

# $\Delta$ TOA

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## **Design a Systolic Processor for Fast and Accurate Radar Identification by Using $\Delta$ TOA**

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### **Abstract**

Radar identification algorithms according to time of arrival (TOA), of the pulse train have very good accuracy. Since this accuracy is achieved by hard consequent computation, they are not suitable for real time applications. In this paper a systolic processor has been designed for radar identification using difference time of arrival matrix,  $\Delta$ TOA. High performance radar identification can be achieved by increasing the size of  $\Delta$ TOA, which increase the size of systolic array. Increasing the size of systolic array causes the clock propagation delay and asynchronous operation of cells. To overcome the above problems, the  $\Delta$ TOA matrix has been partitioned. Then the algorithm is applied to the  $\Delta$ TOA sub matrixes. The simulation results show, the effectiveness of the algorithm when accurate and high-speed identification is needed.

**Key words:** Radar identification, Matrix computation, Parallel processing, Systolic array.

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(ΔTOA)

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$$\Delta TOA = \begin{vmatrix} 0 & t_2 - t_1 & t_3 - t_1 & \dots & t_{N-1} - t_1 & t_N - t_1 \\ t_2 - t_1 & 0 & t_3 - t_2 & \dots & t_{N-1} - t_2 & t_N - t_2 \\ \vdots & \vdots & \vdots & & \vdots & \vdots \\ t_{N-1} - t_1 & t_{N-1} - t_2 & t_{N-1} - t_3 & \dots & 0 & t_N - t_{N-1} \\ t_N - t_1 & t_N - t_2 & t_N - t_3 & \dots & t_N - t_{N-1} & 0 \end{vmatrix} \quad ( )$$

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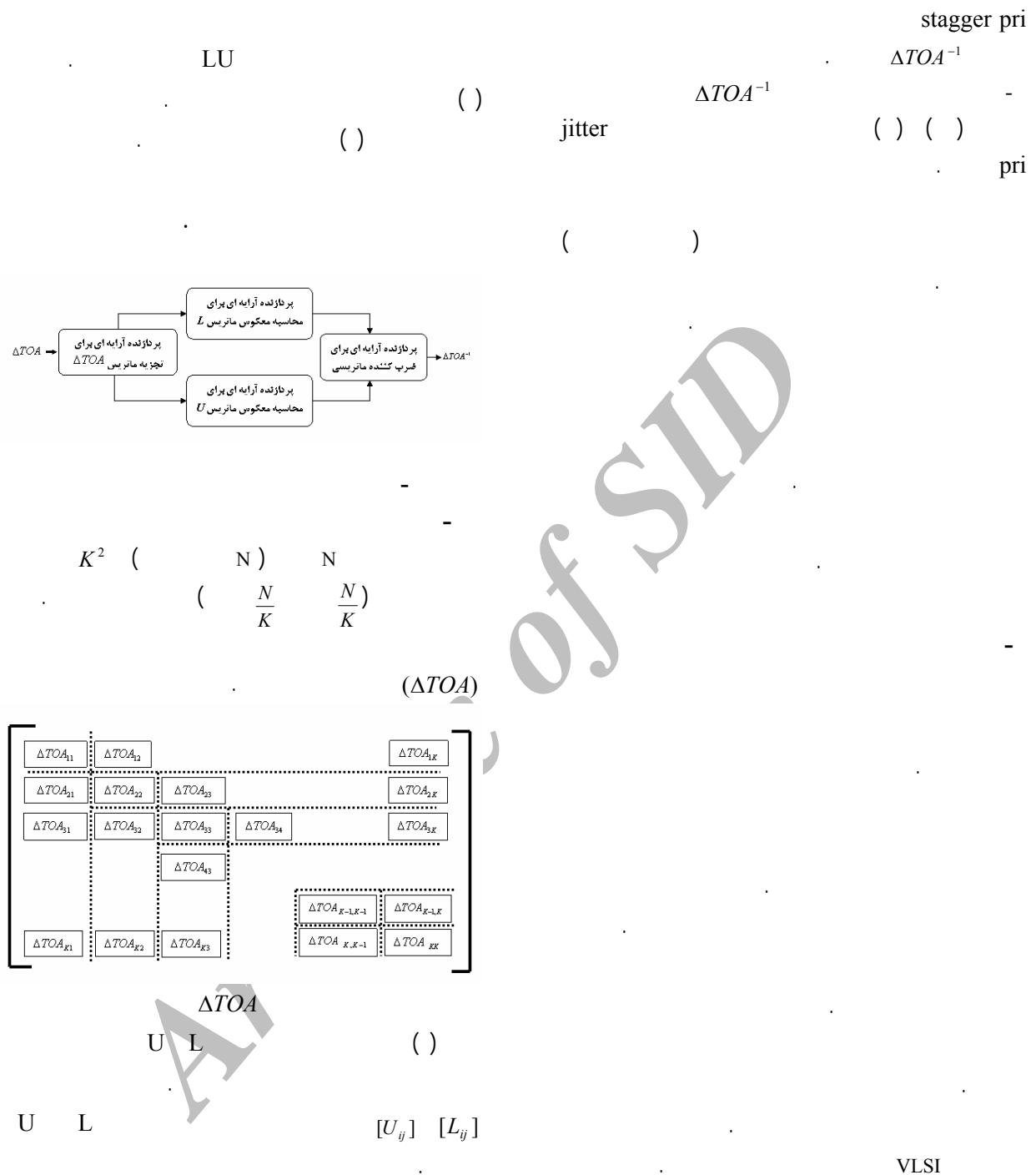
$$\Delta TOA(i, j) = |TOA(i) - TOA(j)| \quad 1 \leq i, j \leq N \quad ( )$$

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 $(\Delta TOA^{-1})$  $\Delta TOA^{-1}$  $\Delta TOA^{-1}$ 

