	10	20	( )

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250	50	70	100	120	180	300	500

(Alternatives) = A<sub>j</sub>  
(m=28)

	X <sub>1</sub>	X <sub>2</sub>	...	X <sub>n</sub>
A <sub>1</sub>	r <sub>11</sub>	r <sub>12</sub>	...	r <sub>1n</sub>
...	...	...	...	...
A <sub>m</sub>	r <sub>m1</sub>	r <sub>m2</sub>	...	r <sub>mn</sub>

(Attributes) = X<sub>i</sub>

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( ) n=10

( ) n = 9

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r<sub>ij</sub>

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( )	( )
15	1.50

$w$  ) (

$i$   $j$  ( )

VMP (Vector Maximization Problem)

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$X^*$

$X^* \in S \quad F(x^*) > F(x) \quad : \quad \text{VMP}$

( $X \in S$ ) )

( A\* [ ]

$$A^* \approx \{X_1^*, X_2^*, \dots, X_n^*\}$$

$$\rightarrow X_j^* = \text{Max}_i U_j(r_{ij}) ; i = 1, 2, \dots, m \quad ( )$$

J ( )  $U_j$

) ( A\* )

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(Decision

Maker)

$r_{11}$  .( )

0.0006	0.0023	0.0028	0.0178	0.0064	0.0230	0.0071	0.0103	0	0.0005
0	0.0027	0.0028	0.0171	0.0016	0.0478	0.0077	0.0023	0	0.0002
0	0.0020	0.0028	0.0276	0.0158	0.0147	0.0157	0	0	0.0008
0.0007	0.0054	0.0014	0.0074	0.0202	0.0048	0.0009	0.0061	0	0.0002
0	0.0013	0	0.0183	0.0107	0.0342	0.0063	0	0	0.0004
0	0.0020	0.0034	0.0069	0.0005	0.0717	0.0055	0	0.0007	0.0013
0.0077	0.0135	0.0089	0.0347	0.0091	0.0201	0.0025	0.0276	0	0.0023
0	0.0154	0.0193	0.0434	0.0105	0.0057	0.0009	0	0	0.0005
0	0.0006	0.0008	0.0064	0.0082	0.0085	0.0011	0.0022	0	0.0001
0	0.0060	0.0093	0.0184	0.0145	0.0226	0.0065	0.0061	0.0003	0.0008
0.0050	0.0015	0.0094	0.0057	0.0117	0.0206	0.0077	0.0088	0	0
0	0.0042	0.0022	0.0018	0.0018	0.0059	0.0004	0.0107	0	0.0001
0	0.0001	0.0034	0.0061	0.0036	0.0145	0.0033	0.0005	0.00007	0.0021
0	0.0010	0.0029	0.0134	0.0119	0.0173	0.0015	0	0	0.0004
0.0106	0.0013	0.0094	0.0230	0.0032	0.0280	0.0094	0.0079	0	0.0005
0.0124	0.0093	0.0061	0.0078	0.0084	0.0120	0.0012	0.0273	0	0
0	0.0001	0	0.0101	0.0140	0.0237	0.0086	0	0	0.0003
0.0002	0.0009	0	0.0095	0.0051	0.0109	0.0010	0.0038	0	0.0003
0	0.0009	0.0004	0.0016	0.0021	0.0046	0.0015	0	0	0.0006
0	0.0002	0.0176	0.0063	0.0334	0.0230	0.0041	0	0	0.0005
0	0.0069	0.0217	0.0182	0.0101	0.0053	0.0010	0.0031	0.00003	0
0	0.0133	0.0044	0.0193	0.0221	0.0582	0.0091	0	0.00005	0.0010
0	0.0058	0.0049	0.0194	0.0045	0.0172	0.0046	0.0076	0	0.0003
0.0005	0.0131	0.0022	0.0193	0.0261	0.0287	0.0052	0.0089	0.00005	0.0012
0	0.0057	0.0024	0.0132	0.0059	0.0196	0.0032	0.0119	0	0
0.0001	0.0005	0.0014	0.0024	0.0066	0.0233	0.0017	0.0044	0.00021	0.0001
0	0.0152	0.0072	0.0197	0.0215	0.0158	0.0089	0	0	0.0004
0	0.0021	0	0.0086	0.0143	0.0090	0.0002	0.0075	0	0.0002

