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## **Quintasymptotic sequences over an ideal and quintasymptotic cograde**

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### **Abstract**

Let  $I$  denote an ideal of a Noetherian ring  $R$ . The purpose of this talk is to introduce the concepts of quintasymptotic sequences over  $I$  and quintasymptotic cograde of  $I$ , and it is shown that they play a role analogous to quintessential sequences over  $I$  and quintessential cograde of  $I$ . Also, we show that, if  $R$  is local, then the quintasymptotic cograde of  $I$  is unambiguously defined and behaves well when passing to certain related local rings. Finally, we use this cograde to characterize two classes of local rings.