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 $\Delta TOA^{-1}$

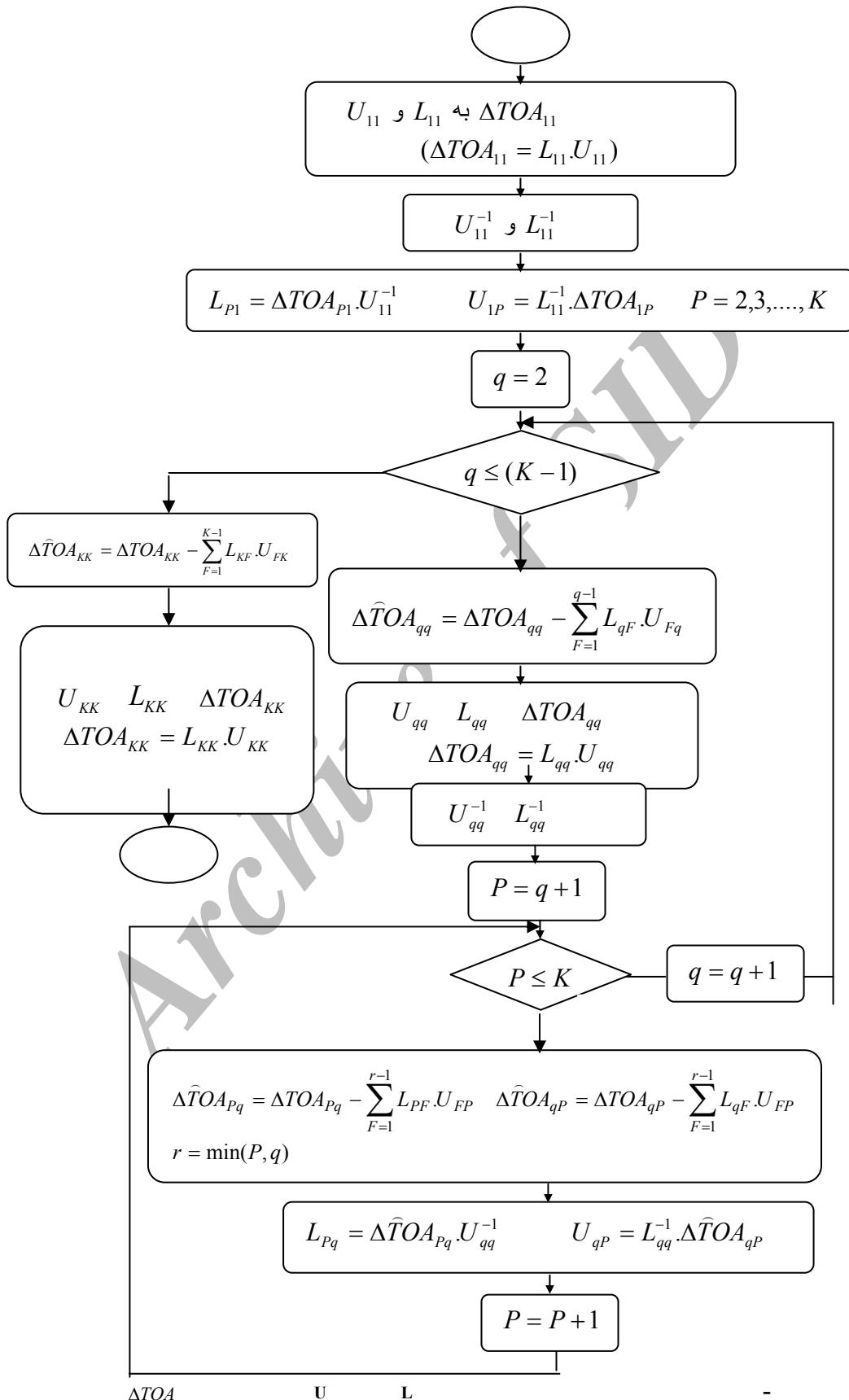


$$L = \begin{bmatrix} [L_{11}] & [0] & \cdots & \cdots & [0] \\ [L_{21}] & [L_{22}] & \cdots & \cdots & [0] \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ [L_{K1}] & [L_{K2}] & \cdots & \cdots & [L_{KK}] \end{bmatrix}$$

$$U = \begin{bmatrix} [U_{11}] & [U_{12}] & \cdots & [U_{1k}] \\ [0] & [U_{22}] & \cdots & [U_{2k}] \\ \vdots & \vdots & \ddots & \vdots \\ [0] & [0] & \cdots & [U_{kk}] \end{bmatrix}$$

ΔTOA

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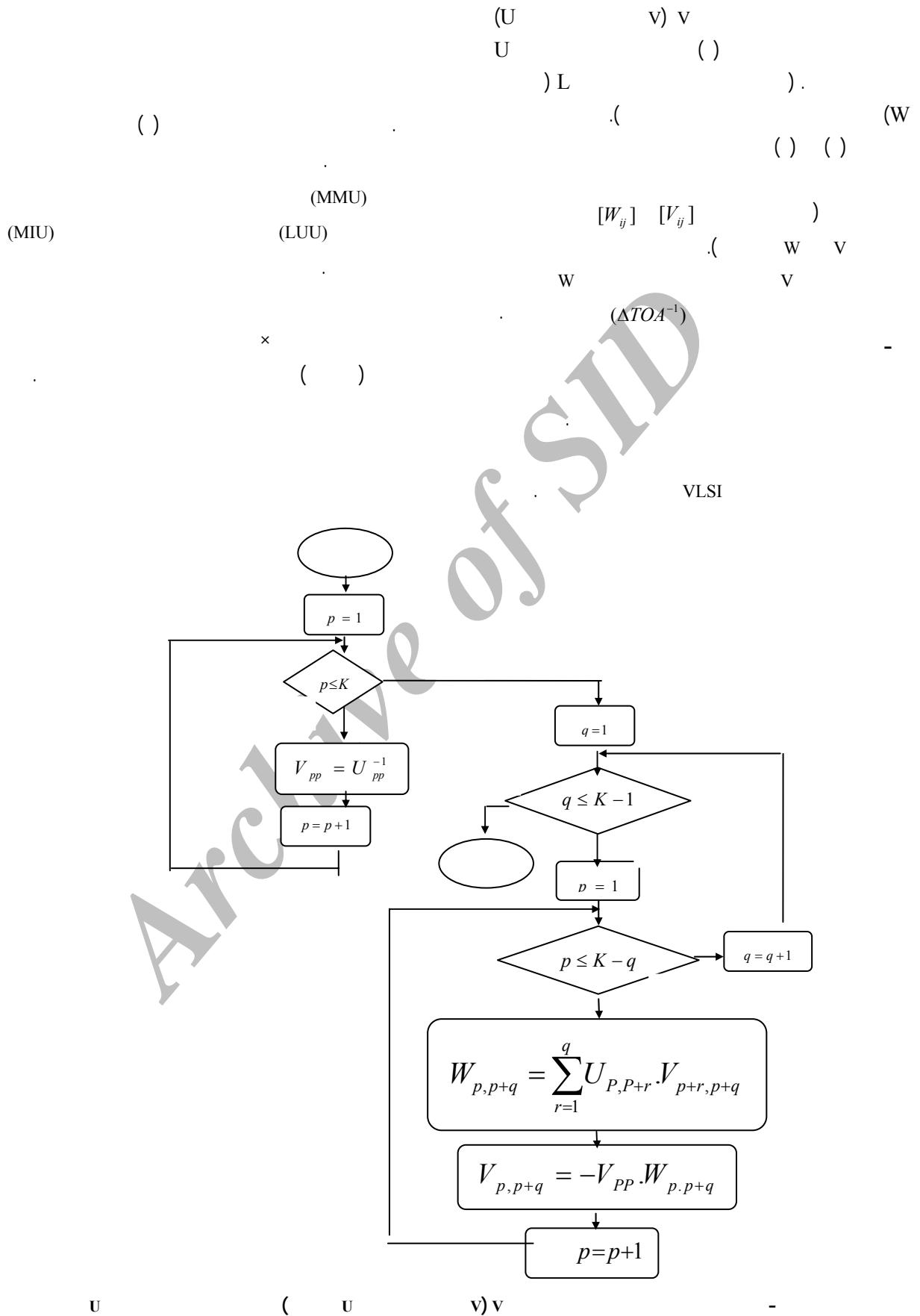