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0.0830	0.1805	0.0159	0.0072	0	0	0.0120	0.0026	0
0.0966	0.0616	0.0029	0.0147	0	0	0.0054	0.0032	0
0.0707	0.0121	0	0	0	0	0.0057	0.0056	0
0.0610	0.2003	0.0029	0.1004	0	0	0.0095	0.0200	0.0058
0.0210	0.0357	0	0	0	0	0.0006	0.0050	0
0.0437	0.0423	0	0	0.0449	0.0210	0.0189	0.0548	0
1.1759	1.3227	0.2040	0.1907	0	0	0.3550	2.8960	0.9715
0.1120	0.0327	0	0	0	0	0.0010	0.0061	0
0.0160	0.0334	0.0139	0.0048	0	0	0.0062	0.0004	0.0292
0.0393	0.2613	0.0166	0.0664	0.0001	0.5394	0.0069	0.0201	0
0.0454	0.0673	0.0374	0.0238	0	0	0	0	0
0.0175	0.0581	0.0063	0.0142	0	0	0	0	0.0873
0.0083	0.0155	0.0005	0.0017	0.0001	0.0193	0.0023	0.0006	0
0.0273	0.1110	0	0	0	0	0.0101	0.0016	0
0.1273	0.1756	0.0213	0.0090	0	0	0	0	0.0097
0.2404	0.1140	0.0105	0.2669	0	0	0	0	0
0.0930	0.0631	0	0	0	0	0.0004	0.0035	0
0.0063	0.0298	0.0012	0.0032	0	0	0.0021	0.0063	0
0.1540	0.0990	0	0	0	0	0.0129	0.0608	0
0.0401	0.0192	0	0	0	0	0	0.0128	0
0.0799	0.1699	0.0052	0.0048	0.0001	0.0143	0.0012	0	0.0551
0.1678	0.0301	0	0	0.0001	0.2365	0.0074	0.0086	0.0093
0.0729	0.1247	0.0105	0	0	0	0.0007	0.00352	0.0218
0.1239	0.2064	0.0132	0.0210	0	0.0923	0.0017	0.00503	0
0.0837	0.2102	0.038	0.0460	0	0	0	0	0
0.0138	0.1510	0.0073	0.0632	0.0007	0.7725	0.0222	0.0154	0
0.1694	0.1954	0	0	0	0	0.0015	0.0061	0
0.0141	0.0615	0.0042	0.0932	0	0	0.0032	0.0088	0

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$$A^* = \{A_i \mid \text{Max}_i \frac{\sum_j w_j r_{ij}}{\sum_j w_j}\} \quad (1)$$

$$\sum_j w_j = 1$$

$$A^* = \{A_i \mid \text{Max}_i \sum_j w_j r_{ij}\} = 1 \quad (2)$$

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(First Generation Method)

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0.320	0.690	0.504	2.136	0.640	1.610	0.355	2.575	0	0.073
0	0.816	0.498	2.052	0.160	3.346	0.385	0.575	0	0.030
0	0.600	0.504	3.312	1.580	1.029	0.785	0	0	0.126
0.365	1.620	0.252	0.888	2.020	0.336	0.0465	1.550	0	0.031
0	0.390	0	2.196	1.067	2.394	0.315	0	0	0.055
0	0.594	0.612	0.829	0.050	5.019	0.275	0	1.050	0.195
3.850	4.050	1.602	4.164	0.911	1.403	0.125	6.900	0	0.345
0	0.462	3.477	5.208	1.050	0.402	0.430	0	0	0.069
0	0.189	0.140	0.767	0.822	0.596	0.056	0.550	0	0.021
0	1.809	1.674	2.211	1.450	1.582	0.325	1.525	0.450	0.124
2.515	0.438	1.688	0.680	1.167	1.442	0.385	2.200	0	0
0	1.263	0.401	0.213	0.184	0.411	0.018	2.675	0	0.011
0	0.021	0.614	0.726	0.360	1.015	0.165	0.135	0.111	0.315
0	0.300	0.520	1.610	1.196	1.212	0.077	0	0	0.055
5.325	0.405	1.685	2.765	0.322	1.960	0.468	1.975	0	0.072
6.185	2.802	1.105	0.939	0.845	0.841	0.058	6.825	0	0
0	0.031	0	1.212	1.398	1.659	0.428	0	0	0.039
0	0.279	0	1.141	0.510	0.766	0.051	0.962	0	0.045
0	0.258	0.074	0.734	0.211	0.325	0.075	0	0	0.091
0	0.060	3.170	0.756	3.340	1.610	0.205	0	0	0.072
0	2.067	3.906	2.187	1.005	0.371	0.050	0.775	0.045	0
0.074	3.978	0.786	2.316	2.214	4.074	0.458	0	0.075	0.150
0	1.731	0.887	2.324	0.454	1.203	0.228	1.900	0	0.039
0.270	3.915	0.399	2.311	2.610	2.014	0.262	2.236	0.075	0.180
0	1.713	0.441	1.583	0.591	1.375	0.162	2.992	0	0
0.055	0.141	0.252	0.284	0.660	1.634	0.083	1.100	0.315	0.015
0	4.572	1.307	2.364	2.148	1.107	0.445	0	0	0.060
0	0.615	0	1.037	1.431	0.631	0.011	1.882	0	0.030