ΔTOA

U

L

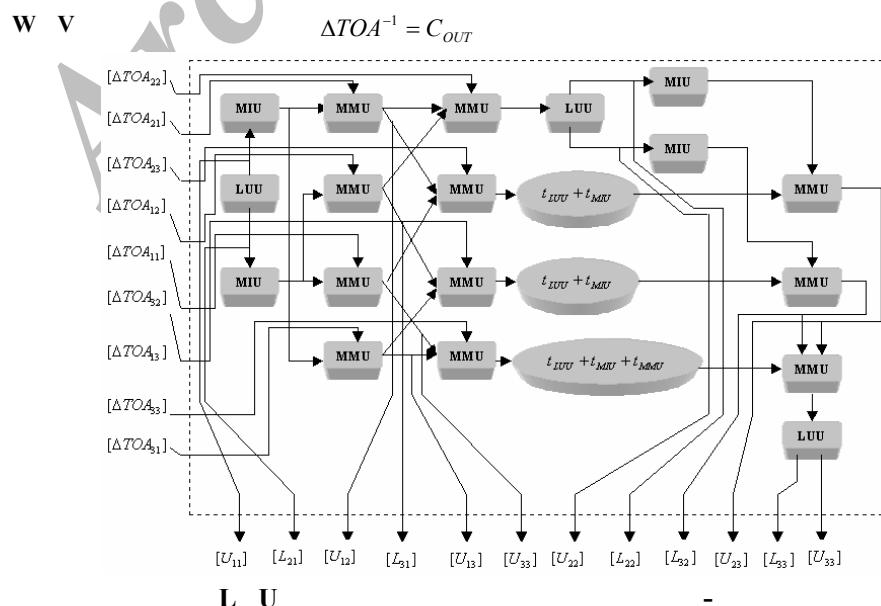
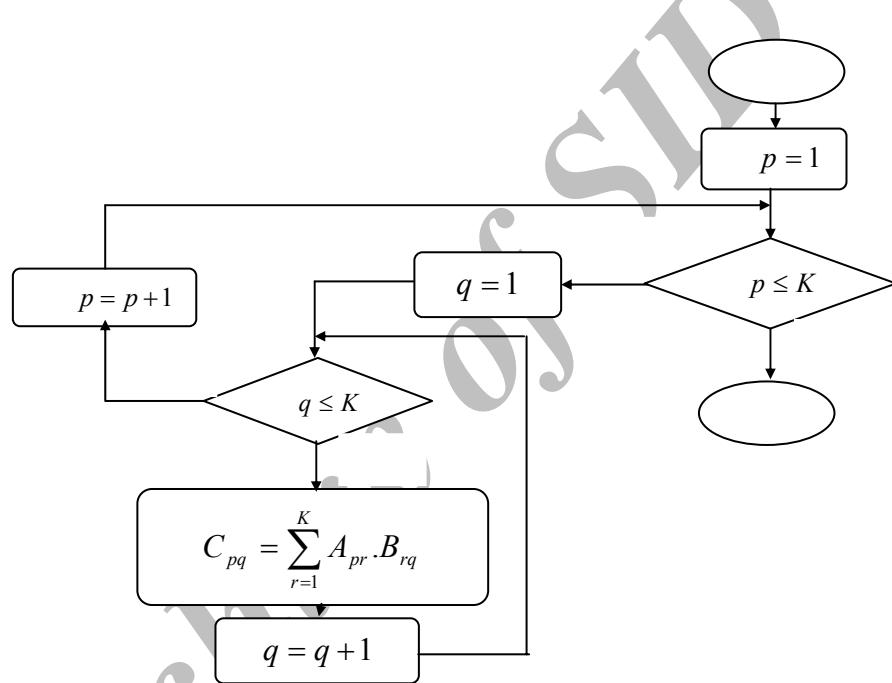
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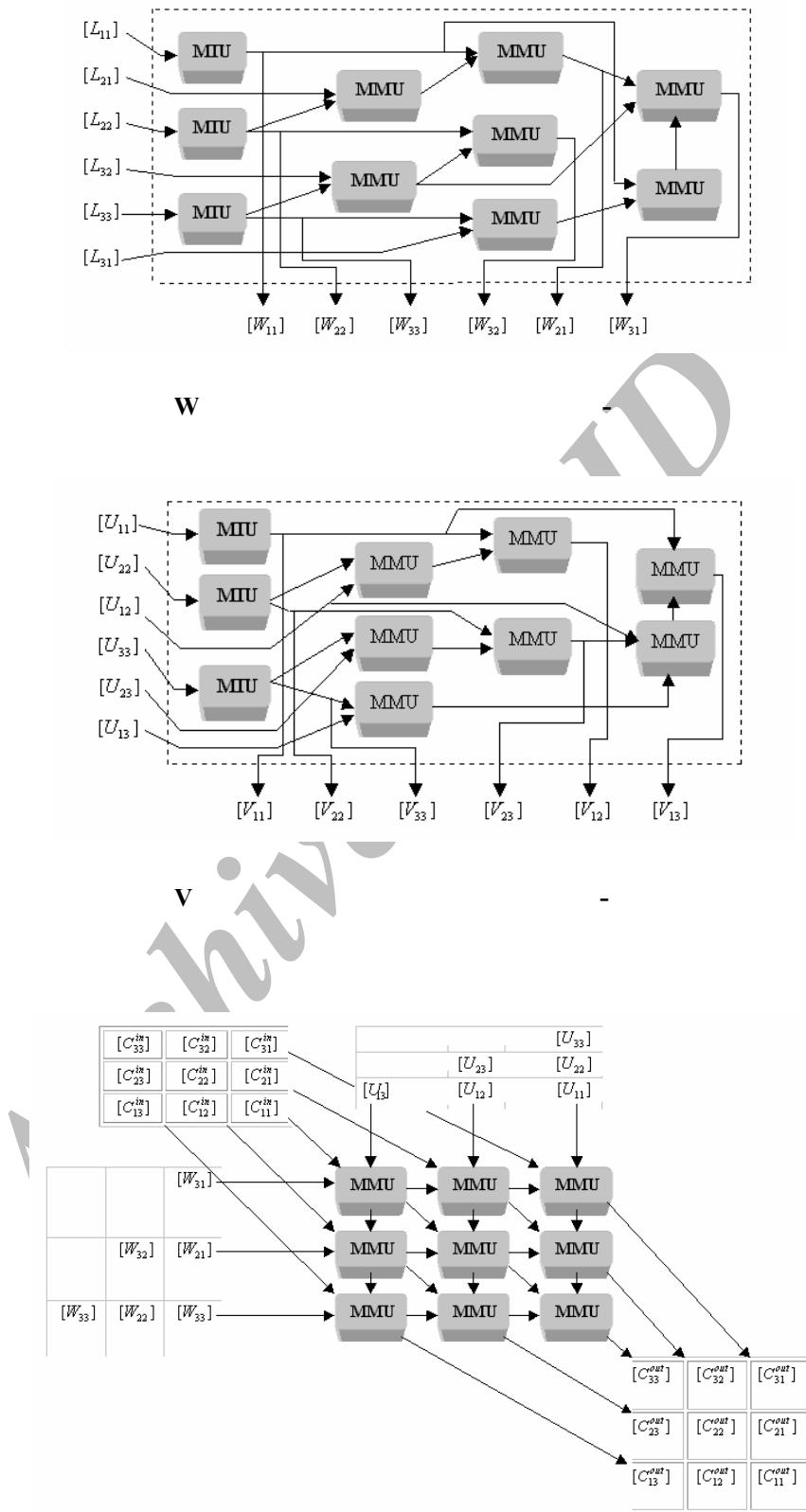


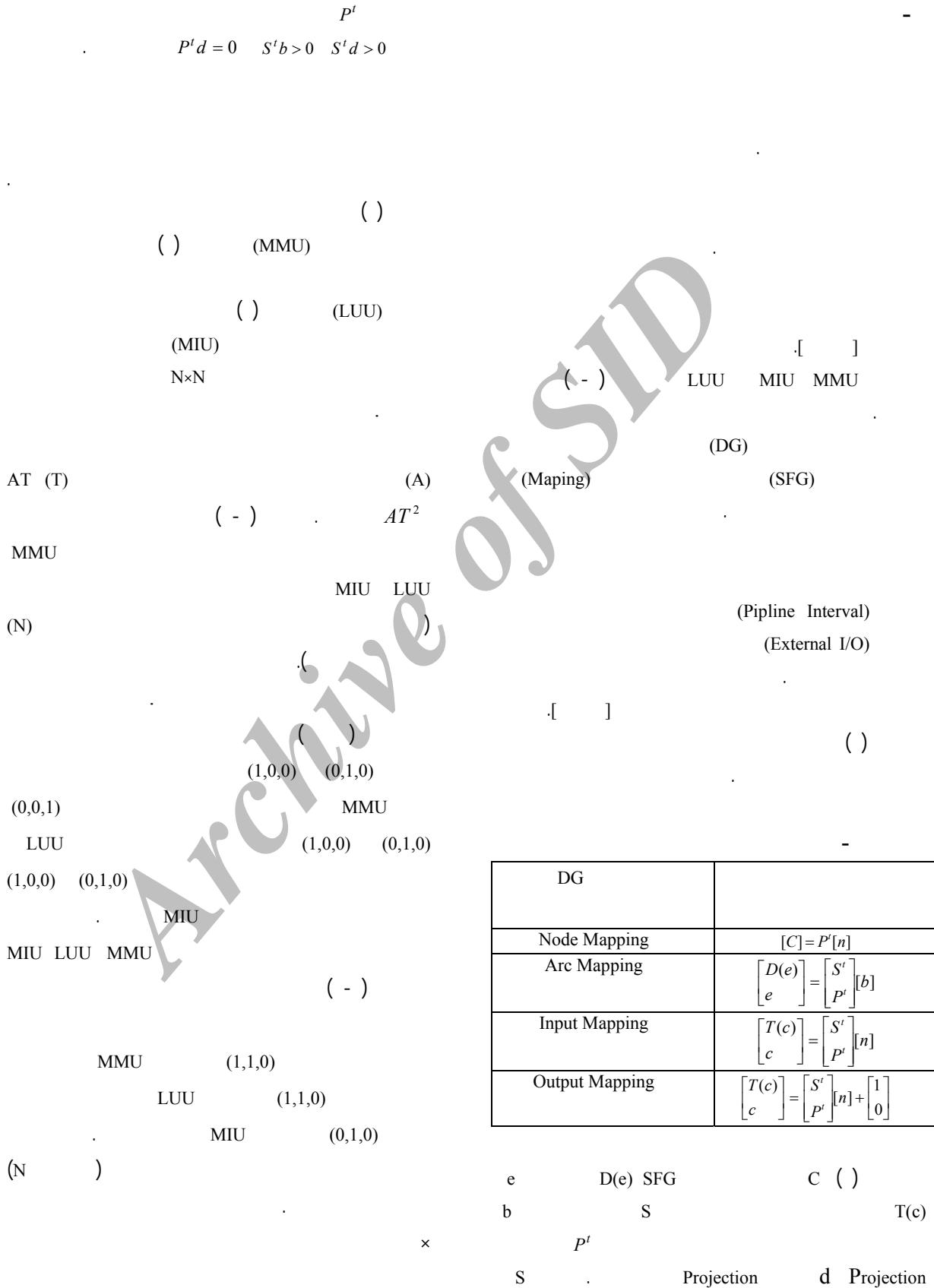
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U L  $\times$   
 $K=3$  ( ) ( ) . )  $\times$   
 U  $\Delta TOA$   $\times$