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0.398	1.805	0.159	0.034	0	0	0.288	0.012	0
0.464	0.616	0.029	0.071	0	0	0.129	0.015	0
0.339	0.121	0	0	0	0	0.137	0.027	0
0.293	2.003	0.029	0.482	0	0	0.229	0.096	0.007
0.101	0.357	0	0	0	0	0.015	0.024	0
0.209	0.423	0	0	0.898	0.096	0.454	0.263	0
5.644	13.27	2.040	0.915	0	0	8.520	13.90	1.214
0.537	0.327	0	0	0	0	0.023	0.029	0
0.077	0.334	0.139	0.023	0	0	0.149	0.002	0.036
0.188	2.613	0.166	0.318	0.002	2.589	0.166	0.965	0
0.218	0.673	0.374	0.114	0	0	0	0	0
0.084	0.581	0.063	0.068	0	0	0	0	0.109
0.039	0.155	0.006	0.008	0.001	0.092	0.055	0.003	0
0.131	1.110	0	0	0	0	0.242	0.008	0
0.611	1.756	0.213	0.043	0	0	0	0	0.012
1.154	1.140	0.105	1.281	0	0	0	0	0
0.446	0.631	0	0	0	0	0.009	0.017	0
0.030	0.298	0.012	0.015	0	0	0.050	0.030	0
0.739	0.990	0	0	0	0	0.309	0.292	0
0.192	0.192	0	0	0	0	0	0.061	0
0.383	1.699	0.052	0.023	0.001	0.068	0.028	0	0.069
0.805	0.300	0	0	0.001	1.135	0.177	0.041	0.017
0.350	1.247	0.105	0	0	0	0.016	0.017	0.027
0.595	2.064	0.132	0.101	0	0.443	0.042	0.024	0
0.401	2.101	0.380	0.221	0	0	0	0	0
0.066	1.510	0.073	0.303	0.015	3.708	0.533	0.074	0
0.813	1.954	0	0	0	0	0.037	0.029	0
0.067	0.615	0.042	0.447	0	0	0.078	0.042	0

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$$\frac{2.515}{6.185} + \frac{0.438}{4.050} + \frac{1.688}{3.906} + \frac{0.680}{4.164} + \dots = 4.0693$$

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$$\frac{0.218}{5.644} + \frac{0.673}{13.227} + \frac{0.374}{2.040} + \frac{0.114}{1.281} + \dots = 1.859$$

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w<sub>j</sub>

$$A_{i+1} \ A_i$$

[1]

$$\sum_j w_j r'_{A_j} > \sum_j w_j r'_{A_{i+j}} \rightarrow \sum_j w_j r'_{ij} > \sum_j w_j r'_{(i+1)j} \quad ( )$$

$$w^t (r'_i - r'_{i+1}) > 0$$

$$w \in W = \left\{ w \mid \sum_j w_j = 1 ; w_j > 0 \right\} \quad ( )$$

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α

$$\alpha (A_1, \dots, A_i, \dots, A_m)$$

i

$$\alpha (i)$$

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0.8911	3.6646	
0.6932	3.4780	
0.6302	2.8111	
1.0205	2.1908	
0.4312	2.4260	
1.6316	3.8522	
2.4072	8.4386	
0.7336	2.9433	
1.0284	2.0565	
2.0089	4.9603	
1.8592	4.0636	
2.9599	1.326	
0.6758	1.8934	
1.0637	3.1199	
1.8711	3.6688	
1.4337	4.0038	
0.6691	2.0819	
0.7295	1.2183	
0.9764	4.0291	
0.4161	3.3819	
0.4641	3.5475	
0.5897	5.0500	
0.9537	2.8494	
0.7849	5.0948	
1.6177	3.5567	
5.0531	2.2446	
0.7378	4.9575	
2.5691	2.5365	