( ) L K=3



 $\Delta \text{TOA}^{-1}$



x

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(N\*N )

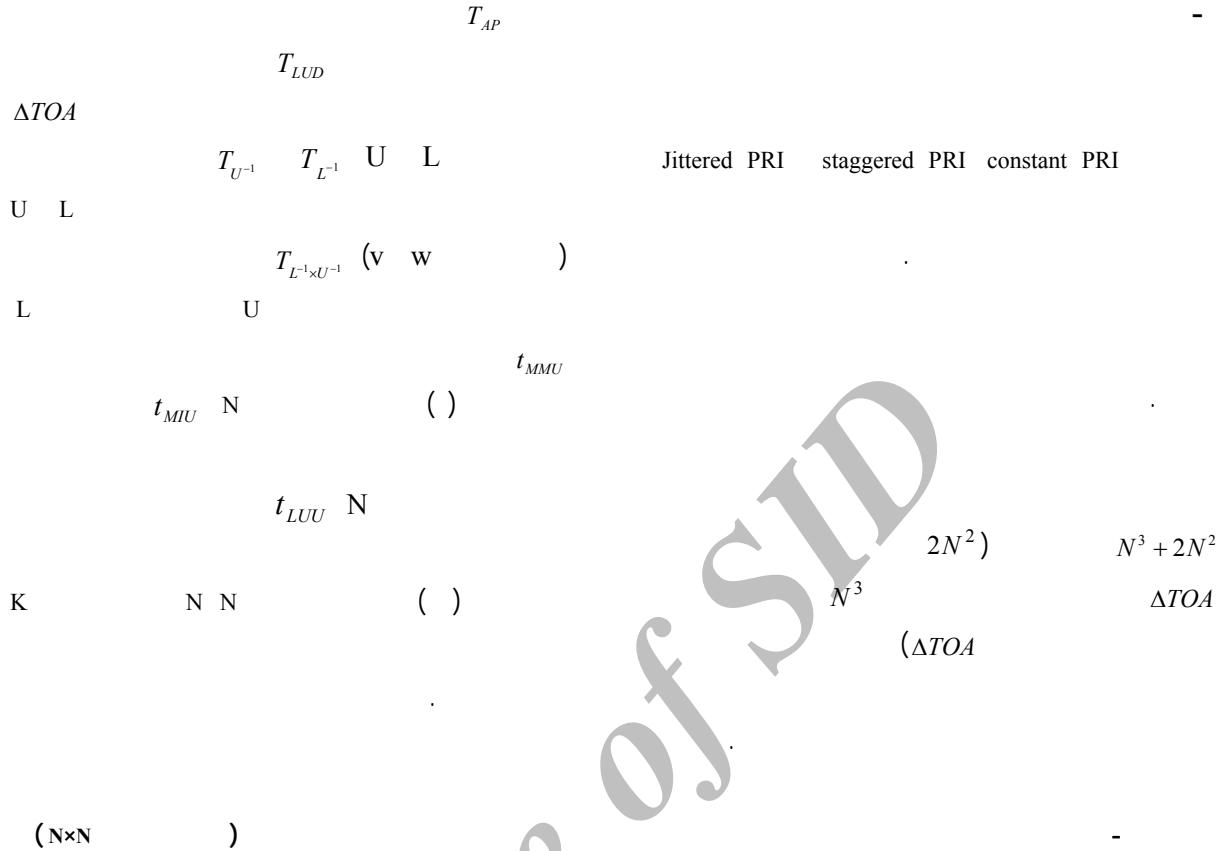
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(Effectiveness)	(Speedup)	(External I/O)	(Pipeline interval)	(Project)
$\frac{N}{3N-2}$	$\frac{N^3}{3N-2}$	2N	1	(0,0,1)
$\frac{N}{3N-2}$	$\frac{N^3}{3N-2}$	3N	1	(0,1,0)
$\frac{N}{3N-2}$	$\frac{N^3}{3N-2}$	3N	1	(1,0,0)
$\frac{N^3}{(3N-2)(2N^2-N)}$	$\frac{N^3}{3N-2}$	6N-2	2	(1,1,0)
$\frac{N^3}{(3N-2)(2N^2-N)}$	$\frac{N^3}{3N-2}$	5N-1	2	(0,1,-1)
$\frac{N^3}{(3N-2)(2N^2-N)}$	$\frac{N^3}{3N-2}$	5N-1	2	(-1,0,1)
$\frac{N^3}{(3N-2)(3N^2-3N+1)}$	$\frac{N^3}{3N-2}$	8N-4	1	(1,1,1)
$\frac{N^3}{(3N-2)(3N^2-3N+1)}$	$\frac{N^3}{3N-2}$	8N-4	1	(1,-1,1)
$\frac{N^3}{(3N-2)(3N^2-3N+1)}$	$\frac{N^3}{3N-2}$	8N-4	1	(-1,1,1)
$\frac{N^3}{(3N-2)(3N^2-3N+1)}$	$\frac{N^3}{3N-2}$	8N-4	3	(1,1,-1)

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(Effectiveness)	(Speedup)	(External I/O)	(Pipeline interval)			
$\frac{11N}{3N^3-2N^2}$	$\frac{11N}{3N-2}$	2N-1	1	N	$N^2 - N$	(0,0,1)
$\frac{11N}{1.5N^3 + 0.5N^2 - N}$	$\frac{11N}{3N-2}$	2N-1	1	1	$0.5N^2 + 0.5N - 1$	(0,1,0)
$\frac{11N}{3N^3-2N^2}$	$\frac{11N}{3N-2}$	3N-1	2	N	$N^2 - N$	(0,1,1)
$\frac{11N}{1.5N^3 + 0.5N^2 - N}$	$\frac{11N}{3N-2}$	2N	1	N	$0.5N^2 - 0.5N$	(1,0,0)
$\frac{11N}{3N^3-2N^2}$	$\frac{11N}{3N-2}$	3N-1	2	N	$N^2 - N$	(1,0,1)
$\frac{11N}{3N^3-2N^2}$	$\frac{11N}{3N-2}$	4N-2	2	N	$N^2 - N$	(1,1,0)
$\frac{11N}{3N^3-2N^2}$	$\frac{11N}{3N-2}$	4N-2	3	N	$N^2 - N$	(1,1,1)
$\frac{11N}{4.5N^3 - 4.5N^2 + N}$	$\frac{11N}{3N-2}$	5N-4	1	N+1	$1.5N^2 - 1.5N - 1$	(1,-1,1)
$\frac{11N}{4.5N^3 - 7.5N^2 + 6N - 2}$	$\frac{11N}{3N-2}$	5N-3	1	2N-1	$1.5N^2 - 3.5N + 2$	(-1,1,1)
$\frac{11N}{6N^3 - 10N^2 + 7N - 2}$	$\frac{11N}{3N-2}$	6N-5	1	2N-1	$2N^2 - 4N + 2$	(1,1,-1)



(Effectiveness)	(Speedup) (External I/O)	(Pipeline interval)				
$\frac{N^3 + 2N}{15N^3 - 6N^2}$	$\frac{N^3 + 2N}{5N - 2}$	0	1	$4N - 2$	$3N^2 - 4N + 2$	(0,0,1)
$\frac{N^3 + 2N}{5N^3 + 3N^2 - 2N}$	$\frac{N^3 + 2N}{5N - 2}$	$2N$	1	0	$N^2 + N$	(0,1,0)
$\frac{N^3 + 2N}{10N^3 + 6N^2 - 9N + 2}$	$\frac{N^3 + 2N}{5N - 2}$	$2N$	2	$3N - 1$	$2N^2 - N$	(0,1,1)
$\frac{N^3 + 2N}{5N^3 + 3N^2 - 2N}$	$\frac{N^3 + 2N}{5N - 2}$	$2N$	1	N	$N^2$	(1,0,0)
$\frac{N^3 + 2N}{10N^3 + 6N^2 - 9N + 2}$	$\frac{N^3 + 2N}{5N - 2}$	$2N$	2	$2N$	$2N^2 - 1$	(1,0,1)
$\frac{N^3 + 2N}{10N^3 - 4N^2}$	$\frac{N^3 + 2N}{5N - 2}$	$4N - 2$	2	$2N$	$2N^2 - 2N$	(1,1,0)
$\frac{N^3 + 2N}{5N^3 + 8N^2 - 4N}$	$\frac{N^3 + 2N}{5N - 2}$	$4N - 2$	3	$2N$	$N^2$	(1,1,1)
$\frac{N^3 + 2N}{15N^3 + 4N^2 - 14N + 4}$	$\frac{N^3 + 2N}{5N - 2}$	$4N - 2$	1	$3N - 1$	$3N^2 - N - 1$	(1,-1,1)
$\frac{N^3 + 2N}{15N^3 + 4N^2 - 14N + 4}$	$\frac{N^3 + 2N}{5N - 2}$	$4N - 2$	1	$4N - 2$	$3N^2 - 2N$	(-1,1,1)
$\frac{N^3 + 2N}{25N^3 - 25N^2 + 11N - 2}$	$\frac{N^3 + 2N}{5N - 2}$	$4N - 2$	1	$6N - 4$	$5N^2 - 9N + 5$	(1,1,-1)

( N×N )

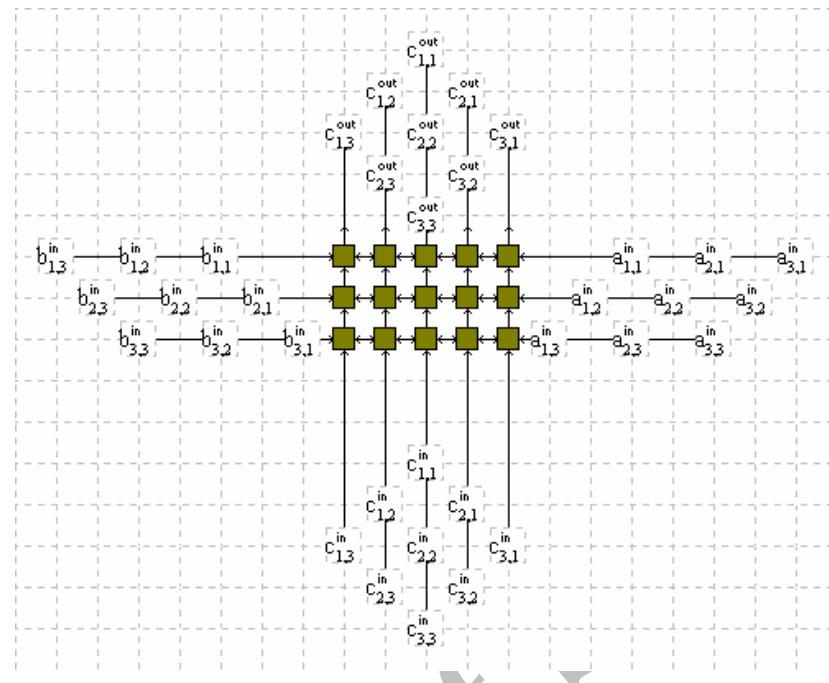
$AT^2$	$AT$	$T$	$A$	-
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(0,0,1)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(0,1,0)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(1,0,0)
$18N^4 - 33N^3 + 20N^2 - 4N$	$6N^3 - 7N^2 + 2N$	$3N - 2$	$2N^2 - N$	(1,1,0)
$18N^4 - 33N^3 + 20N^2 - 4N$	$6N^3 - 7N^2 + 2N$	$3N - 2$	$2N^2 - N$	(0,1,-1)
$18N^4 - 33N^3 + 20N^2 - 4N$	$6N^3 - 7N^2 + 2N$	$3N - 2$	$2N^2 - N$	(-1,0,1)
$27N^4 - 63N^3 + 57N^2 - 24N + 4$	$9N^3 - 15N^2 + 9N - 2$	$3N - 2$	$3N^2 - 3N + 1$	(1,1,1)
$27N^4 - 63N^3 + 57N^2 - 24N + 4$	$9N^3 - 15N^2 + 9N - 2$	$3N - 2$	$3N^2 - 3N + 1$	(1,-1,1)
$27N^4 - 63N^3 + 57N^2 - 24N + 4$	$9N^3 - 15N^2 + 9N - 2$	$3N - 2$	$3N^2 - 3N + 1$	(-1,1,1)
$27N^4 - 63N^3 + 57N^2 - 24N + 4$	$9N^3 - 15N^2 + 9N - 2$	$3N - 2$	$3N^2 - 3N + 1$	(1,1,-1)