(8.4386-5.0948 = 3.3438)

$$\begin{cases} w^t (r^{\alpha(i)} - r^{\alpha(i+1)}) > 0; i = 1, 2, \dots, m-1 \\ w \in W_\alpha; W_\alpha = \{w | w \in W\} \end{cases} \quad (1)$$

$$w_\alpha \quad w \quad ( \quad ) \quad \alpha \quad w \in W_\alpha \quad m-1 \quad ( \quad ) \quad DM \quad ( \quad ) \quad ( \quad )$$

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MAX Z

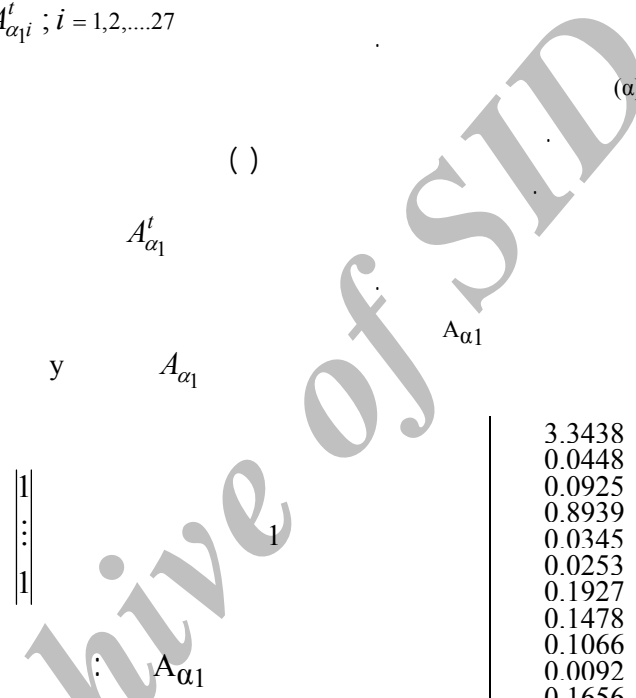
Subjet to :  $A_{\alpha 1}^t \cdot y + Z \cdot 1 \leq A_{\alpha i}^t ; i = 1, 2, \dots, 27$

$y_i \geq 0$

Z :

$$i \quad A_{\alpha 1}^t \quad A_{\alpha 1} \quad A_{\alpha 1}^t \quad A_{\alpha 1} \quad ( \quad ) \quad (x_2) \quad (x_1)$$

$$\begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix} \quad y \quad A_{\alpha 1} \quad ( \quad )$$



3.3438	1.6223
0.0448	0.1952
0.0925	-0.1481
0.8939	-1.1214
0.0345	0.8828
0.0253	-0.4573
0.1927	0.9034
0.1478	-1.3407
0.1066	1.2533
0.0092	0.1536
0.1656	0.0480
0.0297	-1.2155
0.0876	0.8405
0.0866	0.1979
0.0581	-0.4704
0.1766	0.3301
0.0939	-0.2201
0.1591	-1.0552
0.1538	-0.5902
0.1105	2.1678
0.0441	-0.2377
0.1373	-4.3841
0.0538	4.0325
0.1343	-0.0079
0.1631	0.3526
0.5672	-2.2841
0.1079	2.2304

Max Z  
 Subjet to :  
 3.3438Y1+0.0448Y2+0.0925Y3+0.8939Y4+0.0345Y5  
 +0.0253Y6+ 0.1927Y7 +0.1478Y8 +0.1066Y9  
 +0.0092Y10+0.1656Y11 +0.0297Y12+ 0.0876Y13+  
 0.0866Y14+0.0581Y15 +0.1766Y16 +0.0939Y17  
 +0.1591Y18 +0.1538Y19 +0.1105Y20 +0.0441Y21  
 +0.1373Y22+0.0538Y23 +0.1343Y24 +0.1631Y25  
 +0.5672Y26+0.1079Y27+Z<=3.3438  
  