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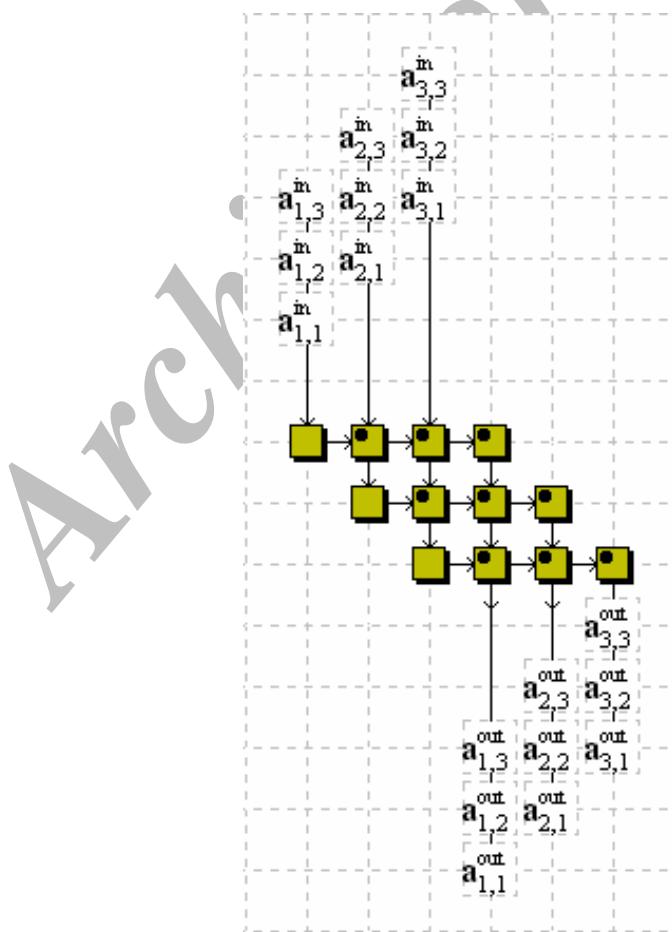
$AT^2$	$AT$	$T$	$A$	-
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(0,0,1)
$4.5N^4 - 1.5N^3 - 4N^2 + 2N$	$1.5N^3 + 0.5N^2 - N$	$3N - 2$	$0.5N^2 + 0.5N$	(0,1,0)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(0,1,1)
$4.5N^4 - 1.5N^3 - 4N^2 + 2N$	$1.5N^3 + 0.5N^2 - N$	$3N - 2$	$0.5N^2 + 0.5N$	(1,0,0)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(1,0,1)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(1,1,0)
$9N^4 - 12N^3 + 4N^2$	$3N^3 - 2N^2$	$3N - 2$	$N^2$	(1,1,1)
$13.5N^4 - 22.5N^3 + 12N^2 - 2N$	$4.5N^3 - 4.5N^2 + N$	$3N - 2$	$1.5N^2 - 0.5N$	(1,-1,1)
$13.5N^4 - 31.5N^3 + 33N^2 - 18N + 4$	$4.5N^3 - 7.5N^2 + 6N - 2$	$3N - 2$	$1.5N^2 - 1.5N + 1$	(-1,1,1)
$18N^4 - 42N^3 + 41N^2 - 20N + 4$	$6N^3 - 10N^2 + 7N - 2$	$3N - 2$	$2N^2 - 2N + 1$	(1,1,-1)

( N×N )

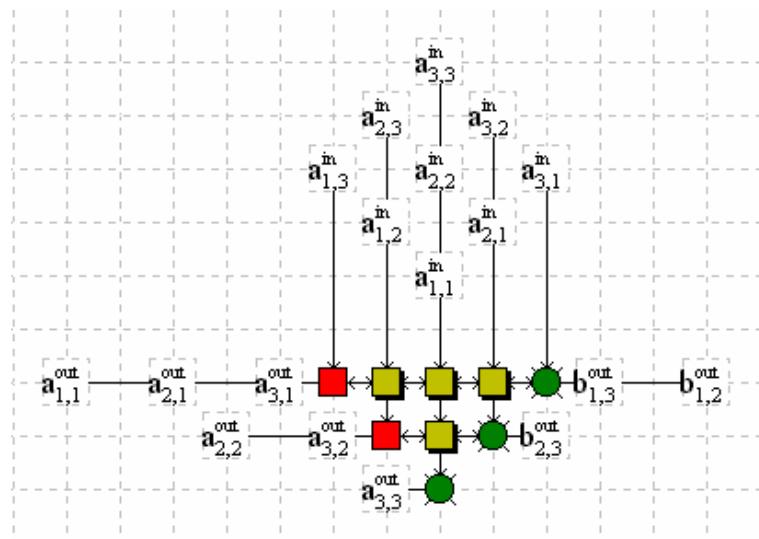
$AT^2$	$AT$	$T$	$A$	-
$75N^4 - 60N^3 + 12N^2$	$15N^3 - 6N^2$	$5N - 2$	$3N^2$	(0,0,1)
$25N^4 + 5N^3 - 16N^2 + 4N$	$5N^3 + 3N^2 - 2N$	$5N - 2$	$N^2 + N$	(0,1,0)
$50N^4 + 10N^3 - 57N^2 + 28N - 4$	$10N^3 + 6N^2 - 9N + 2$	$5N - 2$	$2N^2 + 2N - 1$	(0,1,1)
$25N^4 + 5N^3 - 16N^2 + 4N$	$5N^3 + 3N^2 - 2N$	$5N - 2$	$N^2 + N$	(1,0,0)
$50N^4 + 10N^3 - 57N^2 + 28N - 4$	$10N^3 + 6N^2 - 9N + 2$	$5N - 2$	$2N^2 + 2N - 1$	(1,0,1)
$25N^4 + 30N^3 - 36N^2 + 8N$	$5N^3 + 8N^2 - 4N$	$5N - 2$	$N^2 + 2N$	(1,1,1)
$75N^4 - 10N^3 - 78N^2 + 48N - 8$	$15N^3 + 4N^2 - 14N + 4$	$5N - 2$	$3N^2 + 2N - 2$	(1,-1,1)
$75N^4 - 10N^3 - 78N^2 + 48N - 8$	$15N^3 + 4N^2 - 14N + 4$	$5N - 2$	$3N^2 + 2N - 2$	(-1,1,1)
$125N^4 - 175N^3 + 105N^2 - 32N + 4$	$25N^3 - 25N^2 + 11N - 2$	$5N - 2$	$5N^2 - 3N + 1$	(1,1,-1)

 $N = 3 \quad (1,1,0)$ 

(MMU)

 $N = 3 \quad (1,1,0)$ 

(MIU)

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$$N = 3 \quad (1,1,0)$$

N

$$T_{AP} = T_{LUD} + T_{L^{-1}} + T_{U^{-1} \times L^{-1}} \quad (1)$$

$$T_{LUD} = 3t_{LUU} + 2t_{MIU} + 4t_{mmu} \quad (2)$$

$$T_{L^{-1}} = t_{MIU} + 4t_{mmu} \quad (3)$$

$$T_{U^{-1} \times L^{-1}} = (3 \frac{N}{K} - 2)t_{MMU} \quad (4)$$

$$T_{AP} = (\frac{3N}{K} + 6)t_{MMU} + 3t_{MIU} + 3t_{LUU} \quad (5)$$

$$t_{LUU} = 3\frac{N}{K} - 2 \quad t_{MMU} = 3\frac{N}{K} - 2 \quad t_{MIU} = 5\frac{N}{K} - 2 \quad (6)$$

$$T_{AP} = \frac{9}{K}N^2 + (42 - \frac{6}{K})N - 24 \quad (7)$$

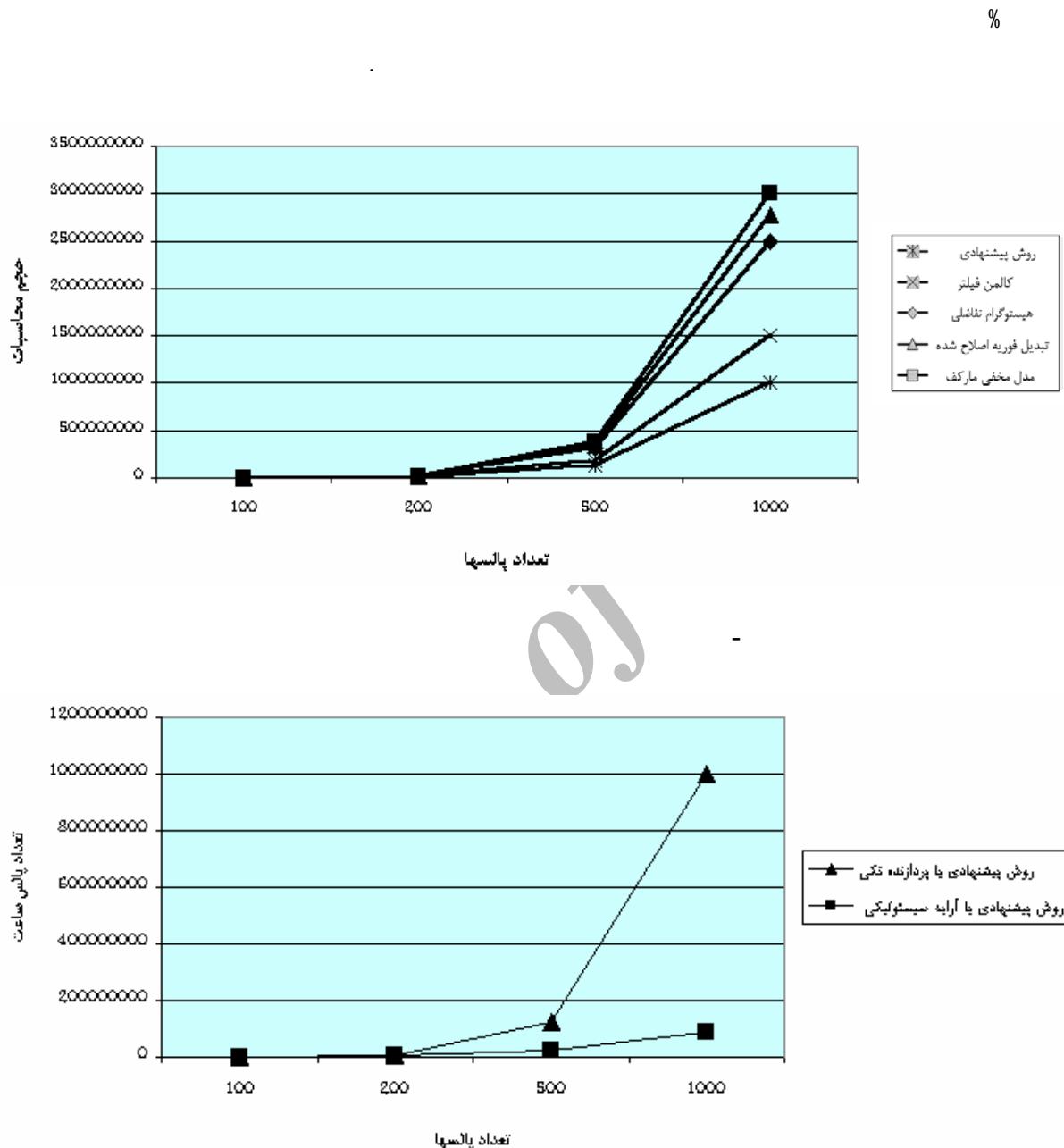
$$Speedup = \frac{N^3 + 2N^2}{\frac{9}{K}N^2 + (42 - \frac{6}{K})N - 24} \quad (8)$$

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$$T_{AP} = \frac{9}{K}N^2 + (42 - \frac{6}{K})N - 24$$



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