 1.6223Y1+0.1952Y2-0.1481Y3-1.1214Y4 +0.8828Y5-  
 0.4573Y6+0.9034Y7-1.3407Y8 +1.2532Y9 +0.1536Y10  
 +0.0481Y11-1.2155Y12+0.8405Y13 +0.1979Y14-  
 0.4704Y15+0.3301Y16-0.2200Y17-1.055Y18 -  
 0.5902Y19 +2.1678Y20-0.2377Y21-  
 4.3841Y22+4.0325Y23-0.0079Y24  
 +0.3526Y25+2.2841Y26 +2.2304Y27 +Z<=1.62  
 Y1>0 , Y2>0 , Y3>0 , Y4 >0 , Y5>0 , Y6>0 , Y7>0 ,  
 Y8 >0 , Y9>0 , Y10>0 , Y11>0 , Y12 >0 , Y13>0 ,  
 Y14>0 , Y15>0 , Y16 >0 , Y17>0 , Y18>0 , Y19>0 ,  
 Y20 >0 , Y21>0 , Y22>0 , Y23>0 , Y24 >0 , Y25>0 ,  
 Y26>0 , Y27>0  
 end.

(A<sub>α1</sub>)

$y_{12} = 1.3843 \quad Z = 3.3026 :$   
 $y_{12} > 0$

$$0.0297w_1 - 1.2155w_2 \geq 0$$

$$w = \begin{pmatrix} 0.9761 \\ 0.0239 \end{pmatrix}$$

( )

(.)

%			
9.03	8.294		
5.44	4.991		
5.38	4.943		
5.29	4.856		
4.37	4.011		
4.31	3.956		
4.29	3.942		
4.07	3.732		
3.94	3.621		
3.79	3.486		
3.78	3.474		
3.61	3.311		
3.60	3.311		
3.49	3.205		
3.39	3.116		
3.34	3.071		
3.15	2.891		
3.05	2.804		
2.91	2.674		
2.76	2.538		
2.59	2.378		
2.55	2.341		
2.52	2.312		
2.35	2.163		
2.21	2.032		
2.03	1.863		
1.48	1.365		
1.31	1.207		

$A_{\alpha 1}$

( )

$z > 0$

( )

)

(.

y

$z^*$

$A_{\alpha 1}$

$y_{12} > 0$

$A_{\alpha 1}$

$(A_{\alpha 1}) A_{\alpha 1}$

$A_{\alpha}$

$\alpha$  (m-1)

$\alpha$  ((m-1)\*n)

$(A_{\alpha(i)})$  i

$W_{\alpha}$

$(r'_{\alpha(i)} - r'_{\alpha(i+1)})$

:

$$A_{\alpha} W \geq 0$$

$$\sum_{j=1}^n w_j = 1$$

$$w_j \geq 0$$

( )

w

$W_{\alpha}$

{w}

:

$$\begin{cases} \begin{vmatrix} 0.0297 & -1.215 \\ & \end{vmatrix} \begin{vmatrix} w_1 \\ w_2 \end{vmatrix} \geq 0 \\ w_1 + w_2 = 1 \\ w_j \geq 0 \end{cases}$$

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[1] Robert W Stokes & James K Banks; Transportation Engineering, Oxford University Press, San Jose, 1999.

" [ ] [2] Thomas. L. Saaty; "Decision Making For Leaders", RWS Publications; 1990.

" [ ] [3] Fodor; Fuzzy Preference Modeling and Multicriteria Decision Support, Kluwer Academic Publication, 1995 .

" [ ] [4] Kerali H. R. et al; Data Analysis Procedures for Long-term Pavement Performance Prediction; Washington DC, National Academy Press, 1996.

" [ ] [5] Y. Wu & K. Lai, "An Approach to Fuzzy Multi-objective and Multi-index Transportation Problems", Proceedings of the 21st IASTED International Conference on Modeling, Identification, and Control, Austria, Feb, 2002

[6] Saaty Thomas; Decision Making With Dependence and Feedback, RWS Publication, Pittsburgh, 2001.

[ ] [7] Kornbluth J. S.; Analyzing Policy Effectiveness Using Cone Restricted Data Envelopment Analyzed; Journal of the Operational Research Society, 1991, 42(12), 1097-104.

[ ] [8] S. J. Chen & C. L. Hwang, "Fuzzy Multiple Attribute Decision Making", Verlag, 1992.

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